

POLYNOMIALS

PPT-2

SUBJECT : MATHEMATICS
CHAPTER NUMBER: 02
CHAPTER NAME : POLYNOMIALS

CHANGING YOUR TOMORROW

Learning outcome

- 1..Students will be able to Students will be able to **know the relationship between zeroes and coefficients of a quadratic polynomial**
- 2.. Students will be able to solve questions involving relationship between zeroes and coefficients of a quadratic polynomial

PREVIOUS KNOWLEDGE TEST

- 1. A **polynomial $p(x)$ in one variable x** is an algebraic expression in x of the form

$$p(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0 \text{ where } a_0, a_1, a_2, \dots, a_n \text{ are constants (real numbers) and } a_n \neq 0.$$

$a_0, a_1, a_2, \dots, a_n$ are respectively the **coefficients** and n is called **the degree of the polynomial**. Each of $a_n x^n, a_{n-1} x^{n-1}, \dots, a_0$ is called a **term** of the polynomial $p(x)$.

2. Every **linear polynomial** in one variable has a **unique zero**, a non-zero constant polynomial has no zero, and every real number is a zero of the zero polynomial
- 3 A **quadratic polynomial** can have at most **2 zeroes** and a **cubic polynomial** can have at most **3 zeroes**
4. General form of linear polynomials $ax + b$ where $a \neq 0$
5. General form of quadratic polynomials $ax^2 + bx + c$ where $a \neq 0$
6. General form of cubic polynomial $ax^3 + bx^2 + cx + d$, where $a \neq 0$

Relationship between zeros and coefficient
<https://youtu.be/5FR1Hix5WLk>{8.06}



: Find the zeroes of the quadratic polynomial $x^2 + 7x + 10$, and verify the relationship between the zeroes and the coefficients.

Solution : We have $x^2 + 7x + 10$

$$= (x + 2)(x + 5)$$

So, the value of $x^2 + 7x + 10$ is zero when $x + 2 = 0$ or $x + 5 = 0$, i.e., when $x = -2$ or $x = -5$. Therefore, the zeroes of $x^2 + 7x + 10$ are -2 and -5 .

Now,

sum of zeroes = $(-2) + (-5) = -7 = -(\text{Coefficient of } x) / \text{Coefficient of } x^2$

product of zeroes = $(-2) \times (-5) = 10 = 10/1 = \text{Constant term} / \text{Coefficient of } x^2$

(iii) $6x^2 - 3 - 7x$

$$= 6x^2 - 7x - 3$$

$$= 6x^2 - 9x + 2x - 3$$

$$= 3x(2x - 3) + 1(2x - 3)$$

$$= (3x + 1)(2x - 3)$$

The value of $6x^2 - 7x - 3$ is zero if $3x + 1 = 0$ or $2x - 3 = 0$.

$$\Rightarrow x = -\frac{1}{3} \text{ or } x = \frac{3}{2}$$

Therefore, the zeroes of $6x^2 - 7x - 3$ are $-\frac{1}{3}$ and $\frac{3}{2}$. Now

$$\text{Sum of zeroes} = -\frac{1}{3} + \frac{3}{2} = \frac{-2 + 9}{6} = \frac{7}{6} = \frac{-(-7)}{6} = \frac{-(\text{Coefficient of } x)}{\text{Coefficient of } x^2}$$

$$\text{Product of zeroes} = \left(-\frac{1}{3}\right) \times \frac{3}{2} = -\frac{1}{2} = \frac{-3}{6} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$$

: Find a quadratic polynomial, the sum and product of whose zeroes are - 3 and 2, respectively.

Solution : Let the quadratic polynomial be $ax^2 + bx + c$, and its zeroes be α and β . We have $\alpha + \beta = - 3 = -b / a$, and $\alpha\beta = 2 = c / a$. If $a = 1$, then $b = 3$ and $c = 2$.

So, one quadratic polynomial which fits the given conditions is $x^2 + 3x + 2$..

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:HOME ASSIGNMENT Ex. 2.2 Q. No 1 & 2 & .

AHA

1. If α, β are the two zeroes of the polynomial $6y^2 - 7y + 2$, find a quadratic polynomial whose zeroes are $\frac{1}{\alpha}$ and $\frac{1}{\beta}$.
2. . If α, β are the two zeroes of the polynomial $3x^2 - 4x + 1$, find a quadratic polynomial whose zeroes are α^2 & β^2 .
3. If α, β are the two zeroes of the polynomial $3x^2 + 2x + 1$, find the quadratic polynomial whose zeroes are $1 - \frac{\alpha}{1 + \alpha}$ & $1 - \frac{\beta}{1 + \beta}$
4. . If α, β are the two zeroes of the polynomial $2x^2 - 5x + 7$, find the quadratic polynomial whose zeroes are $2\alpha + 3\beta$ and $3\alpha + 2\beta$.

THANKING YOU
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