

SETS

PERIOD 2

SUBJECT : MATHEMATICS

CHAPTER NUMBER: 6

CHAPTER NAME : SETS

CHANGING YOUR TOMORROW

Learning outcome

Students will be able to know about cardinal number of a set ,types of sets

Previous knowledge:

set-builder (Rule Method) form :

$$(i) \quad B_1 = \{6, 9, 12, 15, \dots\} \\ = \{x : x = 3n + 3; n \in \mathbb{N}\}$$

$$(ii) \quad B_2 = \{11, 13, 17, 19\} \\ = \{x : x \text{ is a prime number between} \\ \quad \quad \quad 10 \text{ and } 20\}$$

$$(iii) \quad B_3 = \left\{ \frac{1}{3}, \frac{3}{5}, \frac{5}{7}, \frac{7}{9}, \frac{9}{11}, \dots \right\} \\ = \left\{ x : x = \frac{n}{n+2}, \text{ where } n \text{ is an odd} \\ \quad \quad \quad \text{natural number} \right\}$$

$$(iv) \quad B_4 = \{8, 27, 64, 125, 216\} \\ = \{x : x = n^3; n \in \mathbb{N} \text{ and } 2 \leq n \leq \\ \quad \quad \quad 6\}$$

$$(v) \quad B_5 = \{-5, -4, -3, -2, -1\} \\ = \{x : x \in \mathbb{Z}, -5 \leq x \leq -1\}$$

$$(vi) \quad B_6 = \{\dots, -6, -3, 0, 3, 6, \dots\} \\ = \{x : x = 3n, n \in \mathbb{Z}\}$$

Exercise- 6(B)

1) Find the cardinal number of the following sets :

(i) $A_1 = \{-2, -1, 1, 3, 5\}$

(ii) $A_2 = \{x : x \in \mathbb{N} \text{ and } 3 \leq x < 7\}$

(iii) $A_3 = \{p : p \in \mathbb{W} \text{ and } 2p - 3 < 8\}$

(iv) $A_4 = \{b : b \in \mathbb{Z} \text{ and } -7 < 3b - 1 \leq 2\}$

Cardinal Number of a set; The number of elements in a set is called is Cardinal Number.

$$(i) A_1 = \{-2, -1, 1, 3, 5\}$$

Cardinal number of set $A_1 = 5$

$$(ii) A_2 = \{x : x \in \mathbb{N} \text{ and } 3 \leq x < 7\}$$
$$= \{3, 4, 5, 6\}$$

\therefore Cardinal number of set $A_2 = 4$

$$(iii) A_3 = \{P : P \in \mathbb{W} \text{ and } 2P - 3 < 8\}$$
$$2P - 3 < 8$$

$$\Rightarrow 2P - 3 + 3 < 8 + 3$$

(Adding 3 to both sides)

$$\Rightarrow 2P < 11$$

$$\Rightarrow P < \frac{11}{2}$$

(Dividing both sides by 2)

$$\Rightarrow P < 5.5$$

$$\therefore A_3 = \{0, 1, 2, 3, 4, 5\}$$

\therefore Cardinal number of set $A_3 = 6$

$$(iv) A_4 = \{b : b \in \mathbb{Z} \text{ and } -7 < 3b - 1 \leq 2\}$$
$$-7 < 3b - 1$$

$$\Rightarrow -7 + 1 < 3b - 1 + 1$$

(Adding 1 to both sides)

$$\Rightarrow -6 < 3b$$

$$\Rightarrow -\frac{6}{3} < b$$

(Dividing both sides by 3)

$$\Rightarrow -2 < b$$

Again $3b - 1 \leq 2$

$$\Rightarrow 3b - 1 + 1 \leq 2 + 1$$

(Adding 1 to both sides)

$$\Rightarrow 3b \leq 3$$

$$\Rightarrow b \leq \frac{3}{3}$$

(Dividing both sides by 3)

$$\Rightarrow b \leq 1$$

$$\therefore -2 < b \leq 1$$

$$\therefore \text{Given set } A_4 = \{-1, 0, 1\}$$

$$\therefore \text{Cardinal number of set } A_4 = 3$$

Exercise- 6(B)

2) If $P = \{P : P \text{ is a letter in the word "PERMANENT"}\}$. Find $n(P)$.

Sol: $P = \{P : P \text{ is a letter in the word "PERMANENT"}\}$
or $P = \{p, e, r, m, a, n, t\}$
 $n(P) = 7$

3) State, which of the following sets are finite and which are infinite :

- (i) $A = \{x : x \in \mathbb{Z} \text{ and } x < 10\}$
- (ii) $B = \{x : x \in \mathbb{W} \text{ and } 5x - 3 \leq 20\}$
- (iii) $P = \{y : y = 3x - 2, x \in \mathbb{N} \ \& \ x > 5\}$
- (iv) $M = \{r : r = \frac{3}{n}; n \in \mathbb{W} \text{ and } 6 < n \leq 15\}$

Note : (i) A set with finite (limited) number of elements in it, is called a finite set, (ii) A set which is not finite is called an infinite set.

Sol:

$$\begin{aligned}(i) \quad A &= \{x : x \in \mathbb{Z} \text{ and } x < 10\} \\ &= \{\dots, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9\} \\ &= \{9, 8, 7, 6, 5, 4, 3, 2, 1, 0, -1, -2, -3, -4, \dots\}\end{aligned}$$

\therefore It is an infinite set.

$$(ii) \quad B = \{x : x \in \mathbb{W} \text{ and } 5x - 3 \leq 20\}$$

$$5x - 3 \leq 20$$

$$\Rightarrow 5x - 3 + 3 \leq 20 + 3$$

(Adding 3 to both sides)

$$\Rightarrow 5x \leq 20 + 3$$

$$\Rightarrow 5x \leq 23$$

$$\Rightarrow x \leq \frac{23}{5}$$

(Dividing both sides by 5)

$$\Rightarrow x \leq 4.6$$

$$\therefore B = \{0, 1, 2, 3, 4\}$$

\therefore It is a finite set.

Home assignment

Ex 6(B) - 5 to 9

AHA

1. What is empty set? Give an example.
2. What are equivalent sets? Give an example.
3. What are equal sets? Give an example.

THANKING YOU
ODM EDUCATIONAL GROUP

