

Addition and Subtraction of Rational numbers

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 02

CHAPTER NAME : RATIONAL NUMBERS

CHANGING YOUR TOMORROW

Learning outcomes

Students will be able to add and subtract rational numbers



Video on Addition and Subtraction of Rational numbers

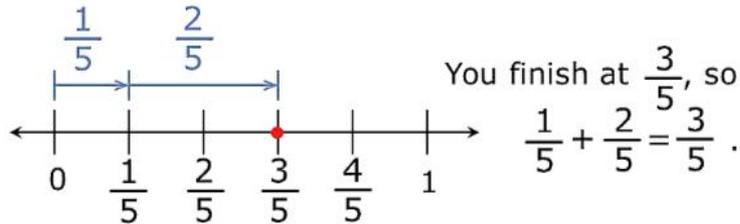
<https://www.youtube.com/watch?v=y0ISIVabPoA> (7:47
seconds)

Addition and Subtraction of Rational numbers

Case 1 : When denominators are equal

Addition of two rational numbers with the same denominator

- i. We can add it using a **number line**.
- ii. On the number line we have to move right from 0 to $\frac{1}{5}$ units and then move $\frac{2}{5}$ units more to the right.
- iii. **Example:**
Add $\frac{1}{5}$ and $\frac{2}{5}$



ii. If we have to **add two rational numbers** whose denominators are same then we simply add their numerators and the denominator remains the same.

Example

$$\frac{3}{11} + \frac{7}{11} = \frac{3+7}{11} = \frac{10}{11}$$

Solution

As the denominator is the same, we can simply add their numerator.

Addition of two Rational Numbers with different denominator

If we have to add two rational numbers with different denominators then we have to take the LCM of denominators and find their equivalent rational numbers with the LCM as the denominator, and then add them.

Example

Add $\frac{2}{5}$ and $\frac{3}{7}$.

Solution

To add the two rational numbers, first, we need to take the LCM of denominators then find the equivalent rational numbers.
LCM of 5 and 7 is 35.

$$\frac{2}{5} \times \frac{7}{7} = \frac{14}{35}$$

$$\frac{3}{7} \times \frac{5}{5} = \frac{15}{35}$$

$$\frac{14}{35} + \frac{15}{35} = \frac{29}{35}$$

Subtraction of two Rational Numbers with different denominator

If we have to subtract two rational numbers with different denominators then we have to take the LCM of denominators and find their equivalent rational numbers with the LCM as the denominator, and then subtract them.

Note: Additive inverse of a rational number is its opposite.

1. Add:

(i) $7/5$ and $2/5$

(ii) $-4/9$ and $2/9$

(iii) $5/-12$ and $1/12$

Solution:

(i) $7/5$ and $2/5$

$$= 7/5 + 2/5$$

$$= (7 + 2)/ 5$$

$$= 9/5$$

$$= 1 \frac{4}{5}$$

(ii) $-4/9$ and $2/9$

$$= -4/9 + 2/9$$

$$= (-4 + 2)/ 9$$

$$= -2/9$$

(iii) $5/-12$ and $1/12$

$$= -5/12 + 1/12$$

$$= (-5 + 1)/ 12$$

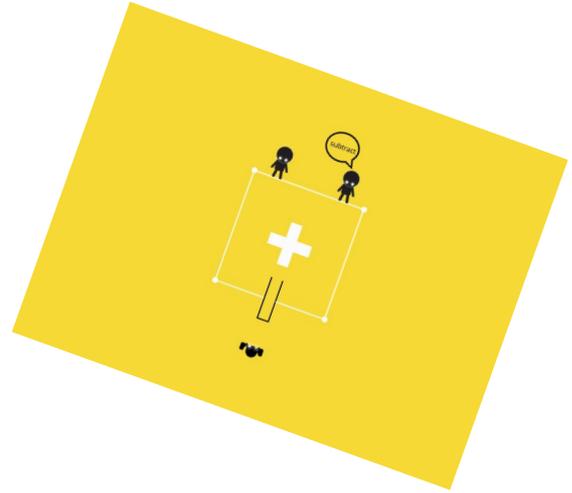
$$= -4/ 12$$

$$= -1/3$$

$$\begin{aligned} & \text{(iv) } 4/-15 \text{ and } -7/-15 \\ & = -4/15 + 7/15 \\ & = (-4 + 7)/15 \\ & = 3/15 \\ & = 1/5 \end{aligned}$$

$$\begin{aligned} & \text{(v) } -7/25 \text{ and } 9/-25 \\ & = -7/25 + -9/25 \\ & = [(-7) + (-9)]/25 \\ & = -16/25 \end{aligned}$$

$$\begin{aligned} & \text{(vi) } -7/26 \text{ and } 7/-26 \\ & = -7/26 + -7/26 \\ & = [(-7) + (-7)]/26 \\ & = -14/26 \\ & = -7/13 \end{aligned}$$



3. Evaluate:

(i) $-2/5 + 3/5 + -1/5$

(ii) $-8/9 + 4/9 + -2/9$

(iii) $5/-24 + -1/8 + 3/16$

Solution:

$$\begin{aligned} \text{(i)} \quad & -2/5 + 3/5 + -1/5 \\ & = (-2 + 3 - 1)/5 \\ & = 0/5 \\ & = 0 \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad & -8/9 + 4/9 + -2/9 \\ & = (-8 + 4 - 2)/9 \\ & = (-10 + 4)/9 \\ & = -6/9 \\ & = -2/3 \end{aligned}$$

$$\begin{aligned} \text{(iii)} \quad & 5/-24 + -1/8 + 3/16 \\ & = -5/24 + -1/8 + 3/16 \\ & \text{LCM of 8, 16 and 24 is 48} \\ & = (-5 \times 2)/(24 \times 2) + (-1 \times 6)/(8 \times 6) + (3 \times 3)/(16 \times 3) \\ & = -10/48 + -6/48 + 9/48 \\ & = (-10 - 6 + 9)/48 \\ & = (-16 + 9)/48 \\ & = -7/48 \end{aligned}$$

5. Subtract:

(iii) $-2/15$ from $-8/15$

(iv) $11/18$ from $-5/18$

(v) $-4/11$ from -2



$$\begin{aligned} & \text{(iii) } -2/15 \text{ from } -8/15 \\ & = -8/15 - (-2/15) \\ & = -8/15 + 2/15 \\ & = (-8 + 2)/15 \\ & = -6/15 \\ & = -2/5 \end{aligned}$$

$$\begin{aligned} & \text{(iv) } 11/18 \text{ from } -5/18 \\ & = -5/18 - 11/18 \\ & = (-5 - 11)/18 \\ & = -16/18 \\ & = -8/9 \end{aligned}$$

$$\begin{aligned} & \text{(v) } -4/11 \text{ from } -2 \\ & = -2/1 - (-4/11) \\ & \text{LCM of 1 and 11 is 11} \\ & = (-2 \times 11)/(1 \times 11) + (4 \times 1)/(11 \times 1) \\ & = -22/11 + 4/11 \\ & = (-22 + 4)/11 \\ & = -18/11 \end{aligned}$$

H.W

Exercise 2C Q.No. 2 & 4

AHA

1. Find a rational number which is $\frac{23}{72}$ more than $\frac{-11}{24}$

2. In a basket of fruits, $\frac{1}{4}$ are apples, $\frac{1}{5}$ are oranges, and $\frac{1}{3}$ are bananas, the remaining are pears. What part of basket of fruits are pears?



THANKING YOU
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