

POLYNOMIALS

INTRODUCTION

SUBJECT : MATHEMATICS
CHAPTER NUMBER: 02
CHAPTER NAME : POLYNOMIALS

CHANGING YOUR TOMORROW

Learning outcome

- 1..Students will be able to define polynomial.
- 2.Students will be able to know the types of polynomials.
- 3.Students will be able to know the general form of linear, quadratic & cubic polynomial.
4. .Students will be able to know geometrical meaning of the zeros of a polynomial.

Introduction about polynomials ,its types and zero of a polynomial.
<https://youtu.be/NmpmGuNNqfl> {4.50}

POLYNOMIALS IN ONE VARIABLE

- A polynomial $p(x)$ in one variable x is an algebraic expression in x of the form

$p(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$ where $a_0, a_1, a_2, \dots, a_n$ are **constants (real numbers)** and $a_n \neq 0$.

$a_0, a_1, a_2, \dots, a_n$ are respectively the **coefficients** and **n** is called **the degree of the polynomial**. Each of a $a_n x^n, a_{n-1} x^{n-1}, \dots, a_0$ is called a **term** of the polynomial $p(x)$.

- ↳ Geometrical meaning of the zeroes of a polynomial
- ↳ <https://youtu.be/mBF7Gd7eiNo> {5.32}

A real number ' a ' is a **zero of a polynomial** $p(x)$ if

$p(a) = 0$. In this case, a is also called a *root* of the equation $p(x) = 0$.

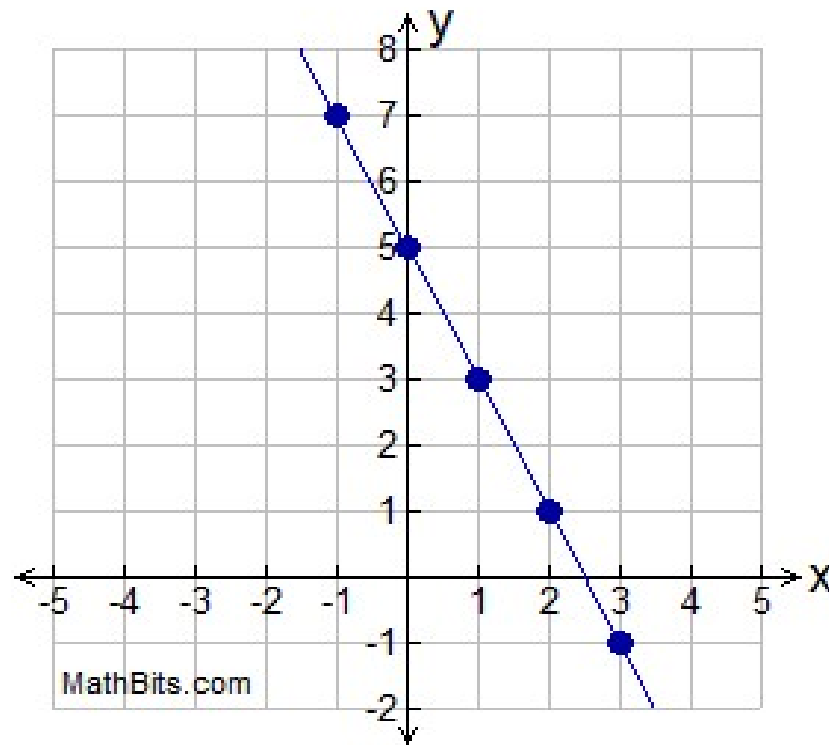
Every **linear polynomial** in one variable has a **unique zero**, a non-zero constant polynomial has no zero, and every real number is a zero of the zero polynomial.

A **quadratic polynomial** can have at most **2 zeroes** and a **cubic polynomial** can have at most **3 zeroes**

Geometrical Meaning of the Zeroes of a Polynomial

The linear polynomial $ax + b$, $a \neq 0$, has exactly one zero, namely $-b/a$ the x-coordinate of the point where the graph of $y = ax + b$ intersects the x-axis. Example : The zero of the linear polynomial $-2x + 5$ is $5/2$ the point where the graph linear equation $y = -2x + 5$ meets the x axis.

GRAPH OF LINEAR EQUATION $Y = -2X + 5$



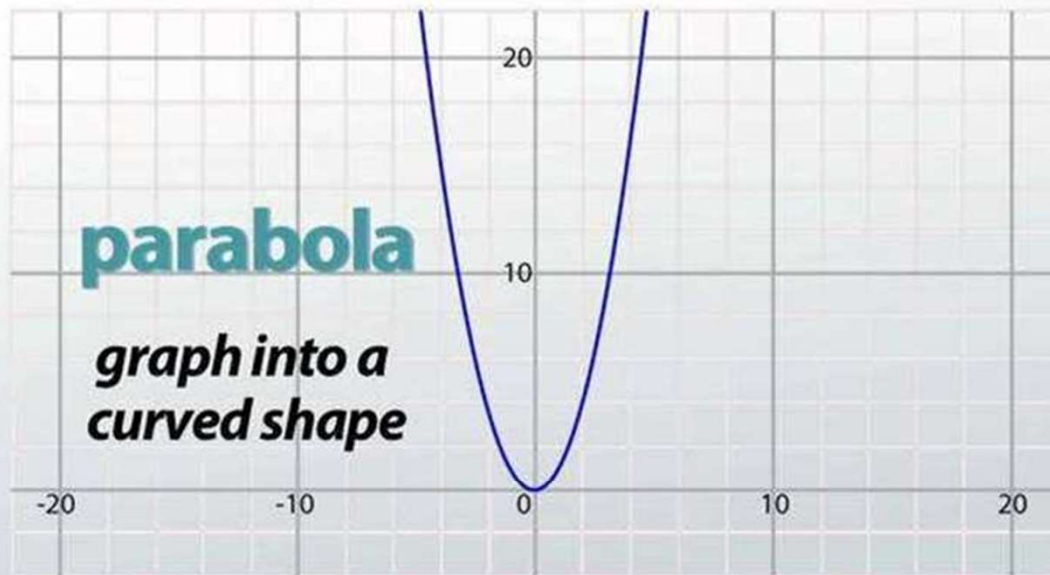
For any quadratic polynomial $ax^2 + bx + c$, $a \neq 0$, the graph of the corresponding equation

$y = ax^2 + bx + c$ has one of the two shapes U either open upwards or open downwards depending on whether $a > 0$ or $a < 0$.

These curves are called **parabolas**.

A parabola is a plane curve which is mirror symmetrical and approximately U-shaped.

GRAPHING QUADRATIC FUNCTIONS

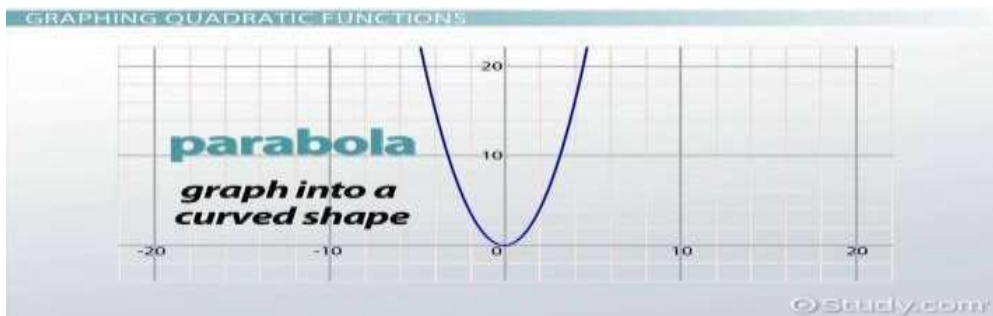


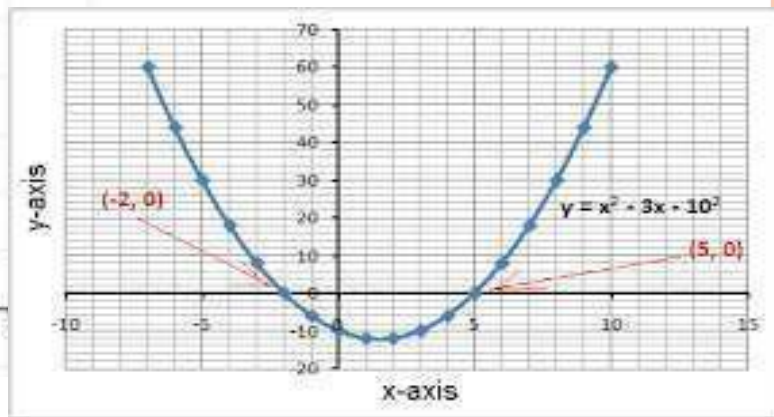
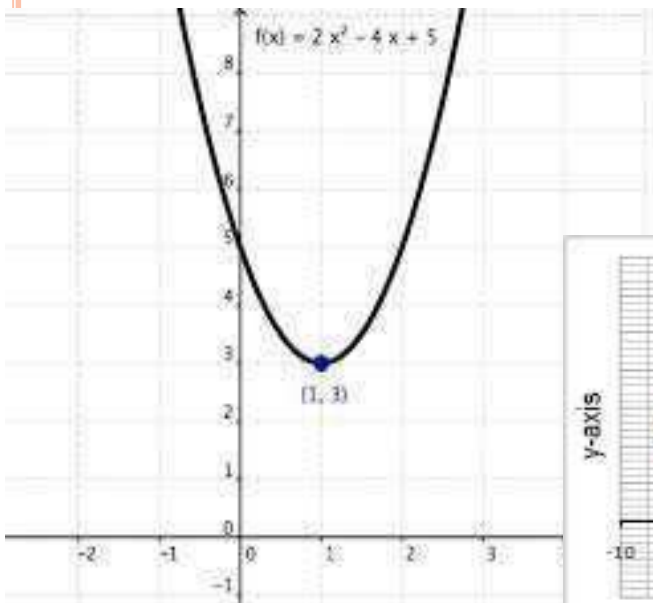
parabola

*graph into a
curved shape*

© Study.co

- ↵ The zeroes of a quadratic polynomial $ax^2 + bx + c$, $a \neq 0$, are precisely the **x-coordinates** of the points where the **parabola** representing $y = ax^2 + bx + c$ intersects the **x-axis**
- ↵ We can see geometrically, from the following graphs, that a quadratic polynomial can have either two distinct zeroes or two equal zeroes (i.e., one zero), or no zero. This also means that a polynomial of degree 2 has at most two zeroes



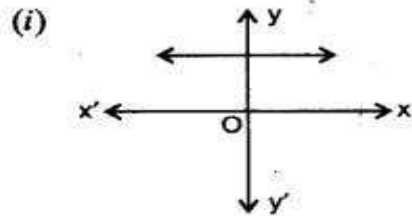


General form of linear polynomials $ax + b$ where $a \neq 0$

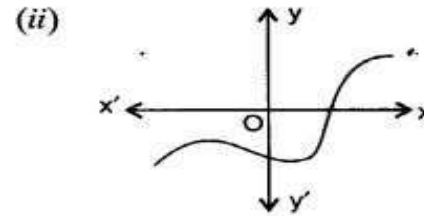
General form of quadratic polynomials $ax^2 + bx + c$ where $a \neq 0$

General form of cubic polynomial $ax^3 + bx^2 + cx + d$, where $a \neq 0$,

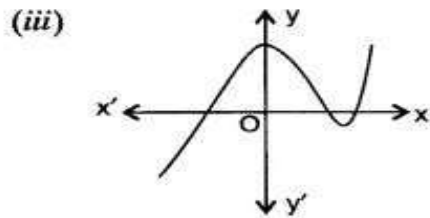
The number of zeroes of $p(x)$ in each graph given; are



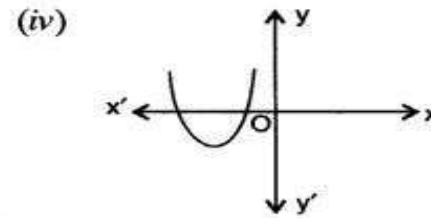
This graph shows $p(x)$ has no zero.



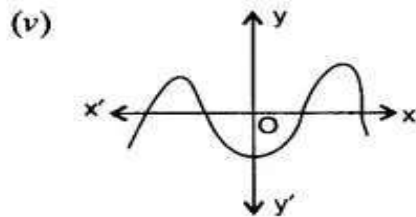
This graph shows $p(x)$ has one zero.



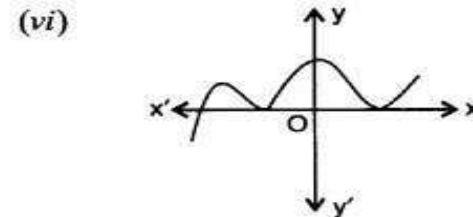
This graph shows $p(x)$ has three zeroes.



This graph shows $p(x)$ has two zeroes.



This graph shows $p(x)$ has four zeroes.



This graph shows $p(x)$ has three zeroes.

HOME ASSIGNMENT Ex. 2.1 Q. No 1

AHA

1. Draw the graph of x^2-3x-4
2. Draw the graph of $x^3- 4x$

THANKING YOU
ODM EDUCATIONAL GROUP

