

Problem solving on the above concept (Multiplication of Rational Numbers)

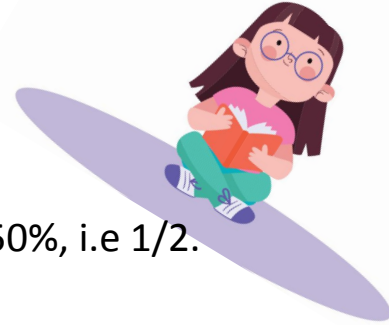
SUBJECT : MATHEMATICS
CHAPTER NUMBER: 02
CHAPTER NAME : RATIONAL NUMBERS

CHANGING YOUR TOMORROW

Learning outcomes

Students will be able to

- multiply rational numbers
- Implement its use in real life situation
like taxes ,banks greatly for calculation of interest and loan ,
share a pizza or anything ,
specifying home work half portion ; you say that you completed 50%, i.e $\frac{1}{2}$.



Video on rules of multiplication of rational numbers

<https://www.youtube.com/watch?v=VMp7bm9khis> (6:46 minutes
)

Exercise 2 D

Q.No.1

(iv) $-45/39 \times -13/15$

It can be written as

$$= (-45 \times -13) / (39 \times 15)$$

By further calculation

$$= (-3 \times -1) / (3 \times 1)$$

So we get

$$= 3/3$$

$$= 1$$

(v) $3 \frac{1}{8} \times (-2 \frac{2}{5})$

It can be written as

$$= (3 \times 8 + 1) / 8 \times (-2 \times 5 + 2) / 5$$

By further calculation

$$= 25/8 \times (-12/5)$$

So we get

$$= (25 \times -12) / (8 \times 5)$$

On further simplification

$$= (5 \times -3) / (2 \times 1)$$

$$= -15/2$$

Note : 0 is the only rational number which has no multiplicative inverse because there do not exist any rational number which when multiplied by 0 gives 1.

(vii) $(-8/9) \times (-3/16)$

It can be written as

$$= (-8 \times -3) / (9 \times 16)$$

By further calculation

$$= (-1 \times -1) / (3 \times 2)$$

$$= 1/6$$

(viii) $(5/-27) \times (-9/20)$

It can be written as

$$= (5 \times -9) / (-27 \times 20)$$

By further calculation

$$= (1 \times 1) / (3 \times 4)$$

$$= 1/12$$

2.ix) $6\frac{2}{3}$ and $-\frac{3}{8}$

It can be written as

$$= \frac{20}{3} \times -\frac{3}{8}$$

By further calculation

$$= \frac{(20 \times -3)}{(3 \times 8)}$$

So we get

$$= \frac{(5 \times -1)}{(1 \times 2)}$$

$$= -\frac{5}{2}$$

(x) $3\frac{3}{5}$ and -10

It can be written as

$$= \frac{(3 \times 5 + 3)}{5} \times -10$$

By further calculation

$$= \frac{18}{5} \times -10$$

So we get

$$= 18 \times -2$$

$$= -36$$

(xi) $27/28$ and -14

It can be written as

$$= 27/28 \times -14$$

By further calculation

$$= (27 \times -1)/ 2$$

$$= -27/2$$

(xii) -24 and $5/16$

It can be written as

$$= (-24 \times 5)/ 16$$

By further calculation

$$= (-3 \times 5)/ 2$$

So we get

$$= -15/2$$

$$\begin{aligned}
& 3. \text{ (iv) } (-5/9 \times 6/-25) + (24/21 \times 7/8) \\
& = (5/9 \times 6/25) + (24/21 \times 7/8) \\
& = 2/ (3 \times 5) + 1 \\
& = 2/15 + 1 \\
& \text{LCM of 15 and 1 is 15} \\
& = (2 + 15)/ 15 \\
& = 17/15 \\
& = 1 \frac{2}{15}
\end{aligned}$$

$$\begin{aligned}
& \text{(v) } (-35/39 \times -13/7) - (7/90 \times -18/14) \\
& = (-35/39 \times -13/7) - (7/90 \times -18/14) \\
& = (-5 \times -1)/ (3 \times 1) - (1 \times -1)/ (5 \times 2) \\
& = 5/3 - (-1/10) \\
& \text{LCM of 3 and 10 is 30} \\
& = (5 \times 10)/ (3 \times 10) + 1/ (10 \times 3) \\
& = (50 + 3)/ 30 \\
& = 53/30 \\
& = 1 \frac{23}{30}
\end{aligned}$$

$$\begin{aligned}
 & 3.(vi) \left(-\frac{4}{5} \times \frac{3}{2}\right) + \left(\frac{9}{-5} \times \frac{10}{3}\right) - \left(-\frac{3}{2} \times -\frac{1}{4}\right) \\
 & = \frac{(-2 \times 3)}{(5 \times 1)} + \frac{(3 \times 2)}{(-1 \times 1)} - \frac{(-3 \times -1)}{(2 \times 4)} \\
 & = -\frac{6}{5} + -\frac{6}{1} - \frac{3}{8}
 \end{aligned}$$

LCM of 5, 1 and 8 is 40

$$\begin{aligned}
 & = \frac{(-6 \times 8)}{(5 \times 8)} - \frac{(6 \times 40)}{(1 \times 40)} - \frac{(3 \times 5)}{(8 \times 5)} \\
 & = \frac{(-48 - 240 - 15)}{40} \\
 & = -\frac{303}{40}
 \end{aligned}$$

4. Find the cost of $3\frac{1}{2}$ m cloth, if one metre cloth costs Rs $325\frac{1}{2}$.

Solution:

It is given that cost of one metre cloth = ₹ $325\frac{1}{2}$

We can write it as

$$= (2 \times 325 + 1)/2$$

By further calculation

$$= (650 + 1)/2$$

$$= ₹ 651/2$$

Cost of $3\frac{1}{2}$ m cloth

$$(2 \times 3 + 1)/2 = 7/2 \text{ m}$$

We get

$$= 651/2 \times 7/2$$

It can be written as

$$= (651 \times 7)/(2 \times 2)$$

$$= 4557/4$$

$$= \text{Rs } 1139\frac{1}{4}$$

5. A bus is moving with a speed of $65\frac{1}{2}$ km per hour. How much distance will it cover in $1\frac{1}{3}$ hours.

Solution:

It is given that

Speed of bus = $65\frac{1}{2}$ km per hour

We can write it as

$$= (2 \times 65 + 1) / 2$$

By further calculation

$$= (130 + 1) / 2$$

$$= 131 / 2 \text{ km}$$

Distance covered in $1\frac{1}{3}$ hour = $\frac{4}{3}$ hour can be written as

$$= \frac{131}{2} \times \frac{4}{3}$$

We get

$$= \frac{131}{1} \times \frac{2}{3}$$

We know that distance covered = speed \times time

$$= \frac{131}{2} \times \frac{4}{3}$$

$$= (131 \times 2) / (1 \times 3)$$

So we get

$$= \frac{262}{3}$$

$$= 87\frac{1}{3} \text{ km}$$

Question 6.

(iv) -7 by $-14/5$

$$= -7 \div -14/5$$

$$= -7 \times 5/-14$$

$$= 1 \times 5/2$$

$$= (1 \times 5)/2$$

$$= 5/2$$

$$= 2 \frac{1}{2}$$

(v) -14 by $7/-2$

$$= -14 \div 7/-2$$

$$= -14 \times -2/7$$

$$= (-2 \times -2)/(1 \times 1)$$

$$= 4$$

(vi) $-22/9$ by $11/18$

$$= -22/9 \div 11/18$$

$$= -22/9 \times 18/11$$

$$= -2/1 \times 2/1$$

$$= (-2 \times 2)/(1 \times 1)$$

$$= -4/1$$

$$= -4$$

$$\begin{aligned} 6. \text{ v) } & -14 \text{ by } 7/-2 \\ & = -14 \div 7/-2 \\ & = -14 \times -2/7 \\ & = (-2 \times -2)/(1 \times 1) \\ & = 4 \end{aligned}$$

$$\begin{aligned} (\text{vi) } & -22/9 \text{ by } 11/18 \\ & = -22/9 \div 11/18 \\ & = -22/9 \times 18/11 \\ & = -2/1 \times 2/1 \\ & = (-2 \times 2)/(1 \times 1) \\ & = -4/1 \\ & = -4 \end{aligned}$$

6.(vii) 35 by $-7/9$

$$= 35 \div -7/9$$

$$= 35 \times 9/-7$$

$$= 5 \times 9/-1$$

$$= (5 \times 9)/-1$$

$$= 45/-1$$

$$= -45$$

(viii) $21/44$ by $-11/9$

$$= 21/44 \div -11/9$$

$$= 21/44 \times -9/11$$

$$= (21 \times -9)/(44 \times 11)$$

$$= -189/484$$

$$\begin{aligned}
& 7.(ii) \ 3 \frac{5}{12} - 1 \frac{2}{3} \\
& = (12 \times 3 + 5)/12 - (3 \times 1 + 2)/3 \\
& = 41/12 - 5/3 \\
& \text{LCM of 12 and 3 is 12} \\
& = (41 \times 1)/(12 \times 1) - (5 \times 4)/(3 \times 4) \\
& = (41 - 20)/12 \\
& = 21/12 \\
& = 2/4 \\
& = 1 \frac{3}{4}
\end{aligned}$$

$$\begin{aligned}
& (iii) \ (3 \frac{5}{12} + 1 \frac{2}{3}) \div (3 \frac{5}{12} - 1 \frac{2}{3}) \\
& = [(12 \times 3 + 5)/12 + (3 \times 1 + 2)/3] \div [(12 \times 3 + 5)/12 - (3 \times 1 + 2)/3] \\
& = (41/12 + 5/3) \div (41/12 - 5/3) \\
& \text{LCM of 12 and 3 is 12} \\
& = (41 + 20)/12 \div (41 - 20)/12 \\
& = 61/12 \div 21/12 \\
& = 61/12 \times 12/21 \\
& = 61/21 \\
& = 2 \frac{19}{21}
\end{aligned}$$

8. The product of two numbers is 14. If one of the numbers is $-\frac{8}{7}$, find the other.

Solution:

It is given that

Product of two numbers = 14

One of the number = $-\frac{8}{7}$

Other number = $14 \div -\frac{8}{7}$

We can write it as

$$= 14 \times -\frac{7}{8}$$

$$= -\frac{98}{8}$$

$$= -\frac{49}{4}$$

H.W.

Exercise 2 D Q.No.4

THANKING YOU
ODM EDUCATIONAL GROUP