

**SUBTOPIC: BASIC CONCEPT, ELEMENTS OF A SET,
REPRESENTATION OF A SET**

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 13

CHAPTER NAME : SET CONCEPTS

CHANGING YOUR TOMORROW

Learning outcomes

Students will be able to

- define a set.
- elements of a set
- represent a set in description method, roster method , set builder/ rule method.
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PREVIOUS CONNECT

- Cite collection of well defined objects.

BASIC CONCEPT

A set is a well-defined collection of distinct objects, things or symbols.

Set and Elements of a Set

The collection of tall students of a class is not well-defined, so it **does not form a set**.

The collection of students of a class with heights between 135 cm and 160 cm is well-defined, so it forms a set.



ELEMENTS OF A SET

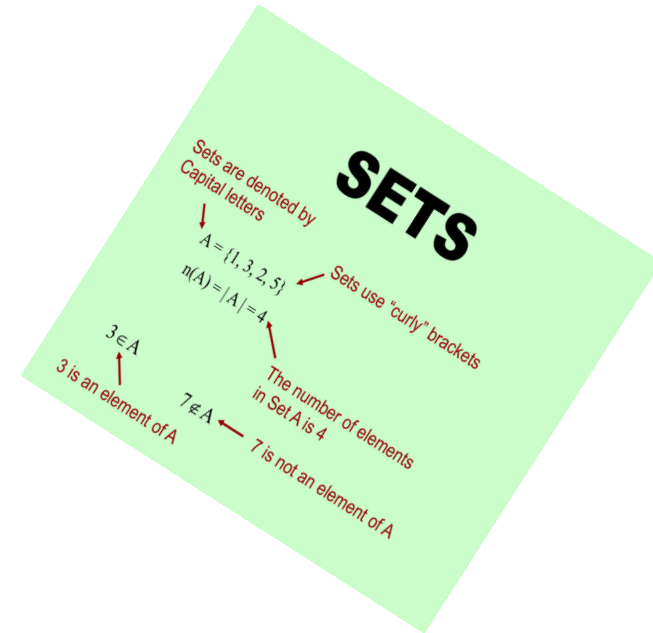
The objects used to form a set are called elements or members of the set.

Set A = {5,10, 12 , 15}

USE OF THE SYMBOL ' \in ' or SYMBOL \notin

The elements in a set can be written in any order.

The elements in a set should not be repeated .



REPRESENTATION OF A SET

DESCRIPTION METHOD (FORM): A well defined description about the set is given.

ROSTER /TABULAR METHOD : The elements of the set are written inside a pair of curly brackets and are separated by commas.

Descriptive Form	Set - Builder Form	Roster Form
The set of all vowels in English alphabet	$\{x : x \text{ is a vowel in the English alphabet}\}$	$\{a, e, i, o, u\}$
The set of all odd positive integers less than or equal to 15	$\{x : x \text{ is an odd number and } 0 < x \leq 15\}$	$\{1, 3, 5, 7, 9, 11, 13, 15\}$
The set of all positive cube numbers less than 100	$\{x : x \text{ is a cube number and } 0 < x < 100\}$	$\{1, 8, 27, 64\}$

TABULAR /ROSTER METHOD (FORM)

The actual elements of the sets are not written , but a rule or statement or a formula is written in the briefest possible way.

EVALUATION QUESTIONS

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1. Find, whether or not, each of the following collections represent a set:

- (i) The collection of good students in your school.**
- (ii) The collection of the numbers between 30 and 45.**
- (iii) The collection of fat-people in your colony.**
- (iv) The collection of interesting books in your school library.**
- (v) The collection of books in the library and are of your interest.**



Solution:

- (i) The collection of good students in your school is not a set as it is not well defined.

- (ii) The collection of the numbers between 30 and 45 is a set.

- (iii) The collection of fat-people in your colony is not a set as it is not well defined.

- (iv) The collection of interesting books in your school library is not a set as it is not well defined.

- (v) The collection of books in the library and are of your interest is a set.

2. State whether true or false:

(i) Set {4, 5, 8} is same as the set {5, 4, 8} and the set {8, 4, 5}

(ii) Sets {a, b, m, n} and {a, a, m, b, n, n} are same.

(iii) Set of letters in the word 'suchismita' is {s, u, c, h, i, m, t, a}

(iv) Set of letters in the word 'MAHMOOD' is {M, A, H, O, D}.

Solution:

(i) It is true.

(ii) It is true.

(iii) It is true as $\{s, u, c, h, i, s, m, i, t, a\} = \{s, u, c, h, i, m, t, a\}$

(iv) It is true as it has the same elements.



3. Let set $A = \{6, 8, 10, 12\}$ and set $B = \{3, 9, 15, 18\}$.

Insert the symbol ' \in ' or ' \notin ' to make each of the following true :

(i) $6 \dots A$

(ii) $10 \dots B$

(iii) $18 \dots B$

(iv) $(6 + 3) \dots B$

(v) $(15 - 9) \dots B$

(vi) $12 \dots A$

(vii) $(6 + 8) \dots A$

(viii) $6 \text{ and } 8 \dots A$

Solution:

(i) $6 \in A$

(ii) $10 \notin B$

(iii) $18 \in B$

(iv) $(6 + 3)$ or $9 \in B$

(v) $(15 - 9)$ or $6 \notin B$

(vi) $12 \in A$

(vii) $(6 + 8)$ or $14 \notin A$

(viii) 6 and $8 \in A$

4. Express each of the following sets in roster form :

(i) Set of odd whole numbers between 15 and 27.

(ii) A = Set of letters in the word “CHITAMBARAM”

(iii) B = {All even numbers from 15 to 26}

(iv) P = {x : x is a vowel used in the word ‘ARITHMETIC’}

(v) S = {Squares of first eight whole numbers}

(vi) Set of all integers between 7 and 94; which are divisible by 6.

(vii) C = {All composite numbers between 2 and 20}

(viii) D = Set of Prime numbers from 2 to 23.

(ix) E = Set of natural numbers below 30 which are divisible by 2 or 5.

(x) F = Set of factors of 24.

(xi) G = Set of names of three closed figures in Geometry.

Solution:

(i) $\{17, 19, 21, 23, 25\}$

(ii) $A = \{C, H, I, T, A, M, B, R\}$

(iii) $B = \{16, 18, 20, 22, 24, 26\}$

(iv) $P = \{a, e, i\}$

(v) $S = \{0, 1, 4, 9, 16, 25, 36, 49\}$

(vi) $\{12, 18, 24, 30, 36, 42, 48, 54, 60, 66, 72, 78, 84, 90\}$

(vii) $C = \{4, 6, 8, 9, 10, 12, 14, 15, 16, 18\}$

(viii) $D = \{2, 3, 5, 7, 11, 13, 17, 19, 23\}$

(ix) $E = \{2, 4, 5, 6, 8, 10, 12, 14, 15, 16, 18, 20, 22, 24, 25, 26, 28\}$

(x) $F = \{1, 2, 3, 4, 6, 8, 12, 24\}$

(

xi) $G = \{\text{Triangle, Circle, Square}\}$

(xii) $H = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$

(xiii) $2x - 3 \leq 17$

$$2x \leq 17 + 3$$

$$2x \leq 20$$

$$x \leq 20/2$$

$$x \leq 10$$

Here $J = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

(xiv) $-3 < x < 5$

We know that x lies between -3 and 5

$K = \{-2, -1, 0, 1, 2, 3, 4\}$

5. Express each of the following sets in set-builder notation (form):

(i) {3, 6, 9, 12, 15}

(ii) {2, 3, 5, 7, 11, 13 }

(iii) {1, 4, 9, 16, 25, 36}

(iv) {0, 2, 4, 6, 8, 10, 12, }

(v) {Monday, Tuesday, Wednesday}

(vi) {23, 25, 27, 29, ... }

(vii) {1/3, 1/4, 1/5, 1/6, 1/7, 1/8}

(viii) {42, 49, 56, 63, 70, 77}

Solution:

(i) {3, 6, 9, 12, 15}

It can be written as

= {x: x is a natural number divisible by 3; $x < 18$ }

(ii) {2, 3, 5, 7, 11, 13}

It can be written as

= {x: x is a prime number}

(iii) {1, 4, 9, 16, 25, 36}

It can be written as

= {x: x is a perfect square natural number; $x \leq 36$ }

(iv) {0, 2, 4, 6, 8, 10, 12,}

It can be written as

= {x: x is a whole number divisible by 2}

(v) {Monday, Tuesday, Wednesday}

It can be written as

= {x: x is one of the first three days of the week}

vi) $\{23, 25, 27, 29, \dots\}$

It can be written as

$= \{x: x \text{ is an odd natural number; } x \geq 23\}$

(vii) $\{1/3, 1/4, 1/5, 1/6, 1/7, 1/8\}$

It can be written as

$= \{x: x = 1/n \text{ when } n \text{ is a natural number; } 3 \leq n \leq 8\}$

(viii) $\{42, 49, 56, 63, 70, 77\}$

It can be written as

$= \{x: x \text{ is a natural number divisible by } 7; 42 \leq x \leq 77\}$

6. Given: $A = \{x : x \text{ is a multiple of } 2 \text{ and is less than } 25\}$

$B = \{x : x \text{ is a square of a natural number and is less than } 25\}$

$C = \{x : x \text{ is a multiple of } 3 \text{ and is less than } 25\}$

$D = \{x : x \text{ is a prime number less than } 25\}$

Write the sets A, B, C and D in roster form.

Solution:

$A = \{x : x \text{ is a multiple of } 2 \text{ and is less than } 25\} = \{2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24\}$

$B = \{x : x \text{ is a square of a natural number and is less than } 25\} = \{1, 4, 9, 16\}$

$C = \{x : x \text{ is a multiple of } 3 \text{ and is less than } 25\} = \{3, 6, 9, 12, 15, 18, 21, 24\}$

$D = \{x : x \text{ is a prime number less than } 25\} = \{2, 3, 5, 7, 11, 13, 17, 19, 23\}$

HOMework

EX 13A

THANKING YOU
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