

Random variable and its probability distribution

SUBJECT : (MATHEMATICS)
CHAPTER NUMBER: 13
CHAPTER NAME : PROBABILITY

CHANGING YOUR TOMORROW

Random Variable

Random Variable is a real valued function whose domain in the sample space of random experiment,

Example:-

If we toss two coins, then the sample Space $S = \{HH, HT, TH, TT\}$

If X denotes the number of heads obtained, then X is a random variable and for each outcome its value is given as

$$X(HH) = 2, \quad X(HT) = 1, \quad X(TH) = 1 \text{ and } X(TT) = 0$$

Again,

If Y denotes the number of heads minus the number of tails and for each outcome its value is given as

$$Y(HH) = 2, \quad Y(HT) = 0, \quad Y(TH) = 0, \text{ and } Y(TT) = -2$$

NOTE:

X and Y are two different random variable for same the same sample space.

Discrete random variables:

A random variable that can take only finite or an accountably infinite number of values is called a discrete random variable.

The probability distribution of a random variable:-

If the values of a random variable together with the corresponding probabilities are given, then this description is called a probability distribution of the random variable.

Example:-

Probability distribution when two coins are tossed;
Let X denoted the number of heads occurred then

$$P(X = 0) = \text{probability of occurrence of zero head} = P(TT) = \frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$$

$$P(X = 1) = \text{probability of occurrence of one head} = P(HT) + P(TH) = \frac{1}{2} \times \frac{1}{2} + \frac{1}{2} \times \frac{1}{2} = \frac{1}{2}$$

$$P(X = 2) = \text{probability of occurrence of two heads} = P(HH) = \frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$$

Thus the probability distribution when two coins are tossed is as given below.

X	0	1	2
P(X)	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{1}{4}$

Problem-1

A random variable X has the following probability distribution:

X	0	1	2	3	4	5	6	7
$P(X)$	0	K	$2K$	$2K$	$3K$	K^2	$2K^2$	$7K^2 + K$

Determine

(i) K

(ii) $P(X < 3)$

(iii) $P(X > 6)$

(iv) $P(0 < X < 3)$

Problem-2

From a lot of 30 bulbs which include 6 defectives, a sample of 4 bulbs is drawn at random with replacement. Find the probability distribution of the number of defective bulbs.

Problem- 3

The random variable X has a probability distribution $P(X)$ of the following form, where k is some number:

$$P(X = x) = \begin{cases} k & , \text{if } x = 0 \\ 2k & , \text{if } x = 1 \\ 3k & , \text{if } x = 2 \\ 0 & , \text{otherwise} \end{cases}$$

(i) Determine the value of k

(ii) Find $P(X < 2)$, $P(X \leq 2)$ and $P(X \geq 2)$

Problem-4

Find the probability distribution of X , the number of heads in two tosses of a coin (or a simultaneous toss of two coins)

Problem- 5

Three cards are drawn from a pack of 52 playing cards. Find the probability distribution of the number of aces.

Problem-6

An urn contains 4 white and 6 red balls. Four balls are drawn at random from the urn. Find the probability distribution of the number of white balls

HOME ASSIGNMENT

- Q1. Four bad oranges are mixed accidentally with 16 good oranges. Find the Probability distribution of the number of bad oranges in a draw of two oranges.
- Q2. We take 8 identical slips of paper, write the number 0 on one of them, the number 1 on three of the slips, the number 2 on three of the slips and the number 3 on one of the slips. These slips are folded, put in a box and thoroughly mixed. One slip is drawn at random from the box. If X is the random variable denoting the number written on the drawn slip, Find the probability distribution of X .
- Q3. A coin is biased so that the head is 3 times as likely to occur as tail. If the coin is tossed twice, Find the probability distribution of number of tails.

THANKING YOU

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