

MONTH : AUGUST

SESSION : 1

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : GCF OR HCF: LISTING METHOD

EXERCISE : 8 B Q.NO. 1,2,3

CHANGING YOUR TOMORROW

HIGHEST COMMON FACTOR

The **GCF** or **HCF** is the greatest whole number that is the **common factor** of given numbers.

Example : Find the H.C.F of 18 and 24

Method 1: Listing Method

Factors of 18 = 1 , 2 , 3 , 6 , 9 , 18

Factors of 24 = 1 , 2 , 3 , 4 , 6 , 8 , 12 , 24

The common factors are: **1,2,3** and **6**

∴ The H.C.F is **6**



LISTING METHOD

Example 2 : Find the H.C.F of 8, 12 and 30

Solution:

❖ Factors of 8 = 1, 2, 4, 8

❖ Factors of 12 = 1, 2, 3, 4, 6, 12

❖ Factors of 30 = 1, 2, 3, 5, 6, 10, 15, 30

□ The common factors are: 1, 2

∴ The H.C.F = 2



EXERCISE : 8 [B]

1. Find the H.C.F of 27 and 36

Solution:

Factors of 27 = 1 , 3, 9, 27

Factors of 36 = 1, 2 , 3, 4, 6, 9, 12, 18, 36

Common factors of 27 and 36 are: 1, 3 and 9

∴ The H.C.F is 9



EXERCISE : 8 [B]

2. Find the H.C.F of 82 and 104

□ **Solution:**

Factors of 82 : 1 , 2 , 41 , 82

Factors of 104: 1 , 2 , 4 , 8 , 13 , 26 , 52 , 104

Common factor of 84 and 104 are: 1 , 2

∴ The H.C.F is 2



EXERCISE : 8 [B]

3. Find the common factors and H.C.F of 20, 35 and 40

Solution:

Factors of 20: 1 , 2 , 4 , 5 , 10 , 20

Factors of 35: 1 , 5 , 7 , 35

Factors of 40: 1 , 2 , 4 , 5 , 8 , 10 , 20 , 40

The common factors of 20, 35 and 40 are 1 and 5

∴ The H.C.F is 5



Home assignment: Complete Ex.8 [B] Q.No.4 and 5 in the notebook.



LEARNING OUTCOME:

Students are able

- **To understand the concept of factors.**
- **To understand to find out common factors and highest common factor.**

THANKING YOU
ODM EDUCATIONAL GROUP

MONTH : AUGUST

SESSION : 2

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : HIGHEST COMMON FACTOR - PRIME FACTOR METHOD,

EXERCISE : 8 [B] Q.NO. 6

CHANGING YOUR TOMORROW

HIGHEST COMMON FACTOR

The **GCF** or **HCF** is the greatest whole number that is the **common factor** of given numbers.

Example : Find the H.C.F of 18 and 24

Solution :

Prime factor method (Method 1)

$$\begin{array}{r|l} 2 & 18 \\ \hline 3 & 9 \\ \hline 3 & 3 \\ \hline & 1 \end{array}$$

$$\begin{array}{r|l} 2 & 24 \\ \hline 2 & 12 \\ \hline 2 & 6 \\ \hline 3 & 3 \\ \hline & 1 \end{array}$$

Prime factors of 18 = $2 \times 3 \times 3$

Prime factors of 24 = $2 \times 2 \times 2 \times 3$

Common factors of 18 and 24 are 2 and 3 .

So H.C.F of 18 and 24 is $2 \times 3 = 6$

HIGHEST COMMON FACTOR

Example : Find the H.C.F of 18 and 24

Prime factor method (Method 2)

$$\begin{array}{l} 2 \quad | \quad 18, 24 \\ \hline 3 \quad | \quad 9, 12 \\ \hline \quad \quad 3, 4 \end{array}$$

So H.C.F of 18 and 24 is $2 \times 3 = 6$

Prime factor method

Example 2 : Find the H.C.F of 48, 72 and 84

Solution: [METHOD 1]

$$\begin{array}{r|l} 2 & 48 \\ \hline 2 & 24 \\ \hline 3 & 12 \\ \hline 2 & 4 \\ \hline 2 & 2 \\ \hline & 1 \end{array}$$

$$\begin{array}{r|l} 2 & 72 \\ \hline 2 & 36 \\ \hline 3 & 18 \\ \hline 3 & 6 \\ \hline 2 & 2 \\ \hline & 1 \end{array}$$

$$\begin{array}{r|l} 2 & 84 \\ \hline 2 & 42 \\ \hline 3 & 21 \\ \hline 7 & 7 \\ \hline & 1 \end{array}$$

$$\begin{aligned} 48 &= 2 \times 2 \times 3 \times 2 \times 2 \\ 72 &= 2 \times 2 \times 3 \times 3 \times 2 \\ 84 &= 2 \times 2 \times 3 \times 7 \end{aligned}$$

Common factors of 48, 72 and 84 are 2, 2 and 3.

So, H.C.F. of 48, 72 and 84 is $2 \times 2 \times 3 = 12$

PRIME FACTOR METHOD

Example 2 : Find the H.C.F of 48, 72 and 84

Solution: [METHOD 2]

$$\begin{array}{r|l} 2 & 48, 72, 84 \\ \hline 2 & 24, 36, 42 \\ \hline 3 & 12, 18, 21 \\ \hline & 4, 6, 7 \end{array}$$

The H.C.F. = $2 \times 2 \times 3 = 12$



EXERCISE : 8 [B]

6. Find the H.C.F of the following numbers by prime factor method.

a. 75 and 125

$$\begin{array}{r|l} 5 & 75, 125 \\ \hline 5 & 15, 25 \\ \hline & 3, 5 \end{array}$$

H.C.F. = $5 \times 5 = 25$

b. 24, 54 and 60

$$\begin{array}{r|l} 2 & 24, 54, 60 \\ \hline 3 & 12, 27, 30 \\ \hline & 4, 9, 10 \end{array}$$

H.C.F. = $2 \times 3 = 6$



EXERCISE : 8 [B]

6. Find the H.C.F of the following numbers by prime factor method.

c. 63 , 70 , 98

$$\begin{array}{l} 7 \overline{) 63, 70, 98} \\ 9, 10, 14 \end{array}$$

∴ The H.C.F is 7

d. 112 , 210 , 252

$$\begin{array}{l} 2 \overline{) 112, 210, 252} \\ 7 \overline{) 56, 105, 126} \\ 8, 15, 36 \end{array}$$

∴ The H.C.F is $2 \times 7 = 14$



EXERCISE : 8 [B]

6. Find the H.C.F of the following numbers by prime factor method.

e. 27 , 99 , 144

$$\begin{array}{l|l} 3 & 27, 99, 144 \\ \hline 3 & 9, 33, 48 \\ \hline & 3, 11, 16 \end{array}$$

$$\text{H.C.F} = 3 \times 3 = 9$$

f. 175 , 250 , 300

$$\begin{array}{l|l} 5 & 175, 250, 300 \\ \hline 5 & 35, 50, 60 \\ \hline & 7, 10, 12 \end{array}$$

$$\text{H.C.F.} = 5 \times 5 = 25$$



LEARNING OUTCOME:

The students are able

- **to understand the concept of factors and prime factors.**
- **to find out common factors and highest common factor by prime factor method.**

HOME ASSIGNMENT:

- Complete Exercise 8 [B] Q.No. 6 (g) to (i) in the notebook.



THANKING YOU
ODM EDUCATIONAL GROUP

MONTH : AUGUST

SESSION : 3

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : HCF: DIVISION METHOD

EXERCISE : 8[B] Q.NO. 7

CHANGING YOUR TOMORROW

HIGHEST COMMON FACTOR

Whenever we are asked to find out the H.C.F. of large numbers we always use the division method.

Example : Find the H.C.F of 300 and 888

$$\begin{array}{r} 2 \\ 300 \overline{) 888} \\ \underline{600} \quad 1 \\ 288 \quad 300 \\ \underline{288} \quad 24 \\ 12 \quad 288 \\ \underline{24} \\ 48 \\ \underline{48} \\ 0 \end{array}$$

H.C.F. = 12, Because **12 is the last divisor.**

Example : Find the H.C.F of 912, 1216 and 2400.

When we are asked to find out the H.C.F. of more than 2 numbers, 1st we find out the H.C.F. of the largest and second largest number.

STEP – 1

$$\begin{array}{r} 1 \\ 1216 \overline{) 2400} \\ \underline{1216} \quad 1 \\ 1184 \overline{) 1216} \\ \underline{1184} \quad 3 \quad 7 \\ 32 \overline{) 1184} \\ \underline{96} \\ 224 \\ \underline{224} \\ 0 \end{array}$$

H.C.F. of 1216 and 2400 = 32, Because 32 is the last divisor.

STEP – 2

Then we find out the H.C.F. of 912 and 32[the 1st H.C.F.].

$$\begin{array}{r} 28 \\ 32 \overline{) 912} \\ \underline{- 64} \\ 272 \\ \underline{- 256} \\ 16 \\ \underline{16} \\ 0 \end{array}$$

H.C.F. of 912, 1216 and 2400 = 16

EXERSICE – 8 [B]

7. Find the H.C.F of the following numbers by the division method.

a. 112 and 189

$$\begin{array}{r} 1 \\ 112 \overline{) 189} \\ \underline{112} \quad 1 \\ 77 \overline{) 112} \\ \underline{77} \quad 2 \\ 35 \overline{) 77} \\ \underline{70} \quad 5 \\ 7 \overline{) 35} \\ \underline{35} \\ 0 \end{array}$$

The H.C.F = 7



EXERSICE – 8 [B]

6. Find the H.C.F of the following numbers by the division method.

b. 34, 51 and 85

$$\begin{array}{r} 51 \overline{) 85} \\ \underline{51} \\ 34 \\ \underline{34} \\ 17 \\ \underline{17} \\ 0 \end{array}$$

$$\begin{array}{r} 17 \overline{) 34} \\ \underline{34} \\ 0 \end{array}$$

∴ H.C.F of 34 ,51 and 85 = 17

The H.C.F of 85 and = 17

EXERSICE – 8 [B]

6. Find the H.C.F of the following numbers by the division method.

c. 95, 152 and 190

$$\begin{array}{r} 1 \\ 152 \overline{) 190} \\ \underline{152} \quad 4 \\ 38 \overline{) 152} \\ \underline{152} \\ 0 \end{array}$$

The H.C.F of 190
and 152 = 38

$$\begin{array}{r} 2 \\ 38 \overline{) 95} \\ \underline{76} \quad 2 \\ 19 \overline{) 38} \\ \underline{38} \\ 0 \end{array}$$

∴ H.C.F of 95, 152 and 190 = 19

EXERSICE – 8 [B]

6. Find the H.C.F of the following numbers by the division method.

d. 650, 900 and 1000

$$\begin{array}{r} 1 \\ 900 \overline{) 1000} \\ \underline{900} \quad 9 \\ 100 \overline{) 900} \\ \underline{900} \\ 0 \end{array}$$

The H.C.F of 1000 and 900 = 100

$$\begin{array}{r} 6 \\ 100 \overline{) 650} \\ \underline{600} \quad 2 \\ 50 \overline{) 100} \\ \underline{100} \\ 0 \end{array}$$

∴ H.C.F of 650, 900 and 1000 = 50

EXERSICE – 8 [B]

6. Find the H.C.F of the following numbers by the division method.

1

e. 690, 966 and 1150

$$\begin{array}{r} 966 \overline{) 1150} \\ \underline{966} \\ 184 \\ 184 \\ \underline{184} \\ 0 \end{array}$$

The H.C.F of 1150 and 966 = 46

$$\begin{array}{r} 46 \overline{) 690} \\ \underline{46} \\ 230 \\ \underline{230} \\ 0 \end{array}$$

∴ H.C.F of 690, 966 and 1150 = 46

EXERSICE – 8 [B]

6. Find the H.C.F of the following numbers by the division method.

f. 738 , 1080 and 1332

$$\begin{array}{r} 1 \\ 1080 \overline{) 1332} \\ \underline{1080} \quad 4 \\ 252 \overline{) 1080} \\ \underline{1008} \quad 3 \\ 72 \overline{) 252} \\ \underline{216} \quad 2 \\ 36 \overline{) 72} \\ \underline{72} \\ 0 \end{array}$$

$$\begin{array}{r} 2 \\ 36 \overline{) 738} \\ \underline{72} \quad 2 \\ 18 \overline{) 36} \\ \underline{36} \\ 0 \end{array}$$

∴ H.C.F of 738, 1080 and 1332 = 18

The H.C.F of 1332 and 1080 = 36

HOME ASSIGNMENT:

- **Complete Exercise 8 [B] Q.No. 7 (g) and (h) in the notebook.**



LEARNING OUTCOME:

The students are able

- **To understand the concept of factors and prime factors.**
- **to find out common factors and highest common factor using Division method.**

THANKING YOU
ODM EDUCATIONAL GROUP

MONTH : AUGUST

SESSION : 4

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : LEAST COMMON MULTIPLE: L.C.M.

PROPERTIES OF L.C.M.

CHANGING YOUR TOMORROW

MULTIPLES

A multiple of a number is a **product** of the number and a whole number.

Examples:

Multiples of 4 are: $4 \times 1 = 4$

$$4 \times 2 = 8$$

$$4 \times 3 = 12 \dots \text{etc.}$$



LEAST COMMON MULTIPLES

The multiples that are common to two or more numbers are called the common multiples of those numbers.



LEAST COMMON MULTIPLES

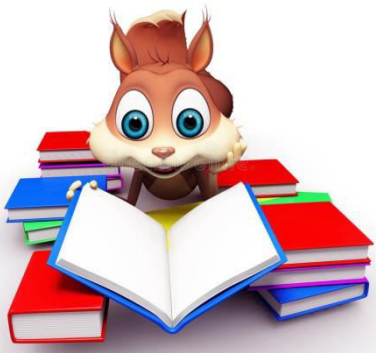
Example:

Multiples of 5 \longrightarrow **5, 10, 15, 20, 25, 30, 35, 40, 45, 50**

Multiples of 4 \longrightarrow **4, 8, 12, 16, 20, 24, 28, 32, 36, 40**

Common multiples are : 20, 40

Least common multiple = 20



PROPERTIES OF LEAST COMMON MULTIPLES

1. The L.C.M. of two prime numbers is their product.

- Example: The L.C.M. of 3 and 5 is 15 or 7 and 11 is 77.

2. If a number is a factor of another number, then their L.C.M. is the greater number.

- Example: The L.C.M. of 3 and 9 is 9 or L.C.M. of 5 and 40 is 40.



PROPERTIES OF LEAST COMMON MULTIPLES

3. The L.C.M. of two or more numbers cannot be less than either of them.

Example: L.C.M. of **5 and 9** is **45**

4. The L.C.M. of two consecutive number is the product of the numbers.

Example: L.C.M. of **5 and 6** is **30**.



LEARNING OUTCOME:



The students are able

- **To understand the concept of Multiples and Least common multiple.**
- **To find out common multiples and L.C.M.**



THANKING YOU
ODM EDUCATIONAL GROUP

MONTH : AUGUST

SESSION : 5

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : LEAST COMMON MULTIPLE: L.C.M. BY

PRIME FACTOR METHOD. EXERCISE 8 C Q.NO.1

CHANGING YOUR TOMORROW

L.C.M. BY PRIME FACTOR METHOD

Example 1: Find the L.C.M. of 12, 15 and 24

Prime factors of 12 = $2 \times 2 \times 3$

Prime factors of 24 = $2 \times 2 \times 2 \times 3$

Prime factors of 15 = 3×5

Common Prime factors are: 3

Remaining common prime factor: $2, 2$

Uncommon prime factor : 2 and 5

$$\text{L.C.M.} = 3 \times 2 \times 2 \times 2 \times 5 = 120$$

The L.C.M. of 12, 15 and 24 is 120 .



L.C.M. by Prime factor method

Example 2: Find the L.C.M. of 20, 30 and 35

Prime factors of 30 = $3 \times 5 \times 2$

Prime factors of 20 = $2 \times 5 \times 2$

Prime factors of 35 = 7×5

Common Prime factors are: 5

Remaining common prime factor: 2

Uncommon prime factor : 3,2,7

$$\text{L.C.M.} = 5 \times 2 \times 3 \times 2 \times 7 = 420$$

The L.C.M. of 20, 30 and 35 is **420**.



EXERCISE 8 [C]

1. Write the prime factors of each number and find the L.C.M.

a. 36 and 63

Prime factors of 36 = $2 \times 2 \times 3 \times 3$

Prime factors of 63 = $7 \times 3 \times 3$

L.C.M. = $3 \times 3 \times 2 \times 2 \times 7 = 252$

The L.C.M. of 36 and 63 is 252.



EXERCISE 8 [C]

1. Write the prime factors of each number and find the L.C.M.

b. 11 and 55

Prime factors of 11 = 1×11

Prime factors of 55 = 5×11

L.C.M. = $11 \times 5 \times 1 = 55$

The L.C.M. of 11 and 55 is **55**.



EXERCISE 8 [C]

1. Write the prime factors of each number and find the L.C.M.

c. 25 and 100

Prime factors of 25 = 5×5

Prime factors of 100 = $5 \times 5 \times 2 \times 2$

L.C.M. = $5 \times 5 \times 2 \times 2 = 100$

The L.C.M. of 25 and 100 is 100.



EXERCISE 8 [C]

1. Write the prime factors of each number and find the L.C.M.

d. 9, 36 and 45

Prime factors of 9 = 3×3

Prime factors of 36 = $3 \times 3 \times 2 \times 2$

Prime factors of 45 = $3 \times 3 \times 5$

L.C.M. = $3 \times 3 \times 2 \times 2 \times 5 = 180$

The L.C.M. of 9, 36 and 45 is 180.



EXERCISE 8 [C]

1. Write the prime factors of each number and find the L.C.M.

e. 12, 15, 18 and 36

$$\text{Prime factors of 12} = 3 \times 2 \times 2$$

$$\text{Prime factors of 15} = 3 \times 5$$

$$\text{Prime factors of 18} = 3 \times 3 \times 2$$

$$\text{Prime factors of 36} = 3 \times 3 \times 2 \times 2$$

$$\text{L.C.M.} = 3 \times 3 \times 2 \times 2 \times 5 = 180$$

The L.C.M. of 12, 15, 18 and 36 **180**.



EXERCISE 8 [C]

1. Write the prime factors of each number and find the L.C.M.

f. 20, 50, 60 and 100

$$\text{Prime factors of 20} = 2 \times \underline{2} \times 5$$

$$\text{Prime factors of 50} = 2 \times \underline{5} \times 5$$

$$\text{Prime factors of 60} = 2 \times \underline{2} \times 5 \times 3$$

$$\text{Prime factors of 100} = 2 \times \underline{2} \times 5 \times \underline{5}$$

$$\text{L.C.M.} = 2 \times 5 \times 2 \times 5 \times 3 = 300$$



The L.C.M. of 20, 50, 60 and 100 is **300**.

**HOME ASSIGNMENT : Complete Exercise 8 C
Q.No. 1 [g] and [h] in the notebook.**



LEARNING OUTCOME:

Students are able

- **To Understand the concept of Multiples and Least common multiple.**
- **To find out common multiples and L.C.M.**

THANKING YOU
ODM EDUCATIONAL GROUP

MONTH : AUGUST

SESSION : 6

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : LEAST COMMON MULTIPLE: L.C.M. BY

COMMON DIVISION METHOD. EXERCISE 8 C Q.NO.2

CHANGING YOUR TOMORROW

L.C.M. BY COMMON DIVISION METHOD

Example 1: Find the L.C.M. of 20, 25, 30 and 36

2	20	25	30	36
2	10	25	15	18
3	5	25	15	9
3	5	25	5	3
5	1	25	5	1
5	1	5	1	1
	1	1	1	1

$$\text{L.C.M.} = 2 \times 2 \times 3 \times 3 \times 5 \times 5 = 900$$



L.C.M. BY COMMON DIVISION METHOD

Example 2: Find the L.C.M. of 9, 36 and 45

3	9	36	45
3	3	12	15
2	1	4	5
2	1	2	5
5	1	1	5
	1	1	1

$$\text{L.C.M} = 3 \times 3 \times 2 \times 2 \times 5 = \mathbf{180}$$



EXERCISE 8 [C]

Find the L.C.M. of each numbers using division method

a. 22, 44, 66

2	22	44	66
1	1	22	33
12	1	2	3
3	1	1	3
	1	1	1

$$\text{L.C.M} = 2 \times 11 \times 2 \times 3 = 132$$



EXERCISE 8 [C]

Find the L.C.M. of each numbers using division method

b. 9, 12, 18, 24

2	9, 12, 18, 24
3	9 6 9 12
2	3 2 3 4
3	3 1 3 2
2	1 1 1 2
	1 1 1 1

$$\text{L.C.M} = 2 \times 3 \times 2 \times 3 \times 2 = 72$$



EXERCISE 8 [C]

Find the L.C.M. of each numbers using division method

c. 8, 40, 54, 135

2	8, 40, 54, 135
3	4 20 27 135
3	4 20 9 45
3	4 20 3 15
2	4 20 1 5
2	2 10 1 5
5	1 5 1 5
	1 1 1 1

$$\text{L.C.M} = 2 \times 3 \times 3 \times 3 \times 2 \times 2 \times 5 = 1080$$



EXERCISE 8 [C]

Find the L.C.M. of each numbers using division method

d. 21, 33, 42, 44

3	21, 33, 42, 44
7	7 1 14 44
2	1 1 2 44
2	1 1 1 22
11	1 1 1 1
1	1 1 1 1

$$\text{L.C.M} = 3 \times 7 \times 2 \times 2 \times 11 = 924$$



EXERCISE 8 [C]

Find the L.C.M. of each numbers using division method

e. 15, 30, 60, 90

3	15, 30, 60, 90
2	5 10 20 30
5	5 5 10 15
3	1 1 2 3
2	1 1 2 1
	1 1 1 1

$$\text{L.C.M} = 3 \times 2 \times 5 \times 3 \times 2 = \mathbf{180}$$



EXERCISE 8 [C]

Find the L.C.M. of each numbers using division method

f. 25, 50, 55, 110

5	25, 50, 55, 110
5	5 10 1 22
1	1 2 1 22
11	1 2 1 2
2	1 1 1 1

$$\text{L.C.M} = 5 \times 5 \times 2 \times 11 = 550$$



**HOME ASSIGNMENT : Complete Exercise 8 C
Q.No. 2 [g] and [h] in the notebook.**



LEARNING OUTCOME:

Students are able

- **To Understand the concept of Multiples and Least common multiple.**
- **To find out common multiples and L.C.M.**

THANKING YOU
ODM EDUCATIONAL GROUP

MONTH : AUGUST

SESSION : 7

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : RELATION BETWEEN H.C.F. , L.C.M. AND

NUMBERS, EXERCISE 8 D Q.NO.1

CHANGING YOUR TOMORROW

Relation between H.C.F. , L.C.M. and the numbers.

1. L.C.M. \times H.C.F. = Product of the two numbers.

Explanation: Consider 6 and 8

STEP.

1

$$\begin{array}{l|l} 2 & 6, 8 \\ \hline & 3, 4 \end{array}$$

H.C.F. of 6 and 8 = **2**

STEP.

2

$$\begin{array}{l|l} 2 & 6, 8 \\ \hline 2 & 3, 4 \\ \hline 2 & 3, 2 \\ \hline 3 & 3, 1 \\ \hline & 1, 1 \end{array}$$

L.C.M. of 6 and 8 = $2 \times 2 \times 2 \times 3 =$ **24**

Relation between H.C.F. , L.C.M. and the numbers.

$$\text{L.C.M.} \times \text{H.C.F.} = 24 \times 2 = 48$$

$$\text{Product of the two numbers} = 6 \times 8 = 48$$

∴ **L.C.M. × H.C.F. = Product of the two numbers.**



Relation between H.C.F. , L.C.M. and the numbers.

IMPORTANT RULES

i. L.C.M. of two numbers = $\frac{\text{Their product}}{\text{Their H.C.F.}}$

ii. H.C.F. of two numbers = $\frac{\text{Their product}}{\text{Their L.C.M.}}$

iii. $\frac{\text{L.C.M.} \times \text{H.C.F.}}{\text{One number}} = \text{The other number}$



Relation between H.C.F. , L.C.M. and the numbers.

EXAMPLE- 1 :

The H.C.F. of two number is 28 and their L.C.M. is 336.
 if one number is 112 , find the other number.

Solution:

$$\frac{\text{L.C.M.} \times \text{H.C.F}}{\text{One number}} = \text{The other number}$$

$$\Rightarrow \text{the other number} = \frac{28 \times \overset{3}{\cancel{336}}}{\cancel{112}} = 28 \times 3 = 84 \text{ Ans.}$$



EXERCISE 8 [D]

1. Find the H.C.F. and L.C.M. of the following numbers.

a. 576 and 1440

H.C.F

$$\begin{array}{r} 2 \\ 576 \overline{) 1440} \\ \underline{1152} \quad 2 \\ 288 \overline{) 576} \\ \underline{576} \\ 0 \end{array}$$

H.C.F. of 576 and 1440 = **288**

EXERCISE 8 [D]

1. Find the H.C.F. and L.C.M. of the following numbers.

a. 576 and 1440

L.C.M.

2	576 , 1440
2	288 , 720
2	144 , 360
3	72 , 180
3	24 , 60
2	8 , 20
2	4 , 10
2	2 , 5
5	1 , 5
	1 , 1

L.C.M. of 576 and 1440 = $2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5 = 2880$

EXERCISE 8 [D]

1. Find the H.C.F. and L.C.M. of the following numbers.

b. 496 and 1116

H.C.F

$$\begin{array}{r} 2 \\ 496 \overline{) 1116} \\ \underline{992} \quad 4 \\ 124 \overline{) 496} \\ \underline{496} \\ 0 \end{array}$$

H.C.F. of 496 and 1116 = **124**

EXERCISE 8 [D]

1. Find the H.C.F. and L.C.M. of the following numbers.

b. 496 and 1116

L.C.M.

$$\begin{array}{r|l} 2 & 496 \\ \hline 2 & 248 \\ \hline 2 & 124 \\ \hline 2 & 62 \\ \hline 31 & 31 \\ \hline & 1 \end{array}$$

$$\begin{array}{r|l} 2 & 1116 \\ \hline 2 & 558 \\ \hline 3 & 279 \\ \hline 3 & 93 \\ \hline 31 & 31 \\ \hline & 1 \end{array}$$

Common multiples :

$$496 = 2 \times 2 \times 2 \times 2 \times 31$$

$$1116 = 2 \times 2 \times 3 \times 3 \times 31$$

$$\text{L.C.M. of 496 and 1116} = 2 \times 2 \times 31 \times 2 \times 2 \times 3 \times 3 = \mathbf{4464}$$

EXERCISE 8 [D]

1. Find the H.C.F. and L.C.M. of the following numbers.

H.C.F

c. 270 and 450

$$\begin{array}{r} 1 \\ 270 \overline{) 450} \\ \underline{270} \quad 1 \\ 180 \overline{) 270} \\ \underline{180} \quad 2 \\ 90 \overline{) 180} \\ \underline{180} \\ 0 \end{array}$$

H.C.F. of 270 and 450 = **90**

EXERCISE 8 [D]

1. Find the H.C.F. and L.C.M. of the following numbers.

c. 270 and 450

L.C.M.

2	270
5	135
3	27
3	9
3	3
	1

2	450
5	225
5	45
3	9
3	3
	1

Common multiples :

$$270 = 2 \times 5 \times 3 \times 3 \times 3$$

$$450 = 2 \times 5 \times 5 \times 3 \times 3$$

$$\text{L.C.M. of 270 and 450} = 2 \times 5 \times 3 \times 3 \times 3 \times 5 = 1350$$

EXERCISE 8 [D]

1. Find the H.C.F. and L.C.M. of the following numbers.

H.C.F

d. 465 and 1116

$$\begin{array}{r} 2 \\ 465 \overline{) 1116} \\ \underline{930} \\ 186 \\ 186 \\ \underline{0} \end{array}$$

2

$$\begin{array}{r} 2 \\ 186 \overline{) 465} \\ \underline{372} \\ 93 \\ 93 \\ \underline{0} \end{array}$$

H.C.F. of 465 and 1116 = **93**

EXERCISE 8 [D]

1. Find the H.C.F. and L.C.M. of the following numbers.

d. 465 and 1116

L.C.M.

$$\begin{array}{r|l} 5 & 465 \\ \hline 3 & 93 \\ \hline 31 & 31 \\ \hline & 1 \end{array}$$

$$\begin{array}{r|l} 2 & 1116 \\ \hline 2 & 558 \\ \hline 3 & 279 \\ \hline 3 & 93 \\ \hline 31 & 31 \\ \hline & 1 \end{array}$$

Common multiples :

$$465 = 5 \times 3 \times 31$$

$$1116 = 2 \times 2 \times 3 \times 3 \times 31$$

$$\text{L.C.M. of 465 and 1116} = 3 \times 31 \times 2 \times 2 \times 3 \times 5 = \mathbf{5580}$$

EXERCISE 8 [D]

1. Find the H.C.F. and L.C.M. of the following numbers.

e. 408 and 1530

H.C.F

$$\begin{array}{r} 3 \\ 408 \overline{) 1530} \\ \underline{1224} \quad 1 \\ 306 \overline{) 408} \\ \underline{306} \quad 3 \\ 102 \overline{) 306} \\ \underline{306} \\ 0 \end{array}$$

H.C.F. of 408 and 1530 = **102**

EXERCISE 8 [D]

1. Find the H.C.F. and L.C.M. of the following numbers.

e. 408 and 1530

L.C.M.

$$\begin{array}{r|l} 2 & 408 \\ \hline 2 & 204 \\ \hline 2 & 102 \\ \hline 3 & 51 \\ \hline 17 & 17 \\ \hline & 1 \end{array}$$

$$\begin{array}{r|l} 2 & 1530 \\ \hline 5 & 765 \\ \hline 3 & 153 \\ \hline 3 & 51 \\ \hline 17 & 17 \\ \hline & 1 \end{array}$$

Common multiples :

$$408 = 2 \times 2 \times 2 \times 3 \times 17$$

$$1530 = 2 \times 5 \times 3 \times 3 \times 17$$

$$\text{L.C.M. of 408 and 1530} = 2 \times 3 \times 17 \times 2 \times 2 \times 5 \times 3 = \mathbf{6120}$$

EXERCISE 8 [D]

1. Find the H.C.F. and L.C.M. of the following numbers.

H.C.F

f. 603 and 1608

$$\begin{array}{r} 2 \\ 603 \overline{) 1608} \\ \underline{1206} \quad 1 \\ 402 \overline{) 603} \\ \underline{402} \quad 2 \\ 201 \overline{) 402} \\ \underline{402} \\ 0 \end{array}$$

H.C.F. of 603 and 1608 = **201**

EXERCISE 8 [D]

1. Find the H.C.F. and L.C.M. of the following numbers.

f. 603 and 1608

L.C.M.

$$\begin{array}{r|l}
 3 & 603 \\
 \hline
 3 & 201 \\
 \hline
 67 & 67 \\
 \hline
 & 1
 \end{array}$$

$$\begin{array}{r|l}
 2 & 1608 \\
 \hline
 2 & 804 \\
 \hline
 2 & 402 \\
 \hline
 3 & 201 \\
 \hline
 67 & 67 \\
 \hline
 & 1
 \end{array}$$

Common multiples :

$$603 = 3 \times 3 \times 67$$

$$1608 = 2 \times 2 \times 2 \times 3 \times 67$$

$$\text{L.C.M. of 603 and 1608} = 3 \times 67 \times 2 \times 2 \times 2 \times 3 = \mathbf{4824}$$

LEARNING OUTCOME:

Students are able

- **To Understand the concept of H.C.F. and L.C.M.**
- **To understand the relation between H.C.F. and L.C.M.**

THANKING YOU
ODM EDUCATIONAL GROUP

MONTH : AUGUST

SESSION : 8

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : RELATION BETWEEN H.C.F. , L.C.M. AND

NUMBERS, EXERCISE 8 D Q.NO. 2 AND 3

CHANGING YOUR TOMORROW

Relation between H.C.F. , L.C.M. and the numbers.

EXAMPLE – 2

Find the smallest number of 4 digits which when divided by 6, 8, 12 and 20 leaves no remainder

- According to the question we have to find the **smallest number** which can be divided by each of the given numbers.
- So we find the **L.C.M.**

$$\begin{array}{r|l} 2 & 6, 8, 12, 20 \\ \hline 2 & 3, 4, 6, 10 \\ \hline 3 & 3, 2, 3, 5 \\ \hline 2 & 1, 2, 1, 5 \\ \hline 5 & 1, 1, 1, 5 \\ \hline & 1, 1, 1, 1 \end{array}$$

$$\text{L.C.M.} = 2 \times 2 \times 3 \times 2 \times 5 = \mathbf{120}$$

Relation between H.C.F. , L.C.M. and the numbers.

- We have to find 4 digit number, and which is the smallest multiple of 120.
- The smallest 4 digit number= 1000
- Let's check whether 120 divides 1000 exactly.

$$\begin{array}{r} 8 \\ 120 \overline{) 1000} \\ \underline{960} \\ 40 \end{array}$$

- So the 8th multiple of 120 is a 3 digit number. **[960]**
- We'll take the 9th multiple of 120. which is $120 \times 9 = 1080$

Ans: So the smallest 4 digit number divisible by 6, 8, 12 and 20 is 1080

Relation between H.C.F. , L.C.M. and the numbers.

EXAMPLE – 3

Find the greatest number of 4 digits which when divided by 7, 10, 15, 21 and 28 leaves no remainder

We find the **L.C.M.**

2	7 , 10 , 15, 21 , 28
7	7 , 5 , 15 , 21 , 14
3	1 , 5 , 15 , 3 , 2
2	1 , 5 , 5 , 1 , 2
5	1 , 5 , 5 , 1 , 1
	1, 1, 1, 1, 1

$$\text{L.C.M.} = 2 \times 7 \times 3 \times 2 \times 5 = 420$$

Relation between H.C.F. , L.C.M. and the numbers.

- The greatest 4 digit number= 9999
- Let's check whether 420 divides 9999 exactly.

$$\begin{array}{r} 23 \\ 420 \overline{) 9999} \\ \underline{840} \\ 1599 \\ \underline{1260} \\ 339 \end{array}$$

The remainder is 339 .

- Subtract 339 from 9999 .
- [9999 – 339= 9660] which is divisible by 420.

Ans: So the greatest 4 digit number divisible by 7, 10, 15, 21 and 28 is **9660**

EXERCISE 8 [D]

2. The L.C.M. and H.C.F. of two numbers are 720 and 5 respectively. If one of the two numbers is 45, find the other number.

Solution:

$$\frac{\text{L.C.M.} \times \text{H.C.F.}}{\text{One number}} = \text{The other number}$$

$$\Rightarrow \text{the other number} = \frac{\cancel{720} \times \cancel{5}}{\cancel{45}} = 80 \text{ Ans.}$$

~~9~~

EXERCISE 8 [D]

3. The L.C.M. of 576 and 128 is 1152. Find the H.C.F.

Solution:

$$\text{H.C.F. of two numbers} = \frac{\text{Their product}}{\text{Their L.C.M.}}$$

$$\text{Their product} = 576 \times 128 = 73728$$

$$\text{H.C.F. of two numbers} = \frac{73728}{1152} = 64 \text{ Ans.}$$

ROUGH

$$\begin{array}{r} 576 \\ \times 128 \\ \hline 4608 \\ 11520 \\ 57600 \\ \hline 73728 \end{array}$$

LEARNING OUTCOME:

Students are able

- **To Understand the concept of H.C.F. and L.C.M.**
- **To understand the relation between H.C.F. and L.C.M.**

THANKING YOU
ODM EDUCATIONAL GROUP

MONTH : AUGUST

SESSION : 9

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : RELATION BETWEEN H.C.F. , L.C.M. AND

NUMBERS, EXERCISE 8 D Q.NO. 5 TO 8

CHANGING YOUR TOMORROW

EXERCISE 8 [D]

5. The greatest number which divides 1155 and 3080 exactly is 385. find the least number which is divisible by 1155 and 3080

Solution:

The greatest number that divides 1155 and 3080 is **385**.

Which means **H.C.F.** of 1155 and 3080 = **385**

The least number which is divisible by 1155 and 3080 is **L.C.M.**
of **1155 and 3080**



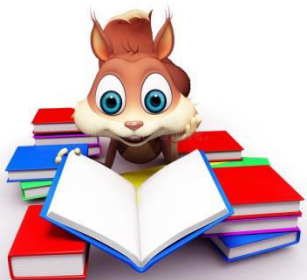
EXERCISE 8 [D]

1155 and 3080

5	1155 , 3080
3	231 , 616
7	77 , 616
11	11 , 88
2	1 , 8
2	1 , 4
2	1 , 2
	1 , 1

$$\text{L.C.M.} = 5 \times 3 \times 7 \times 11 \times 2 \times 2 \times 2 = 9240$$

∴ The least number divisible by 1155 and 3080 is 9240



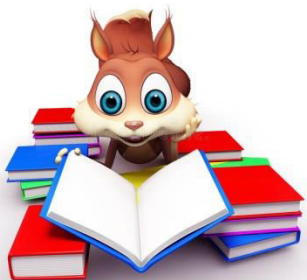
EXERCISE 8 [D]

6. Find the greatest number that can divide 663 and 975 exactly.

The H.C.F. of 663 and 975 = **39**

$$\begin{array}{r} 1 \\ 663 \overline{) 975} \\ \underline{663} \\ 312 \\ 312 \\ \underline{312} \\ 0 \end{array}$$

∴ The greatest number which can divide 663 and 975 exactly is **39**



EXERCISE 8 [D]

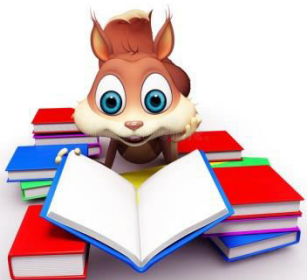
7. Which is the greatest 3-digit number which is exactly divisible by 9 and 21.

The L.C.M. of 9 and 21 = $3 \times 3 \times 7 = 63$

3	9, 21
3	3, 7
7	1, 7
	1, 1

The greatest 3-digit number = **999**

Let's find if 63 can divide 999 exactly



EXERCISE 8 [D]

$$\begin{array}{r} 15 \\ 63 \overline{) 999} \\ \underline{63} \\ 369 \\ \underline{315} \\ 54 \end{array}$$

54 = remainder

□ The greatest 3-digit number which is exactly divisible by 63 = $999 - 54 = 945$

•• The greatest 3-digit number which is exactly divisible by 9 and 21 is **945**



EXERCISE 8 [D]

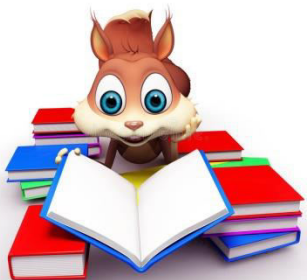
8. Find the greatest 4-digit number which is exactly divisible by 12, 32 and 48

The L.C.M. of 12, 32 and 48 = $2 \times 2 \times 2 \times 3 \times 2 \times 2 = 96$

2	12, 32, 48
2	6, 16, 24
2	3, 8, 12
3	3, 4, 6
2	1, 4, 2
2	1, 2, 1
	1, 1, 1

The greatest 4-digit number = **9999**

Let's find if 96 can divide 9999 exactly



EXERCISE 8 [D]

$$\begin{array}{r} 104 \\ 96 \overline{) 9999} \\ \underline{96} \\ 39 \\ \underline{36} \\ 390 \\ \underline{360} \\ 390 \\ \underline{384} \\ 15 \end{array}$$

15 = remainder

□ The greatest 4-digit number which is exactly divisible by 96 = $9999 - 15 = 9984$

•• The greatest 4-digit number which is exactly divisible by 12, 32 and 48 is **9984**



EXERCISE 8 [D]

- Home Assignment – Complete Exercise 8 D
Q.No. 4,9 and 10 in your notebook.



LEARNING OUTCOME:

Students are able

- **To Understand the concept of H.C.F. and L.C.M.**
- **To understand the relation between H.C.F. and L.C.M.**

THANKING YOU
ODM EDUCATIONAL GROUP

MONTH : AUGUST

SESSION : 10

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : DOUBT CLEARING AND CLASS TEST

CHANGING YOUR TOMORROW

1. FILL IN THE BLANKS

$$5 \times 1 = 5$$

- a. _____ is the only prime number which is even.
- b. A number is divisible by _____ if it's one's digit carries 0 or 5.
- c. A number which has more than 2 factors is called a _____ number.
- d. _____ is a factor of every number.
- e. The 9th multiple of 18 is _____.



2. Do as directed

$3 \times 2 = 6$

**a. Find the L.C.M.
9 , 27 and 45**

**b. Find the H.C.F.
8 and 64**

c. Find the first 4 multiples of 15.



3. Solve **$2 \times 2 = 4$**

- a. Find the greatest number which divides 603 and 1608 exactly.
- b. The H.C.F of two numbers is 9 and their product is 2268. Find the L.C.M.



ANSWER

1. FILL IN THE BLANKS

$5 \times 1 = 5$

- a. 2 is the only prime number which is even.
- b. A number is divisible by 5 if it's one's digit carries 0 or 5.
- c. A number which has more than 2 factors is called a composite number.
- d. 1 is a factor of every number.
- e. The 9th multiple of 18 is 162.



2. Do as directed **$3 \times 2 = 6$** **a. Find the L.C.M.****9 , 27 and 45**

3	9	27	45
3	3	9	15
5	1	3	5
3	1	3	1
	1	1	1

$L.C.M. = 3 \times 3 \times 5 \times 3 = 135$



2. Do as directed **$3 \times 2 = 6$**

b. Find the H.C.F.
8 and 64

2	8 , 64
2	4 , 32
2	2 , 16
	1 , 8

$$\text{H.C.F.} = 2 \times 2 \times 2 = 8$$

c. Find the first 4 multiples of 15.

Ans. The first 4 multiples of 15 = 15 , 30 , 45 , 60



3. Solve **$2 \times 2 = 4$**

- a. Find the greatest number which divides 603 and 1608 exactly.

$$\begin{array}{r} 2 \\ \hline 603 \overline{) 1608} \\ \underline{1206} \quad 1 \\ \hline 402 \overline{) 603} \\ \underline{402} \quad 2 \\ \hline 201 \overline{) 402} \\ \underline{402} \\ \hline 0 \end{array}$$

H.C.F. = 201

3. Solve **$2 \times 2 = 4$**

b. The H.C.F of two numbers is 9 and their product is 2268.
Find the L.C.M.

Solution

L.C.M. of two numbers = $\frac{\text{Their product}}{\text{Their H.C.F.}}$

$$\text{L.C.M. of two numbers} = \frac{2268}{9} = \boxed{252}$$



LEARNING OUTCOME :

- Children are able to find H.C.F. and L.C.M. of different numbers.
- They are able to find prime numbers and composite numbers.



THANKING YOU
ODM EDUCATIONAL GROUP

SESSION : 17

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : TEST OF DIVISIBILITY: RULES AND EXAMPLES

CHANGING YOUR TOMORROW

Let's revise:

A. Numbers which are multiples of 2 are called even numbers.

Examples: 2, 4, 6, 8, 10, 12, 14, 16... etc.

B. Numbers which are not the multiples of 2 are odd numbers.

Examples: 1, 3, 5, 7, 9, 11, 13, 15... etc.



Even and Odd Numbers

EVEN NUMBERS	ODD NUMBERS
END IN	END IN
0 2 4	1 3 5
6 8	7 9
Ex: 12, 46, 30	Ex: 11, 37, 23

learn teacher

TEST OF DIVISIBILITY: 2



If its one's digit is **even** or **0**, then the number is divisible by 2

Examples: 0, 8, 36, 64, 1264... etc.

TEST OF DIVISIBILITY: 5

If its last [**one's**] digit is **0 or 5**, then the number is divisible by 5.

Examples: 15, 55, 90, 345, 7910

TEST OF DIVISIBILITY: 10

If the **one's digit** is 0, then the number is divisible
by 10.

Examples: 20, 250, 500, 12540... etc.



TEST OF DIVISIBILITY: 3

If the **sum** of its digits is divisible **by 3**, then the number is divisible by 3.

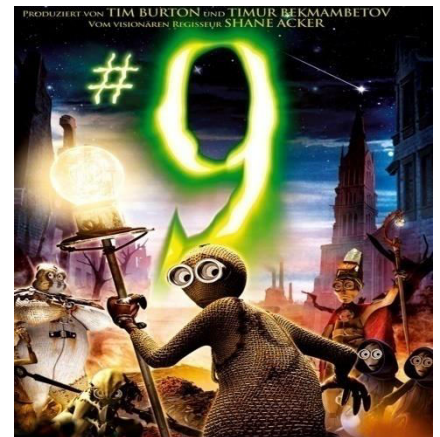
Examples: 6, 12, 21, 18, 111, 2163... etc.



TEST OF DIVISIBILITY: 9

If the **sum** of its digits is divisible **by 9** then, the number is divisible by 9.

Example: 18, 45, 72, 144, 3267... etc.



TEST OF DIVISIBILITY: 4

If the number formed by its **last two digits** are divisible by 4

or

If the last two digits are **both 0**, then the numbers is divisible by 4.

Examples: 124, 416, 5440, 9600



TEST OF DIVISIBILITY: 8

If the number formed by its **last three digits** are divisible by 8

or

If the last three digits are **0**, then the numbers is divisible by

8.
Examples: 124, 416, 5440, 9600



WRAP UP

A number is Divisible by	If the last digit is
2	0, 2, 4, 6, 8
5	0, 5
10	0

A number is Divisible by	If the sum of its digit is divisible by
3	3
9	9

A number is Divisible by	If it is divisible by
6	2 and 3
12	3 and 4
15	3 and 5

TEST OF DIVISIBILITY: 6

If the number is divisible by **both 2 and 3** , then it is divisible by 6.

Example: 72, 216, 3018, 21324... etc.

TEST OF DIVISIBILITY: 12

If it is divisible by **both 3 and 4**, then the number is divisible by 12

Example: 24, 60, 2700, 56100... etc.



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TEST OF DIVISIBILITY: 15

If it is divisible by **both 3 and 5**, then the number is divisible by 15.

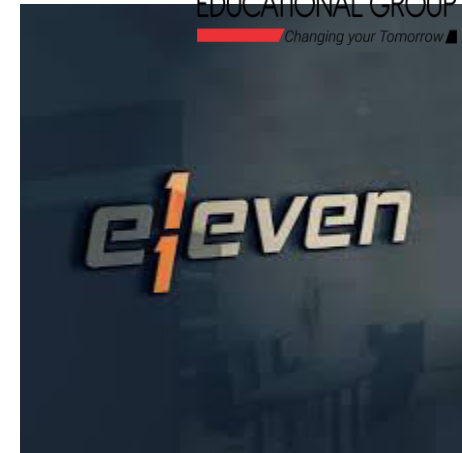
Example: 45, 90, 450, 2700... etc.



TEST OF DIVISIBILITY: 11

If the **difference** between the sum of the digits in the **odd** places and the sum of the digits in the **even** places is either **0** or **11**, then the number is divisible by 11

Examples: 308, 1331, 61809, 6556... etc.



Number	Sum of the digits (at odd places) From the right	Sum of the digits (at even places) From the right	Difference
308	$8 + 3 = 11$	0	$11 - 0 = 11$
1331	$1 + 3 = 4$	$3 + 1 = 4$	$4 - 4 = 0$
61809	$9 + 8 + 6 = 23$	$0 + 1 = 1$	$23 - 1 = 22$
6556	$6 + 5 = 11$	$6 + 5 = 11$	$11 - 11 = 0$

LEARNING OUTCOME :

Students are able to check the divisibility of a number by using the rules of tests of divisibility.

THANKING YOU
ODM EDUCATIONAL GROUP

SESSION : 18

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : TEST OF DIVISIBILITY

Exercise 8 A Q.No.1 & 2

CHANGING YOUR TOMORROW

A number is Divisible by	If the last digit is
2	0, 2, 4, 6, 8
5	0, 5
10	0

A number is Divisible by	If the sum of its digit is divisible by
3	3
9	9



A number is Divisible by	If it is divisible by
6	2 and 3
12	3 and 4
15	3 and 5

EXERCISE- 8 (A)

1. From the numbers given below mark the number which are divisible and which are not divisible by the numbers given on the left.

Divisible by	Numbers					
	99	184	7065	12480	23343	12210
3	✓	X	✓	✓	✓	✓
4	X	✓	X	✓	X	X
5	X	X	✓	✓	X	✓
6	X	X	X	✓	X	✓
9	✓	X	✓	X	X	X
11	✓	X	X	X	X	✓
12	X	X	X	✓	X	X
15	X	X	✓	✓	X	✓



EXERCISE- 8 (A)

2. What is the smallest number which should be (i) subtracted from and (ii) added to:

a. **3646** to get a number divisible by **3**

i. **1**

ii. **2**

Checking : $3 + 6 + 4 + 6 = 19$

$19 - 1 = 18$ or $19 + 2 = 21$

b. **12642** to get a number divisible by **4**

i. **2**

ii. **2**

c. **5213** to get a number divisible by **5**

i. **3**

ii. **2**



EXERCISE- 8 (A)

2. What is the smallest number which should be
(i) subtracted from and (ii) added to:

d. **7427** to get a number divisible by **6**

i. 5

ii. 1

e. **9466** to get a number divisible by **9**

i. 7

ii. 2

f. **26,303** to get a number divisible by **11**

i. 2

ii. 9



HOME ASSIGNMENT:

- **Complete Exercise – 8 A in your notebook.**



LEARNING OUTCOME :

Students are able to check the divisibility of a number by using the rules of tests of divisibility.

THANKING YOU
ODM EDUCATIONAL GROUP

SESSION : 19

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : Important facts Multiples and factors

Exercise- 8 A Q. No. 3

CHANGING YOUR TOMORROW

EXERCISE- 8 (A)

2. What is the smallest number which should be (i) subtracted from and (ii) added to:

a. **3646** to get a number divisible by **3** i. **1** ii. **2**

Checking : $3 + 6 + 4 + 6 = 19$
 $19 - 1 = 18$ or $19 + 2 = 21$

b. **12642** to get a number divisible by **4** i. **2** ii. **2**

Checking : $4 \times 10 = 40$, $4 \times 11 = 44$
So, we have to subtract 2 or add 2 to make it divisible by 4.

c. **5213** to get a number divisible by **5** i. **3** ii. **2**

EXERCISE- 8 (A)

2. What is the smallest number which should be (i) subtracted from and (ii) added to:

d. **7427** to get a number divisible by **6** i. 5 ii. 1

$$\begin{aligned}\text{Checking : } & 7 + 4 + 2 + 7 = 20 \\ & 20 - 5 = 15 \quad \text{and} \quad 20 + 1 = 21\end{aligned}$$

e. **9466** to get a number divisible by **9** i. 7 ii. 2

$$\begin{aligned}\text{Checking : } & 9 + 4 + 6 + 6 = 25 \\ & 25 - 7 = 18 \quad \text{and} \quad 25 + 2 = 27\end{aligned}$$

f. **26,303** to get a number divisible by **11** i. 2 ii. 9

$$\begin{aligned}\text{Checking : } & 3 + 3 + 2 = 8, \quad 0 + 6 = 6 \\ & 8 - 6 = 2 \quad (\text{Either it should be } 0 \text{ or } 11 \text{ or multiples of } 11) \\ & \text{So, we have to subtract } 2 \text{ or add } 9 \text{ to make it divisible by } 11.\end{aligned}$$

IMPORTANT FACTS

PRIME NUMBER

A **prime** number is a whole number **greater than 1** which has only **two different factors** namely **1** and the number **itself**.

Examples:- 1, 3, 5, 7, 11... etc.

2 is the only **even** number which is a **prime** number, all other prime numbers are **odd** numbers.

COMPOSITE NUMBER

A number which is **not a prime** number is a **composite** number. It has more than **2 factors**

Examples:- 4, 6, 8, 9, 10, 12, 16... etc.

1 is a **unique** number as it has only **one factor**. It is **neither prime nor composite** number.

MULTIPLE

A multiple of a number is a **product** of the number and a whole number.

Examples: multiples of 4 are: $4 \times 1 = 4$
 $4 \times 2 = 8$
 $4 \times 3 = 12 \dots$ etc.

So, multiples of 4 are 4, 8, 12,etc.

FACTORS

A factor is a **divisor** which divides a number **exactly**. Or the number is a factor of another number if it **divides** the number **exactly** .[0 as remainder]

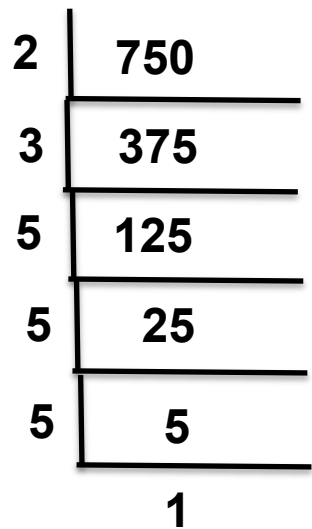
Examples: $15 \div 5 = 3$, here **5 is the factor of 15**
 $24 \div 4 = 6$, here **4 is the factor of 24**

A factor which is a **prime** number is called a **prime factor**.

We can find out prime factor of a number using short division method.

Short division method

Find the prime factors of 750



∴ Prime factors of 750 are 2, 3 and 5

EXERCISE 8 A

□ Q. 3 FIND OUT IF THE FIRST NUMBER IS THE FACTOR OF THE SECOND NUMBER. SAY “YES” OR “NO”.

a. 8 : 1 0 0 8

Yes

b. 7 : 6 5 8

Yes

c. 9 : 3 1 4 5

No

d. 1 1 : 3 6 4 4

No

EXERCISE 8 A

Q. 3 FIND OUT IF THE FIRST NUMBER IS THE FACTOR OF THE SECOND NUMBER. SAY “YES” OR “NO”.

e. 19 : 626

No

f. 17 : 398

No

g. 13 : 4163556

No

h. 12 : 780

Yes

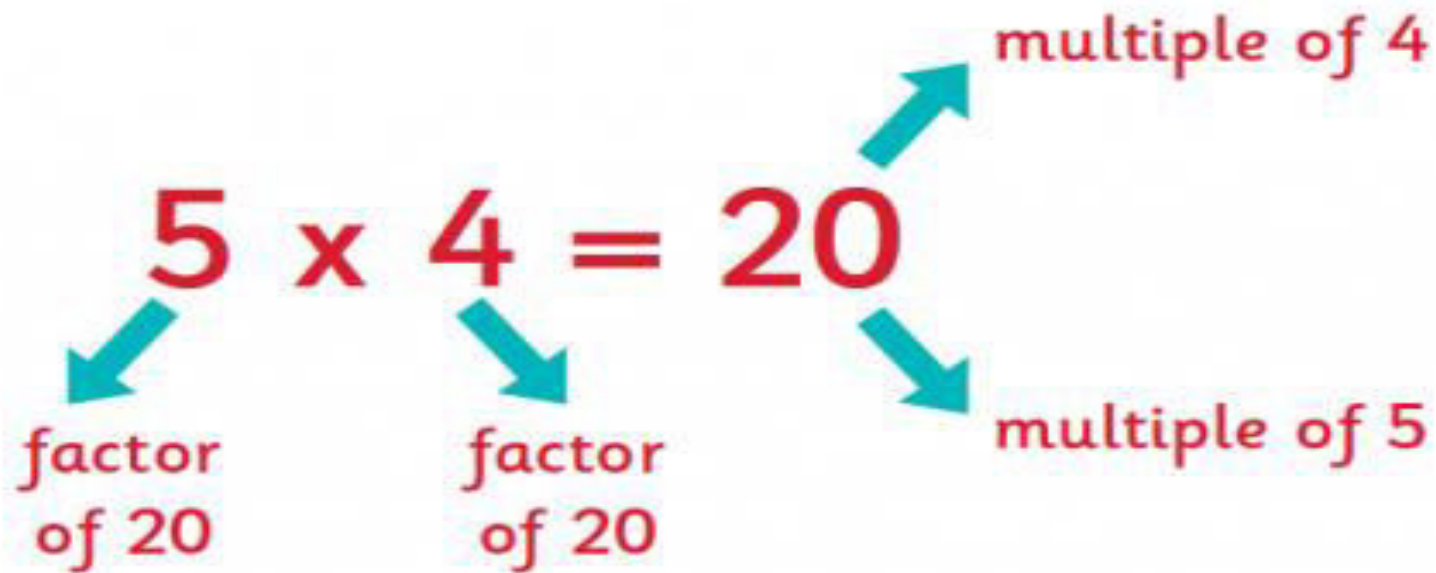
What have we learned so far?

Prime Number & Composite Numbers

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

What have we learned so far?

Factors And Multiples



LEARNING OUTCOME :

Students are able

- **To find out the multiples and factors of a number**
- **Understand the difference between multiples and factors**

THANKING YOU
ODM EDUCATIONAL GROUP

SESSION : 20

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : Co-prime , twin prime, properties of factors and multiples & Exercise 8 A Q.No. 4

CHANGING YOUR TOMORROW

Let's revise

Prime Number & Composite Numbers

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



CO-PRIME NUMBERS

- ❖ Those numbers which do **not** have a **common factor** between them **except 1** are called co-prime numbers.

- ❖ Example: factors of **16** are : 1,2,4,8,16
Factors of **25** are: 1,5, 25
 - The only **common factor** these two numbers is 1

 - So 16 and 25 are **co-prime** numbers.



CO-PRIME NUMBERS

- Two prime numbers are always **co-prime**
- Example: **5 & 11 , 13 & 23** etc.
- Two **consecutive numbers** are always **co-prime** as they will **not** have any **common factor** other than **1**

Example: factors of 20 → **1, 2, 4, 5, 10, 20**

Factors of 21 → **1, 3, 7, 21**

- Common factor is **1**
- Other Example: **4 & 5, 34 & 35** etc.

TWIN PRIME NUMBERS

❖ Twin prime numbers are two **consecutive prime numbers** whose difference is **2**

Examples:

❖ **3 & 5**

❖ **11 & 13**

❖ **17 & 19 etc.**



PROPERTIES OF FACTORS

❖ 1 is a factor of every number.

❖ Every number is a factor of itself.

❖ Every number is a factor of 0

❖ A factor of a number is either less than or equal to the number.



PROPERTIES OF MULTIPLES

- ❖ Every number is a multiple of 1
- ❖ Every number is a multiple of itself.
- ❖ 0 is a multiple of every number.
- ❖ Every [non-zero] multiple of a whole number is either greater than or equal to that number.



Example : Find the factors of 48

Solution:

Method-1

$$1 \times 48 = 48$$

$$2 \times 24 = 48$$

$$3 \times 16 = 48$$

$$4 \times 12 = 48$$

$$6 \times 8 = 48$$

Method-2

$$48 \div 1 = 48$$

$$48 \div 2 = 24$$

$$48 \div 3 = 16$$

$$48 \div 4 = 12$$

$$48 \div 6 = 8$$

So, the factors of 48 are 1, 2, 3, 4, 6, 8, 12, 16, 24 and 48.



EXERCISE 8 [A]

4. LIST THE FACTORS OF THE FOLLOWING

a. 48 1 2 3 4 6 8 12 16 24 48

b. 63 1 3 7 9 21 63

c. 84 1 2 3 4 6 7 12 14 21 28 42 84

d. 108 1 2 3 4 6 9 12 18 27 36 54 108



EXERCISE 8 [A]

4. LIST THE FACTORS OF THE FOLLOWING

e. 32 1 2 4 8 16 32

f. 169 1 13 169

g. 343 1 7 49 343

h. 150 1 2 3 5 6 10 15 25 30 50 75 150



LEARNING OUTCOME :

Students are able

- **To understand the difference between multiples and factors**
- **To understand the concept of co-prime, twin prime numbers.**
- **To understand the properties of Factors and multiples.**

THANKING YOU
ODM EDUCATIONAL GROUP

SESSION : 21

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : Activity – Sieve of Eratosthenes

Exercise – 8 A Q. No. 6 to 11

CHANGING YOUR TOMORROW

Let's revise

SIEVE OF ERATOSTHENES

	2	3	4	5	6	7	8	9	10	Prime numbers
11	12	13	14	15	16	17	18	19	20	
21	22	23	24	25	26	27	28	29	30	
31	32	33	34	35	36	37	38	39	40	
41	42	43	44	45	46	47	48	49	50	
51	52	53	54	55	56	57	58	59	60	
61	62	63	64	65	66	67	68	69	70	
71	72	73	74	75	76	77	78	79	80	
81	82	83	84	85	86	87	88	89	90	
91	92	93	94	95	96	97	98	99	100	
101	102	103	104	105	106	107	108	109	110	
111	112	113	114	115	116	117	118	119	120	



EXERCISE 8 [A]

5. Find the multiples :

a. Find the first six multiples of 9 : **9, 18, 27, 36, 45 and 54**

b. Find the seventh multiple of 16 : **112**

c. Find the fifth multiple of 15 : **75**

d. Find the ninth multiple of 16 : **144**

e. Find the multiples of 11 greater than 55 but less than 180 :

66, 77, 88, 99, 110, 121, 132, 143, 154, 165, 176

f. Find the multiples of 15 greater than 120 but less than 225 :

135, 150, 165, 180, 195, 210



EXERCISE 8 [A]

6. Write down the prime numbers between :

a. 50 to 65

53, 59, and 61

b. 80 to 100

83, 89 and 97

c. 110 to 125

113

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



EXERCISE 8 [A]

7. Write down the composite numbers between :

a. 70 to 80 : **72, 74, 75, 76, 77, and 78**

b. 100 to 110 :

102, 104, 105, 106 and 108

c. 40 to 50 : **42, 44, 45, 46, 48, and 49**

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



EXERCISE 8 [A]

8. Is 1 a prime number ? **NO**

9. What is the smallest composite number ? **4**

10. Write the prime number which is even. **2**

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



EXERCISE 8 [A]

**11. Find the prime factors of the following numbers :
 27, 35, 63, 91, 100, 77, 54, and 143.**

a)

$$\begin{array}{r} 3 \overline{) 27} \\ \underline{3} \\ 9 \\ \underline{9} \\ 0 \end{array}$$

3

So, Prime factors of 27 is 3.

c)

$$\begin{array}{r} 3 \overline{) 63} \\ \underline{3} \\ 21 \\ \underline{21} \\ 0 \end{array}$$

7

So, Prime factors of 63 are 3 and 7.

b)

$$\begin{array}{r} 5 \overline{) 35} \\ \underline{5} \\ 0 \end{array}$$

7

So, Prime factors of 35 are 5 and 7.

d)

$$\begin{array}{r} 7 \overline{) 91} \\ \underline{7} \\ 13 \end{array}$$

So, Prime factors of 91 is 7 and 13.

EXERCISE 8 [A]

**11. Find the prime factors of the following numbers :
 27, 35, 63, 91, 100, 77, 54, and 143.**

e)

$$\begin{array}{r}
 2 \overline{) 100} \\
 \underline{200} \\
 2 \overline{) 50} \\
 \underline{100} \\
 5 \overline{) 25} \\
 \underline{50} \\
 5
 \end{array}$$

So, Prime factors of 100 are 2 and 5.

g)

$$\begin{array}{r}
 2 \overline{) 54} \\
 \underline{108} \\
 3 \overline{) 27} \\
 \underline{81} \\
 3 \overline{) 9} \\
 \underline{27} \\
 3
 \end{array}$$

So, Prime factors of 54 are 2 and 3.

f)

$$\begin{array}{r}
 7 \overline{) 77} \\
 \underline{77} \\
 11
 \end{array}$$

So, Prime factors of 77 are 7 and 11.

d)

$$\begin{array}{r}
 11 \overline{) 143} \\
 \underline{153} \\
 13
 \end{array}$$

So, Prime factors of 143 is 11 and 13.

HOME ASSIGNMENT:

- **Complete Exercise – 8 (A) Q.NO. 6 to 11 in your notebook.**

LEARNING OUTCOME:

Students are able

- **To understand the difference between multiples and factors**
- **To understand the concept of prime, composite, co-prime and twin prime numbers.**
- **To understand the properties of Factors and multiples.**

THANKING YOU
ODM EDUCATIONAL GROUP

SESSION : 22

CLASS : V

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 8

CHAPTER NAME : FACTORS AND MULTIPLES

SUB-TOPIC : EXTRA QUESTIONS (QUIZ)

CHANGING YOUR TOMORROW

EXERCISE 8 [A]

**11. Find the prime factors of the following numbers :
 27, 35, 63, 91, 100, 77, 54, and 143.**

a)

$$\begin{array}{r} 3 \overline{) 27} \\ \underline{3 } \\ 9 \\ \underline{9} \\ 0 \end{array}$$

So, Prime factors of 27 is 3.

c)

$$\begin{array}{r} 3 \overline{) 63} \\ \underline{3 } \\ 21 \\ \underline{21} \\ 0 \end{array}$$

So, Prime factors of 63 are 3 and 7.

b)

$$\begin{array}{r} 5 \overline{) 35} \\ \underline{5 } \\ 0 \end{array}$$

So, Prime factors of 35 are 5 and 7.

d)

$$\begin{array}{r} 7 \overline{) 91} \\ \underline{7 } \\ 13 \end{array}$$

So, Prime factors of 91 is 7 and 13.

EXERCISE 8 [A]

**11. Find the prime factors of the following numbers :
 27, 35, 63, 91, 100, 77, 54, and 143.**

e)

$$\begin{array}{r}
 2 \overline{) 100} \\
 \underline{200} \\
 2 \overline{) 50} \\
 \underline{100} \\
 5 \overline{) 25} \\
 \underline{50} \\
 5
 \end{array}$$

So, Prime factors of 100 are 2 and 5.

g)

$$\begin{array}{r}
 2 \overline{) 54} \\
 \underline{108} \\
 3 \overline{) 27} \\
 \underline{81} \\
 3 \overline{) 9} \\
 \underline{27} \\
 3
 \end{array}$$

So, Prime factors of 54 are 2 and 3.

f)

$$\begin{array}{r}
 7 \overline{) 77} \\
 \underline{77} \\
 11
 \end{array}$$

So, Prime factors of 77 are 7 and 11.

d)

$$\begin{array}{r}
 11 \overline{) 143} \\
 \underline{153} \\
 13
 \end{array}$$

So, Prime factors of 143 is 11 and 13.

A number is Divisible by	If the last digit is
2	0, 2, 4, 6, 8
5	0, 5
10	0

A number is Divisible by	If the sum of its digit is divisible by
3	3
9	9



A number is Divisible by	If it is divisible by
6	2 and 3
12	3 and 4
15	3 and 5

Say Yes or No for each of the following :

- a) Is 49 a composite number ?
- b) Is 67 a composite number ?
- c) Is 99 a composite number ?
- d) Is 73 a prime number ?
- e) Is 59 a prime number ?
- f) Is 75 a prime number ?
- g) Is 89 a prime number ?
- h) Is 91 a prime number ?



Express each of the following as the sum of two prime numbers :

a) $12 = \underline{\quad\quad} + \underline{\quad\quad}$

b) $18 = \underline{\quad\quad} + \underline{\quad\quad}$

c) $20 = \underline{\quad\quad} + \underline{\quad\quad}$

d) $30 = \underline{\quad\quad} + \underline{\quad\quad}$

e) $36 = \underline{\quad\quad} + \underline{\quad\quad}$

f) $44 = \underline{\quad\quad} + \underline{\quad\quad}$



Express each of the following as the difference of two prime numbers :

a) $4 = \underline{\quad} - \underline{\quad}$

b) $10 = \underline{\quad} - \underline{\quad}$

c) $15 = \underline{\quad} - \underline{\quad}$

d) $20 = \underline{\quad} - \underline{\quad}$

e) $27 = \underline{\quad} - \underline{\quad}$

f) $31 = \underline{\quad} - \underline{\quad}$



ANSWERS

Say Yes or No for each of the following :

a) Is 49 a composite number ?

b) Is 67 a composite number ?

c) Is 99 a composite number ?

d) Is 73 a composite number ?

e) Is 59 a prime number ?

f) Is 75 a prime number ?

g) Is 89 a prime number ?

h) Is 91 a prime number ?



Express each of the following as the sum of two prime numbers:

a) $12 = \underline{7} + \underline{5}$

b) $18 = \underline{11} + \underline{7}$

c) $20 = \underline{17} + \underline{3}$

d) $30 = \underline{11} + \underline{19}$

e) $36 = \underline{17} + \underline{19}$

f) $44 = \underline{13} + \underline{31}$



Express each of the following as the difference of two prime numbers :

$$\text{a) } 4 = \frac{7}{\quad} - \frac{3}{\quad}$$

$$\text{b) } 10 = \frac{13}{\quad} - \frac{3}{\quad}$$

$$\text{c) } 15 = \frac{17}{\quad} - \frac{2}{\quad}$$

$$\text{d) } 20 = \frac{23}{\quad} - \frac{3}{\quad}$$

$$\text{e) } 27 = \frac{29}{\quad} - \frac{2}{\quad}$$

$$\text{f) } 32 = \frac{37}{\quad} - \frac{5}{\quad}$$



LEARNING OUTCOME:

Students are able

- **To understand the difference between multiples and factors**
- **To understand the concept of prime, composite, co-prime and twin prime numbers.**
- **To understand the properties of Factors and multiples.**

THANKING YOU
ODM EDUCATIONAL GROUP