

Chapter- 16

Understanding Shapes

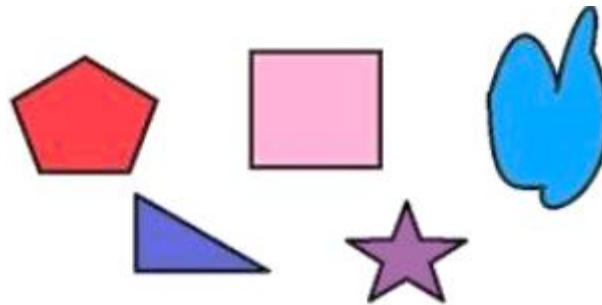
Plane Surface

A flat surface like paper is a plane surface.

Plane Curve

When we get a curve by joining the number of points without lifting the pencil is a plane curve.

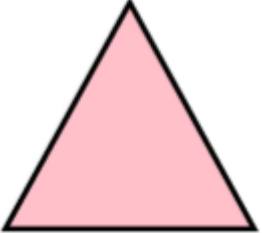
It could be an open or closed curve.

Open Curve**Closed Curve****Polygons**

The simple closed curves which are made up of line segments only are called the **Polygons**.

**Classification of Polygons**

Polygons can be classified by the **number of sides or vertices** they have.

Number of sides	Name of Polygon	Figure
3	Triangle	

4 Quadrilateral



5 Pentagon



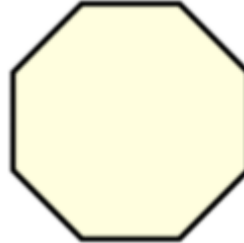
6 Hexagon



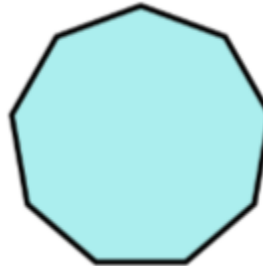
7 Heptagon



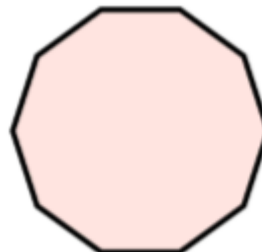
8 Octagon



9 Nonagon



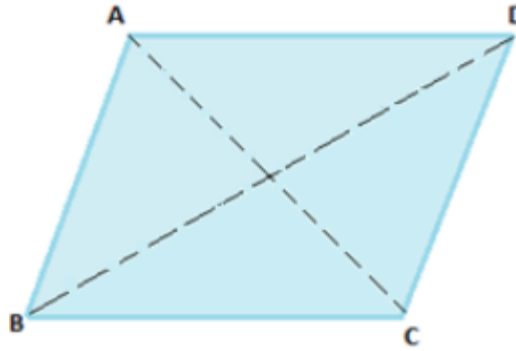
10 Decagon



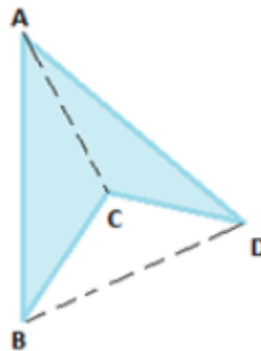
n n-gon

Convex and Concave Polygons

The polygons which have all the diagonals inside the figure are known as a **Convex Polygon**.



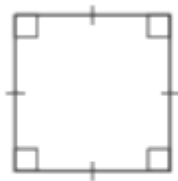
The polygons which have some of its diagonals outside the figure also are known as a **Concave Polygon**.



Regular and Irregular Polygons

Polygons which are equiangular and equilateral are called **Regular Polygons** i.e. a polygon is regular if-

- It's all sides are equal.
- It's all angles are equal.



Regular polygons

Polygons that are not regular

Hence square is a regular polygon but a rectangle is not as its angles are equal but sides are not equal.

Angle Sum Property

The sum of all the interior angles of a polygon remains the same according to the number of sides regardless of the shape of the polygon.

The sum of interior angles of a polygon is-

$$(n - 2) \times 180^\circ$$

Where n = number of sides of the polygon

Example

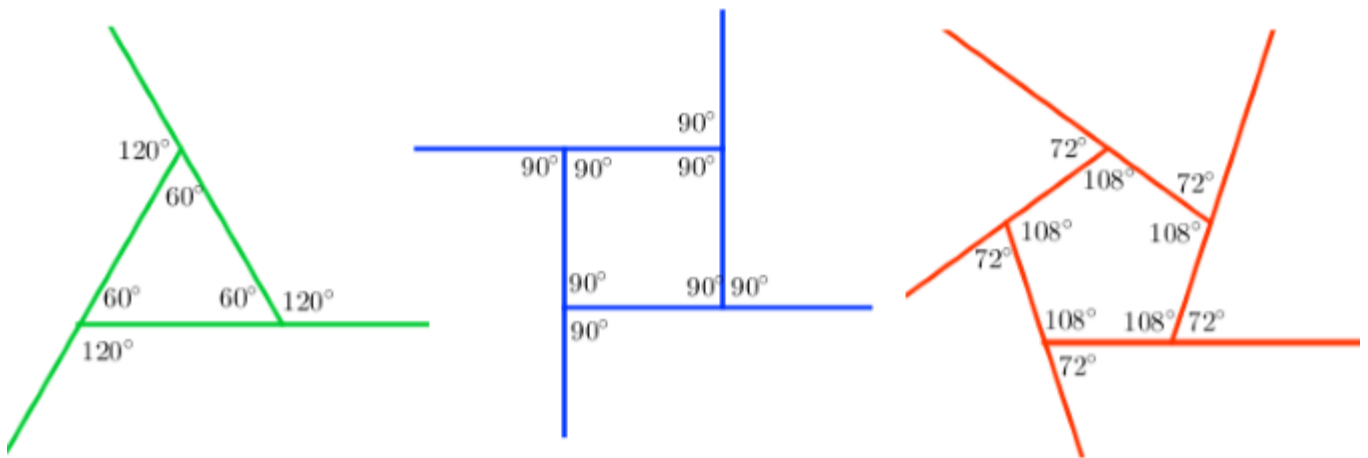
Polygon	Number of Sides	Sum of Interior Angles
Triangle	3	$(3 - 2) \times 180^\circ = 180^\circ$
Quadrilateral	4	$(4 - 2) \times 180^\circ = 360^\circ$
n-gon	n	$(n - 2) \times 180^\circ$

Remark: This property is applicable to both convex and concave polygon.

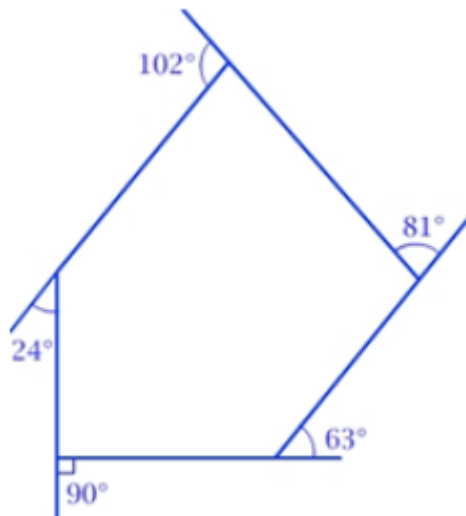
Sum of the Measures of the Exterior Angles of a Polygon

The sum of the exterior angles of any polygon will be 360° .

This is used to find the number of sides in a regular polygon.



This is applicable to **irregular polygon** also. The sum will remain the same whether it is a regular or irregular, small or large polygon.



Sum of all the exterior angles in the above irregular pentagon is

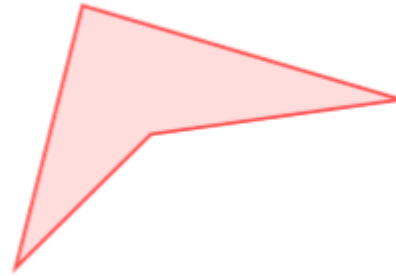
$$102^\circ + 81^\circ + 63^\circ + 90^\circ + 24^\circ = 360^\circ$$

Quadrilateral

Any closed polygon with four sides, four angles and four vertices are known as Quadrilateral. It could be a regular or irregular polygon.



Regular Quadrilateral



Irregular Quadrilateral

Angle sum property of a Quadrilateral

- Sum of all the interior angles of a Quadrilateral = 360°
- Sum of all the exterior angles of a Quadrilateral = 360°