

MATHEMATICS

CHAPTER NUMBER :~ 6

CHAPTER NAME :~ LINES AND ANGLES

CHANGING YOUR TOMORROW

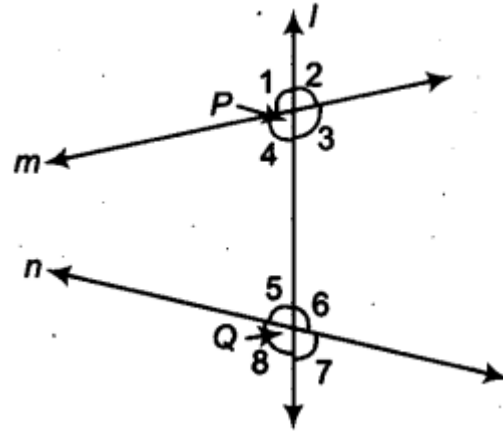
Previous Knowledge Test

1. If 2 lines intersect each other then 2 pairs of vertically opposite angles are produced.
If one of the angles measures 60° , then find the measurements of other angles.

LEARNING OUTCOME:~

1. Students will be able to know the relationship between pairs of corresponding angles and interior opposite angles.
2. Students will be able to learn about the co-interior angles.

Parallel Lines and a Transversal: A line which intersects two or more lines at distinct points is called a transversal.



Here, line l is a transversal of the lines m and n , respectively.

Line l intersects m and n at P and Q respectively, then four angles are formed at each of the points P and Q namely

$\angle 1, \angle 2, \angle 3, \dots, \angle 8$

$\angle 1, \angle 2, \angle 7$ and $\angle 8$ are called exterior angles.

$\angle 3, \angle 4, \angle 5$ and $\angle 6$ are called interior angles.

We classify these eight angles in the following groups

(i) Corresponding angles.

- $\angle 1$ and $\angle 5$
- $\angle 2$ and $\angle 6$
- $\angle 4$ and $\angle 8$
- $\angle 3$ and $\angle 7$

(ii) Alternate interior angles

$\angle 4$ and $\angle 6$

$\angle 3$ and $\angle 5$

(iii) Alternate exterior angles

$\angle 1$ and $\angle 7$

$\angle 2$ and $\angle 8$

(iv) Interior angles on the same side of the transversal

$\angle 4$ and $\angle 5$

$\angle 3$ and $\angle 6$

Note: Interior angles on the same side of the transversal are also referred to as consecutive interior angles or allied angles or co-interior angles.

Theorem 6.2 :-

If a transversal intersects two parallel lines, then each pair of alternate interior angles are equal.

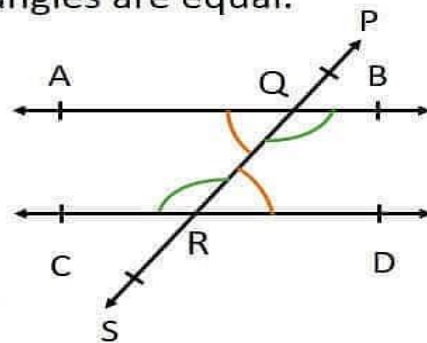
Given :- Two parallel lines AB and CD.

Let PS be the transversal intersecting AB at Q and CD at R.

To Prove :- Each pair of alternate interior angles are equal.

i.e, $\angle BQR = \angle CRQ$

and $\angle AQR = \angle QRD$



Proof :- First, we will prove $\angle BQR = \angle CRQ$

For lines AB & CD,

with transversal PS

$$\angle AQP = \angle CRQ \quad (\text{Corresponding angles}) \dots(1)$$

For lines AB & PS

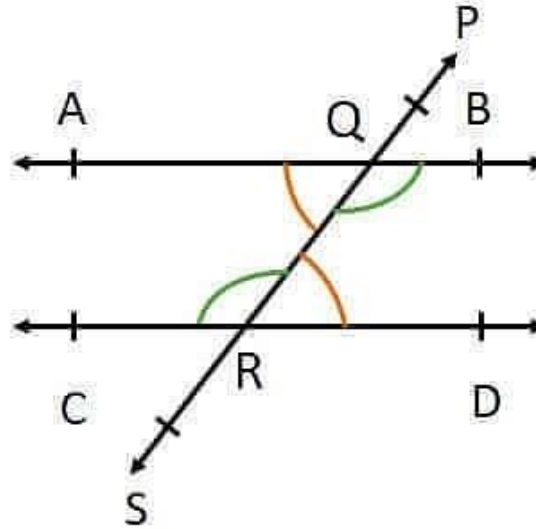
$$\angle AQP = \angle BQR \quad (\text{Vertically opposite angles}) \dots(2)$$

From (1) and (2)

$$\angle BQR = \angle CRQ$$

Similarly we can prove

$$\angle AQR = \angle QRD$$



Hence, pair of alternate interior angles are equal.

Hence proved.

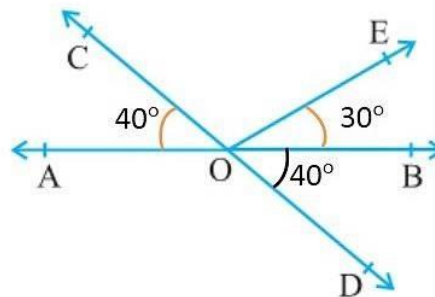
Theorem 6.3~ If a transversal intersects two lines such that a pair of interior opposite angles is equal then the two lines are parallel.

Ex 6.1, 1

In the given figure, lines AB and CD intersect at O. If $\angle AOC + \angle BOE = 70^\circ$ and $\angle BOD = 40^\circ$ find $\angle BOE$ and reflex $\angle COE$.

Given

$$\angle BOD = 40^\circ$$



Since AB & CD intersect,

$$\angle AOC = \angle BOD \quad (\text{Vertically opposite angles})$$

$$\angle AOC = 40^\circ$$

$$\text{Also, } \angle AOC + \angle BOE = 70^\circ \quad (\text{Given})$$

$$40^\circ + \angle BOE = 70^\circ$$

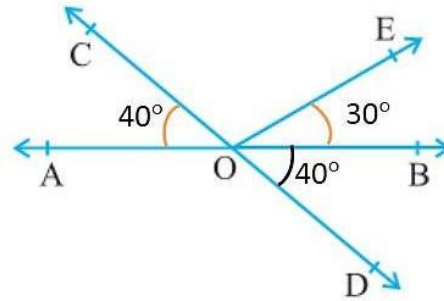
$$\angle BOE = 70^\circ - 40^\circ$$

$$\angle BOE = 30^\circ$$

We need to find reflex $\angle COE$

$$\text{Reflex } \angle COE = 360^\circ - \angle COE$$

First we finding $\angle COE$



Now,

$$\therefore \angle AOC + \angle COE + \angle BOE = 180^\circ \quad (\text{Linear pair})$$

$$\angle COE + (\angle AOC + \angle BOE) = 180^\circ$$

$$\angle COE + (40^\circ + 30^\circ) = 180^\circ$$

$$\angle COE + (70^\circ) = 180^\circ$$

$$\angle COE = 180^\circ - 70^\circ$$

$$\angle COE = 110^\circ$$

$$\text{Reflex } \angle COE = 360^\circ - 110^\circ$$

$$= 250^\circ$$

Ex 6.1, 2

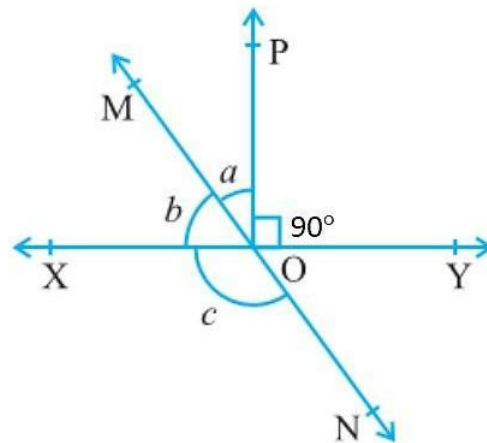
In the given figure, lines XY and MN intersect at O. If $\angle POY = 90^\circ$ and $a:b = 2 : 3$, find c .

Given

$$a : b = 2 : 3$$

$$\text{Let } a = 2x$$

$$\text{ \& } b = 3x, \text{ where } x \text{ is some number}$$



Now,

$$\angle POX + \angle POY = 180^\circ \quad (\text{Linear pair})$$

$$a + b + 90^\circ = 180^\circ$$

$$a + b = 180^\circ - 90^\circ$$

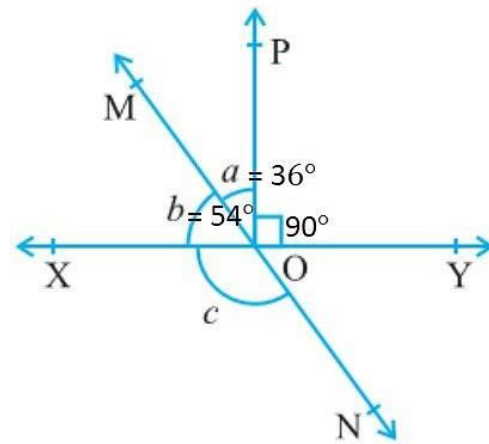
$$2x + 3x = 90^\circ$$

$$5x = 90^\circ$$

$$x = \frac{90^\circ}{5} = 18^\circ$$

$$a = 2x = 2 \times 18^\circ = 36^\circ$$

$$b = 3x = 3 \times 18^\circ = 54^\circ$$



We need to find c,

Since MN is a line, we can use linear pair

$$\angle MOX + \angle XON = 180^\circ \quad (\text{Linear pair})$$

$$b + c = 180^\circ$$

$$54^\circ + c = 180^\circ$$

$$c = 180^\circ - 54^\circ$$

$$c = 126^\circ$$

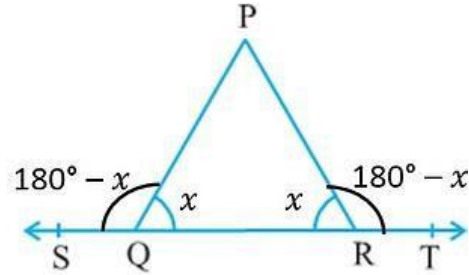
Ex6.1, 3

In the given figure, $\angle PQR = \angle PRQ$, then prove that $\angle PQS = \angle PRT$.

Let $\angle PQR = x$

Hence,

$\angle PRQ = x$ (Given $\angle PQR = \angle PRQ$)



Now,

$\angle PQS + \angle PQR = 180^\circ$ (Linear pair)

$\angle PQS = 180^\circ - \angle PQR$

$\angle PQS = 180^\circ - x$... (1)

Also, we can say

$\angle PRT + \angle PRQ = 180^\circ$ (Linear pair)

$\angle PRT = 180^\circ - \angle PRQ$

$\angle PRT = 180^\circ - x$... (2)

Ex 6.1, 4

In the given figure, if $x + y = w + z$, then prove that AOB is a line.

We know that

$$x + y + w + z = 360^\circ$$

*Sum all angles round
a point is equal to 360°*

$$(x + y) + (w + z) = 360^\circ$$

$$(x + y) + (x + y) = 360^\circ \quad (\text{Given } x + y = w + z)$$

$$2(x + y) = 360^\circ$$

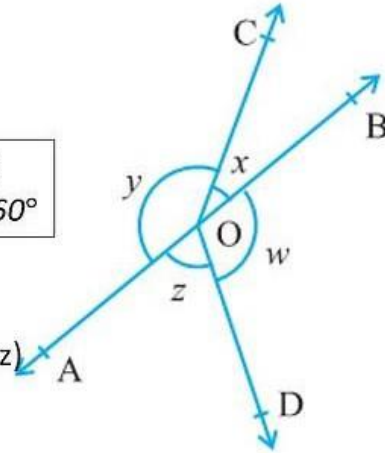
$$(x + y) = \frac{360^\circ}{2}$$

$$x + y = 180^\circ$$

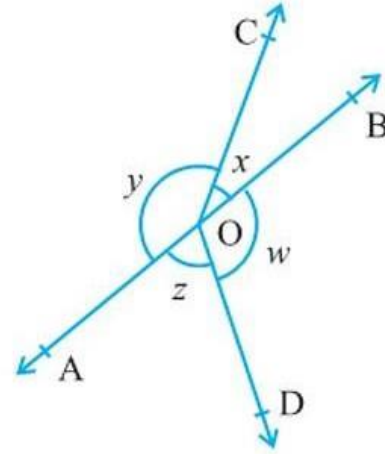
Since,

$$w + z = x + y$$

$$w + z = 180^\circ$$



Now, $x + y = 180^\circ$ & $w + z = 180^\circ$



From Axiom 6.2: If the sum of two adjacent angles is 180° , then non-common arms form a line (*Reverse Linear Pair*)

\therefore AOB is a straight line

Hence proved

Ex 6.1, 5

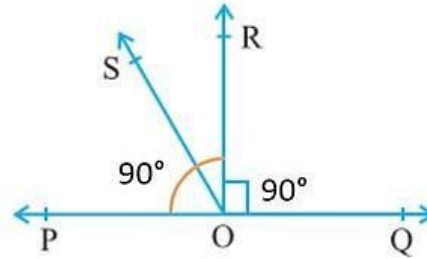
In the given figure, POQ is a line. Ray OR is perpendicular to line PQ. OS is another ray lying between rays OP and OR. Prove that

$$\angle ROS = \frac{1}{2} (\angle QOS - \angle POS)$$

Since $OR \perp PQ$

Hence, $\angle ROP = 90^\circ$

& $\angle ROQ = 90^\circ$



We can say that

$$\angle ROP = \angle ROQ$$

$$\angle POS + \angle ROS = \angle ROQ$$

$$\angle POS + \angle ROS = \angle QOS - \angle ROS$$

$$\angle POS + \angle ROS = \angle QOS - \angle ROS$$

$$2(\angle ROS) = \angle QOS - \angle POS$$

$$\angle ROS = \frac{1}{2} (\angle QOS - \angle POS)$$

Ex 6.1, 6

It is given that $\angle XYZ = 64^\circ$ and XY is produced to point P. Draw a figure from the given information. If ray YQ bisects $\angle ZYP$, find $\angle XYQ$ and reflex $\angle QYP$.

XYP is a straight line,

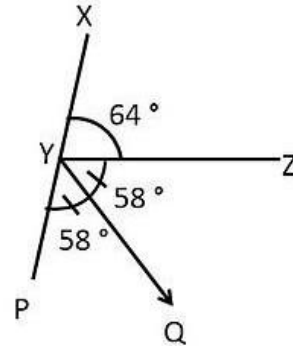
$$\angle XYZ + \angle ZYP = 180^\circ$$

$$\angle ZYP = 180^\circ - \angle XYZ$$

$$\angle ZYP = 180^\circ - 64^\circ$$

$$\angle ZYP = 116^\circ$$

(Linear pair)



Since YQ bisects $\angle ZYP$

$$\angle ZYQ = \angle QYP = \frac{1}{2} \angle ZYP$$

$$= \frac{1}{2} \times 116^\circ$$

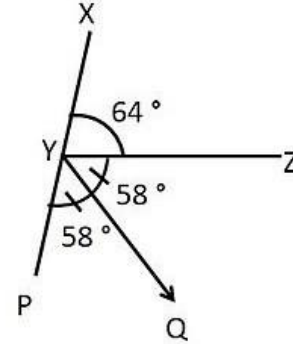
$$= 58^\circ$$

$$\begin{aligned}\angle XYQ &= \angle XYZ + \angle ZYQ \\ &= 64^\circ + 58^\circ \\ &= 122^\circ\end{aligned}$$

We have to find Reflex $\angle QYP$

$$\text{Reflex } \angle QYP = 360^\circ - \angle QYP$$

$$\begin{aligned}\text{Reflex } \angle QYP &= 360^\circ - 58^\circ \\ &= 302^\circ\end{aligned}$$



HOMEWORK ASSIGNMENT

EXERCISE 6.2 Q No 1,2,3

AHA

1. The exterior angles obtained on producing the base of a triangle both ways are 100° and 120° . Find the angles.

THANKING YOU
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