

Integration By Parts

SUBJECT : MATHEMATICS
CHAPTER NUMBER:7
CHAPTER NAME :INTEGRALS

CHANGING YOUR TOMORROW

Rule of By Parts (Product Rule)

let u and v be two differentiate functions of a single variable x , then the integral of the product of these two functions denoted as $\int u \cdot v \, dx$ and defined as

$$\int u \cdot v \, dx = u \int v \, dx - \int \left(\frac{d}{dx}(u) \int v \, dx \right) dx.$$

If in the product two functions are of different types, then take that function as first function (i.e u) which comes first in the word *ILATE*, where,

I: Inverse trigonometric function

L: Logarithmic function

A: Algebraic function

T : Trigonometric function

E: Exponential function

Example

Evaluate the Integral

$$\int x \sin x \, dx$$

Example

Evaluate the Integral

$$\int \log x \, dx$$

Example

Evaluate the Integral

$$\int e^x \cos x \, dx$$

Note:- Above integral can also be determined by taking $\cos x$ as the first function and

e^x the second function.

Example

Evaluate the Integrals

$$(a) \int e^{ax} \cos bx \, dx$$

$$(b) \int e^{ax} \sin bx \, dx$$

Assignments

1. Evaluate the Integrals

$$(a) \int x^2 \sin x \, dx$$

$$(b) \int \sin \sqrt{x} \, dx$$

$$(c) \int (\log x)^2 \, dx$$

$$(d) \int \operatorname{cosec}^3 x \, dx$$

$$(e) \int x \cot^{-1} x \, dx$$

$$(f) \int x^3 \log(2x) \, dx$$

2. Answer the questions from Qno. 1 to 15 Exercise 7.6 from NCERT book.

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