

Example 8 :

If the side of an equilateral triangle is $2a$, find the coordinate of its vertices.

Sol. In figure, OAB is an equilateral triangle of $2a$.

$$\therefore OA = AB = OB = 2a$$

Now, from the point B, draw BM perpendicular on OA.

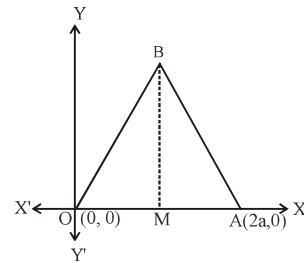
$$\therefore OM = MA = a$$

Therefore from right triangle OMB,

$$OB^2 = OM^2 + MB^2 \text{ or } (2a)^2 = (a)^2 + MB^2 \quad \text{or } MB^2 = 3a^2 \quad \therefore MB = \sqrt{3}a$$

Hence the coordinates of vertices of equilateral triangle are O (0, 0), A (2a, 0) and B(a, $\sqrt{3}a$)

because $OM = a$ and $MB = \sqrt{3}a$


QUESTION BANK
EXERCISE - 1

- Q.1** Explain Cartesian system briefly.
- Q.2** What are quadrants in a Cartesian plane.
- Q.3** What is the name of horizontal and vertical lines drawn in Cartesian plane to determine the position of a point? Name each part of plane and name of point of intersection.
- Q.4** What are the coordinates of the origin.
- Q.5** Write the answer of each of the following questions :
- (i) What is the name of horizontal and the vertical lines drawn to determine the position of any point in the Cartesian plane
- (ii) What is the name of each part of the plane formed by these two lines?
- (iii) Write the name of the point where these two lines intersect.
- Q.6** In which quadrant or on which axis do each of the points $(-2, 4)$, $(3, -1)$, $(-1, 0)$, $(1, 2)$ and $(-3, -5)$ lie? Verify your answer by locating them on the Cartesian plane.
- Q.7** Taking rectangular axes, plot the points O (0, 0), P (3, 0) and R (0, 4). Find the coordinate of the fourth point Q such that OPQR forms a rectangle.
- Q.8** If the coordinates of the mid points of the sides of a triangle are $(1, 2)$, $(0, -1)$ and $(2, -1)$. Find the coordinate of its vertices.
- Q.9** Plot the points A, B, C, D, E from the table given below :

Point	A	B	C	D	E
Abscissa	-7	-3	5	2	-3
Ordinate	2	0	-4	2	+2

and answer the following :

- (i) Coordinates of A, B, C, D, E? (ii) Measure AC, DC, AD?
- (iii) Shade the triangle. (iv) Verify that $AD + DC > AC$.

EXERCISE - 2

- Q.1** A $(-2, 4)$, C $(4, 10)$ and D $(-2, 10)$ are the vertices of a squares ABCD. Use graphical method to find the co-ordinates of the fourth vertex B. Also, find :
- (i) the co-ordinates of the mid-point of BC
- (ii) the co-ordinates of the mid-point of CD
- (iii) the co-ordinates of the point of intersection of the diagonals of the square ABCD.

- Q.2** Find the co-ordinate of the image of each of the following points under reflection in the origin.
 (i) (2, -3) (ii) (-7, 2) (iii) (-3, -6) (iv) (2, 1/2) (v) (5/2, 0) (vi) (0, 9)
- Q.3** Which of the following points do not lie in any quadrants? (3, 4), (0, 5), (6, 9), (4, 0)
- Q.4** Draw the quadrilateral with vertices (-4, 4), (-6, 0), (-4, -4), (-2, 0). Name the type of quadrilateral and find its area.

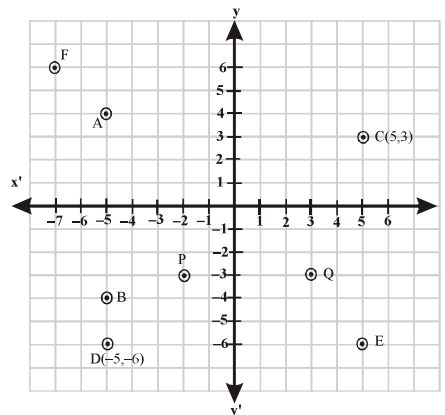
EXERCISE - 3

Fill in the blanks –

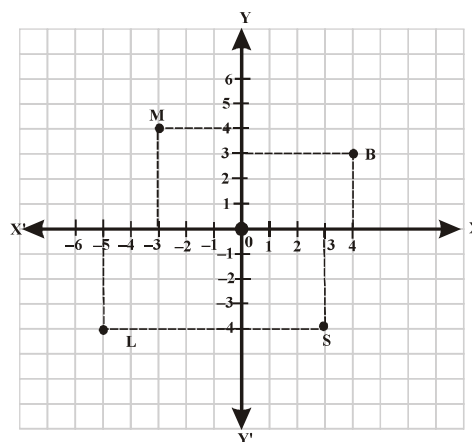
- Q.1** Draw a quadrilateral whose vertices are (1, 4), (-5, 4), (-5, -3) and (1, -3). The type of quadrilateral is
- Q.2** The points (-2, 0), (2, 0), (2, 2), (0, 4), (-2, 2) are joined in order. Figure is
- Q.3** The opposite vertices of a square are (5, 4) and (-3, 2) the length of its diagonal is
- Q.4** One end of a line is (4, 0) and the mid point is (4, 1). Are the coordinates of the other end
- Q.5** If P (2, -1), Q (3, 4), R (-2, 3) and S (-3, -2) be four points in the plane, PQRS is a
- True-False Statement :**
- Q.6** The ordinate of a point is its x-coordinate.
- Q.7** The point (a, b) lies on y-axis if $b = 0$
- Q.8** The origin is in the first quadrant.
- Q.9** The origin (0, 0) lies on x-axis.
- Q.10** If the ordinate of a point is equal to its abscissa, the point lies either in the first quadrant or in the second quadrant.
- Q.11** The y-axis is the vertical number line.
- Q.12** Every point is located in one of the four quadrant.

EXERCISE - 4

- Q.1** The quadrilateral, whose vertices are (-1, 1), (0, -3), (5, 2) and (4, 6) is –
 (A) a square (B) a rectangle (C) a rhombus (D) a parallelogram
- Q.2** The distance between two points (0, 3) and (-2, 0) is –
 (A) $\sqrt{14}$ (B) $\sqrt{15}$ (C) $\sqrt{13}$ (D) $\sqrt{5}$
- Q.3** The distance of the point (3, 4) from y-axis is –
 (A) 1 (B) 4 (C) 2 (D) 3
- Q.4** The triangle, whose vertices are (2, 1), (2, -2) and (5, 2) is –
 (A) Right angled triangle (B) Equilateral triangle
 (C) Isosceles (D) None of them
- Q.5** The distance of the point (5, -2) from x-axis is –
 (A) 5 (B) -2 (C) 3 (D) 2
- Q.6** In the given figure, find Coordinate of A –
 (A) (-5, 4) (B) (5, 4)
 (C) (-5, -4) (D) (4, 5)
- Q.7** In the given figure, points identified by the coordinates (-2, -3)
 (A) P (-2, -3) (B) Q (-2, -3)
 (C) A (-2, -3) (D) C (-2, -3)
- Q.8** In the given figure, find Abscissa of C –
 (A) 4 (B) 5
 (C) 6 (D) 7
- Q.9** In the given figure, find Coordinate of the point E
 (A) (1, 2) (B) (5, -6)
 (C) (5, 6) (D) (-5, -6)



- Q.10** In the figure, the coordinates of B are –
 (A) $(-3, 4)$ (B) $(4, 3)$
 (C) $(-5, -4)$ (D) $(3, -4)$
- Q.11** In the figure, the coordinates of M are –
 (A) $(-3, 4)$ (B) $(4, 3)$
 (C) $(-5, -4)$ (D) $(3, -4)$
- Q.12** In the figure, the coordinates of L are –
 (A) $(-3, 4)$ (B) $(4, 3)$
 (C) $(-5, -4)$ (D) $(3, -4)$
- Q.13** In the figure, the coordinates of S are –
 (A) $(-3, 4)$ (B) $(4, 3)$
 (C) $(-5, -4)$ (D) $(3, -4)$



EXERCISE - 5

Match the column– Each question contains statements given in two columns which have to be matched. Statements (A,B,C,D) in **column I** have to be matched with statements (p, q, r, s) in **column II**.

Q.1 Match the column –

Column I

- (A) abscissa
 (B) ordinate
 (C) coordinate
 (d) origin

Column II

- (p) x
 (q) y
 (r) x, y
 (s) 0

Q.2 Column II give quadrant for points given in column I, match them correctly.

Column I

- (A) 4, 4
 (B) $-3, 7$
 (C) $2, -3$
 (D) $-1, -3$

Column II

- (p) I quadrant
 (q) II quadrant
 (r) III quadrant
 (s) IV quadrant

EXERCISE - 6

PREVIOUS YEAR COMPETITION PROBLEMS

- Q.1** If the distance between the points $(a, 2)$ and $(3, 4)$ be 8, then $a =$
 (A) $2 + 3\sqrt{15}$ (B) $2 - 3\sqrt{15}$ (C) $2 \pm 3\sqrt{15}$ (D) $3 \pm 2\sqrt{15}$
- Q.2** The line $x + y = 4$ divides the line joining the points $(-1, 1)$ and $(5, 7)$ in the ratio –
 (A) $2 : 1$ (B) $1 : 2$ (C) $1 : 2$ externally (D) None of these
- Q.3** If the three vertices of a rectangle taken in order are the points $(2, -2)$, $(8, 4)$ and $(5, 7)$. The coordinates of the fourth vertex is–
 (A) $(1, 1)$ (B) $(1, -1)$ (C) $(-1, 1)$ (D) None of these
- Q.4** If P $(1, 2)$, Q $(4, 6)$, R $(5, 7)$ and S (a, b) are the vertices of a parallelogram PQRS, then –
 (A) $a = 2, b = 4$ (B) $a = 3, b = 4$ (C) $a = 2, b = 3$ (D) $a = 3, b = 5$
- Q.5** If A $(3, 5)$, B $(-3, -4)$, C $(7, 10)$ are the vertices of a parallelogram taken in the order, then the coordinates of the fourth vertex are –
 (A) $(10, 19)$ (B) $(15, 10)$ (C) $(19, 10)$ (D) $(15, 19)$