

PERIOD 4

MATHEMATICS

CHAPTER NUMBER :~ 8

CHAPTER NAME :~QUADRILATERALS

CHANGING YOUR TOMORROW

PREVIOUS KNOWLEDGE TEST

1. ABCD is a parallelogram in which P and Q are the midpoints of opposite sides AB and CD. If AQ intersects DP at S and BQ intersects CP at R, show that APCQ is a parallelogram.

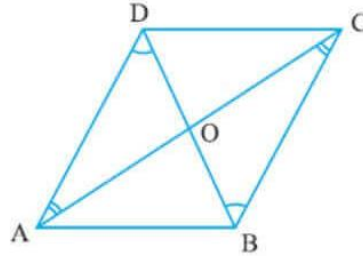
LEARNING OUTCOME:~

- 1.Students will be able to learn some more properties of parallelogram.
- 2.Students will be able to solve application sums on parallelogram.

Theorem 8.6

The diagonals of a parallelogram bisect each other

Given : ABCD is a Parallelogram with
AC and BD diagonals & O is the
point of intersection of AC and BD



To Prove : $OA = OC$ & $OB = OD$

Proof : Since, opposite sides of Parallelogram are parallel.

AD \parallel BC
with transversal BD

$\angle ODA = \angle OBC$ (*Alternate interior angles*)

AD \parallel BC
with transversal AC

$\angle OAD = \angle OCB$ (*Alternate interior angles*)

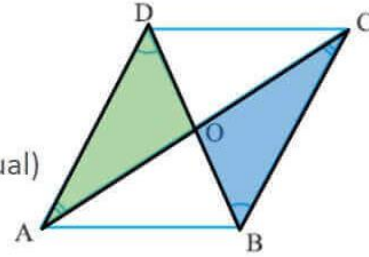
In $\triangle AOD$ and $\triangle BOC$

$$\angle OAD = \angle OCB \quad (\text{From (1)})$$

$$AD = CB \quad (\text{Opposite side of Parallelogram are equal})$$

$$\angle ODA = \angle OBC \quad (\text{From (2)})$$

$$\triangle AOD \cong \triangle BOC \quad (\text{ASA rule})$$



So,

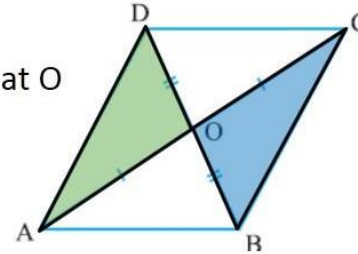
$$OA = OC \quad \& \quad OB = OD \quad (\text{CPCT})$$

Hence Proved

Theorem 8.7

If the diagonals of a quadrilateral bisect each other, then it is a parallelogram.

Given: ABCD is a quadrilateral with
AC and BD are diagonals intersecting at O
Diagonals bisect each other
i.e. $OA = OC$ & $OB = OD$



To Prove: ABCD is a parallelogram

Proof : In $\triangle AOD$ and $\triangle COB$

$$OA = OC \quad (\text{Given})$$

$$\angle AOD = \angle COB \quad (\text{Vertically opposite angles})$$

$$OD = OB \quad (\text{Given})$$

$$\triangle AOD \cong \triangle COB \quad (\text{SAS congruency})$$

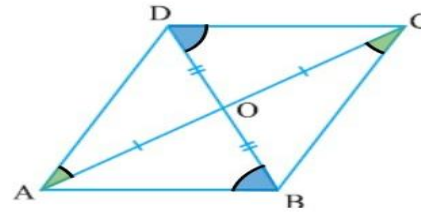
$$\triangle AOD \cong \triangle COB$$

$$\therefore \angle OAD = \angle OCB \quad (\text{CPCT}) \dots(1)$$

Similarly, we can prove

$$\triangle AOB \cong \triangle COD$$

$$\therefore \angle ABO = \angle CDO \quad (\text{CPCT}) \dots(2)$$



For lines **AB and CD**
with transversal BD,

$\angle ABO$ & $\angle CDO$ are alternate
angles and are equal.

\therefore Lines are parallel i.e. $AB \parallel CD$

For lines **AD and BC**
with transversal AC,

$\angle OAD$ & $\angle OCB$ are alternate
angles and are equal.

\therefore Lines are parallel i.e. $AD \parallel BC$

Thus, In ABCD,

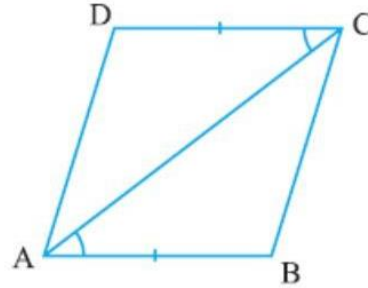
Both pairs of opposite sides are parallel,

\therefore ABCD is a parallelogram

Theorem 8.8

A quadrilateral is a parallelogram if a pair of opposite sides is equal and parallel.

Given : ABCD is a quadrilateral
where $AB \parallel CD$ & $AB = CD$



To Prove : ABCD is a Parallelogram

Proof :

Given $AB \parallel CD$

with transversal AC.

$$\angle BAC = \angle DCA \quad (\text{Alternate angles}) \dots(1)$$

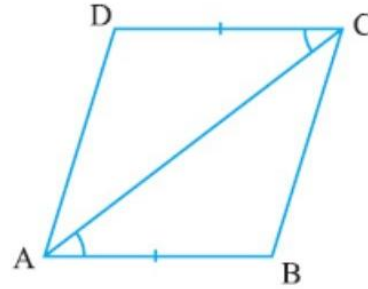
In $\triangle ADC$ & $\triangle CBA$

$$AB = CD \quad (\text{Given})$$

$$\angle BAC = \angle DCA \quad (\text{From (1)})$$

$$AC = CA \quad (\text{Common})$$

$$\therefore \triangle ADC \cong \triangle CBA \quad (\text{SAS Rule})$$



$$\text{Hence, } DA = BC \quad (\text{CPCT})$$

Thus, In ABCD,

Both pairs of opposite sides are equal

\therefore ABCD is a Parallelogram.

Hence proved

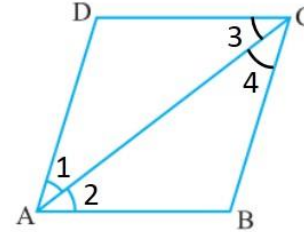
Ex 8.1, 6

Diagonal AC of a parallelogram ABCD bisects $\angle A$. Show that

(i) it bisects $\angle C$ also,

Given: Parallelogram ABCD

where $\angle 1 = \angle 2$... (1)



To prove: AC bisects $\angle C$

i.e. $\angle 3 = \angle 4$

Proof:

Now,

$\angle 1 = \angle 2$ (Given)

$\angle 2 = \angle 3$

AB \parallel DC & AC as transversal,
Alternate angles equal

$\angle 1 = \angle 4$

AD \parallel BC & AC as transversal,
Alternate angles equal

Hence, we can say that

$\angle 1 = \angle 2 = \angle 3 = \angle 4$

So, $\angle 3 = \angle 4$

Hence proved

Ex 8.1, 7

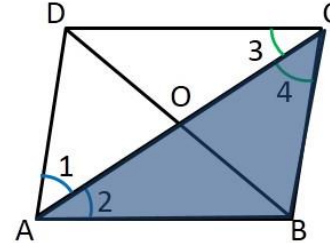
ABCD is a rhombus. Show that diagonal AC bisects $\angle A$ as well as $\angle C$ and diagonal BD bisects $\angle B$ as well as $\angle D$.

Given:

Rhombus ABCD

To prove:

- (i) AC bisects $\angle A$, i.e. $\angle 1 = \angle 2$ & bisects $\angle C$, i.e. $\angle 3 = \angle 4$
- (ii) BD bisects $\angle D$ & $\angle B$

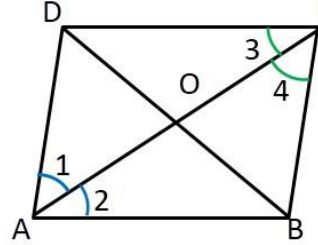


Proof:

In $\triangle ABC$,

$AB = BC$ (Sides of rhombus are equal)

So, $\angle 4 = \angle 2$ (Angles opposite to equal sides are equal) ... (1)



Now, $AD \parallel BC$ (*Opposite sides of rhombus are parallel*)
and transversal AC.

$$\angle 1 = \angle 4 \quad (\text{Alternate angles}) \dots (2)$$

From (1) & (2)

$$\angle 1 = \angle 2$$

\Rightarrow AC bisects $\angle A$

Now, $AB \parallel DC$ (*Opposite sides of rhombus are parallel*)
and transversal AC.

$$\angle 2 = \angle 3 \quad (\text{Alternate angles}) \dots (3)$$

From (1) & (3)

$$\angle 4 = \angle 3$$

\Rightarrow AC bisects $\angle C$

Hence,

AC bisects $\angle C$ & $\angle A$

Similarly we can prove that BD bisects $\angle B$ & $\angle D$

Hence proved

HOMEWORK ASSIGNMENT

Exercise 8.1
Question number 6,7

AHA

1. A diagonal of a parallelogram bisects one of its angles. Prove that it's a rhombus.

THANKING YOU
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