

# Related problems on Homogeneous differential equations of first order and first degree

**SUBJECT : (MATHEMATICS)**  
**CHAPTER NUMBER: 09**  
**CHAPTER NAME : Differential Equations**

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# Problems on Homogeneous differential Equations of first order and first degree

Show that the differential equation  $x \cos\left(\frac{y}{x}\right) \frac{dy}{dx} = y \cos\left(\frac{y}{x}\right) + x$  is homogeneous and solve it.

## Example

Show that the differential equation  $2ye^{\frac{x}{y}}dy + \left(y - 2xe^{\frac{x}{y}}\right)dx = 0$  is homogeneous. Find the particular solution of this differential equation, given that  $x = 0$ , when  $y = 1$ .

## Example

Show that the family of curves for which  $\frac{dy}{dx} = \frac{x^2+y^2}{2xy}$  is given by  $x^2 - y^2 = cx$ .

## Example

Solve the differential equation  $y \left\{ x \cos \left( \frac{y}{x} \right) + y \sin \left( \frac{y}{x} \right) \right\} dx - x \left\{ y \sin \left( \frac{y}{x} \right) - x \cos \left( \frac{y}{x} \right) \right\} dy = 0$

## Example

Solve the differential equation  $(1 + e^{\frac{x}{y}})dx + e^{\frac{x}{y}}(1 - \frac{x}{y})dy = 0$ .

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## Example

Solve the initial value problem  $2x^2 \frac{dy}{dx} - 2xy + y^2 = 0, y(e) = e$ .



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