

PERIOD 4

MATHEMATICS

CHAPTER NUMBER :~ 7

CHAPTER NAME :~ TRIANGLES

CHANGING YOUR TOMORROW

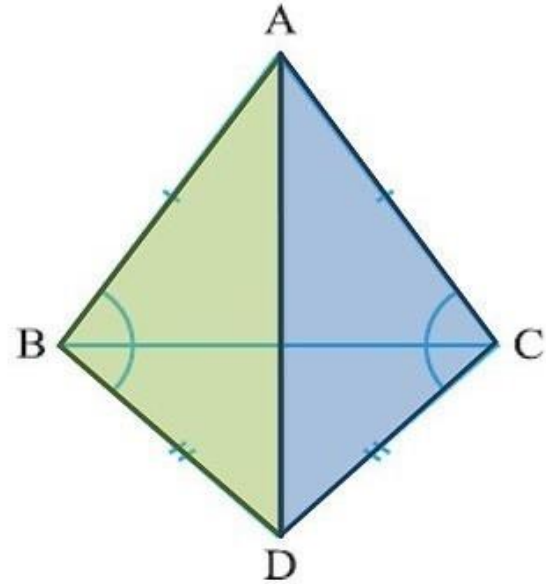
PREVIOUS KNOWLEDGE TEST

- 1. In $\triangle PQR$ the sides QP and RP have been produced to S and T such that $PQ=PS$ and $PR=PT$. Prove that the segment $QR\parallel ST$.

LEARNING OUTCOME:~

1. Students will be able to solve the sums based on ASA and AAS congruence rule.

ABC and DBC are two isosceles triangles on the same base BC (see the given figure). Show that $\angle ABD = \angle ACD$.



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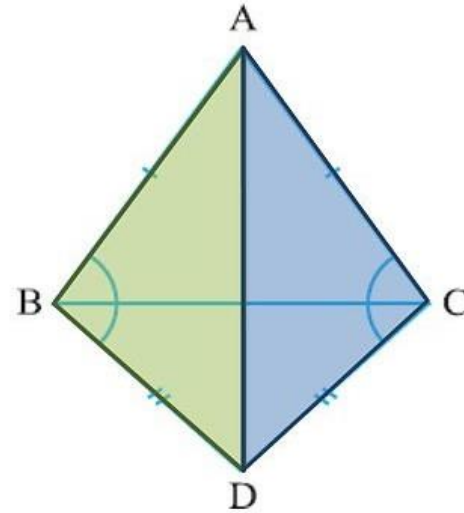
Given:

$\triangle ABC$ is isosceles

So, $AB = AC$... (1)

$\triangle DBC$ is isosceles

So, $DB = DC$... (2)



To prove: $\angle ABD = \angle ACD$

Proof

Let us join AD.

We take $\triangle ABD$ and $\triangle ACD$,

In $\triangle ABD$ and $\triangle ACD$,

$$AB = AC \quad (\text{From (1)})$$

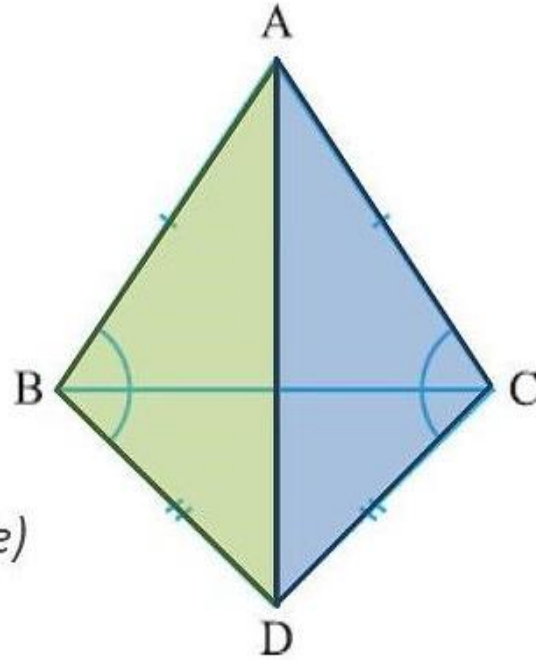
$$BD = CD \quad (\text{From (2)})$$

$$AD = AD \quad (\text{Common})$$

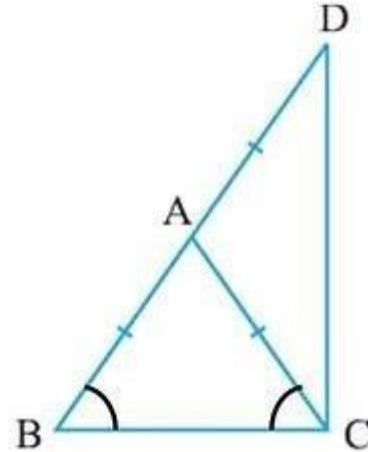
$$\therefore \triangle ABD \cong \triangle ACD \quad (\text{SSS congruence rule})$$

$$\Rightarrow \angle ABD = \angle ACD \quad (\text{CPCT})$$

Hence proved



$\triangle ABC$ is an isosceles triangle in which $AB = AC$. Side BA is produced to D such that $AD = AB$ (see the given figure). Show that $\angle BCD$ is a right angle.



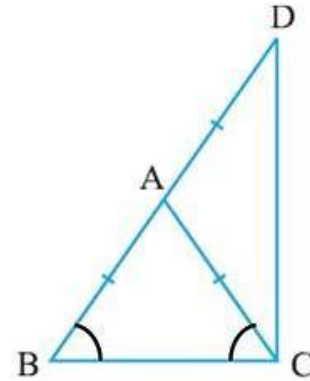
$\triangle ABC$ is an isosceles triangle in which $AB = AC$. Side BA is produced to D such that $AD = AB$ (see the given figure). Show that $\angle BCD$ is a right angle.

Given:

$$AB = AC$$

Also, $AD = AB$

$$\text{i.e. } AC = AB = AD$$



To prove: $\angle BCD = 90^\circ$

Proof:

In $\triangle ABC$,

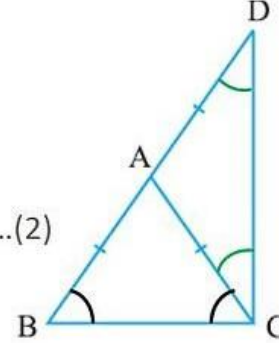
$$AB = AC$$

$$\Rightarrow \angle ACB = \angle ABC \quad (\text{Angles opposite to equal sides are equal}) \quad \dots(1)$$

In $\triangle ACD$,

$$AC = AD$$

$$\angle ADC = \angle ACD \quad (\text{Angles opposite to equal sides are equal}) \quad \dots(2)$$



In $\triangle BCD$,

$$\angle ABC + \angle BCD + \angle BDC = 180^\circ \quad (\text{Angle sum property of triangle})$$

$$\angle ACB + \angle BCD + \angle ACD = 180^\circ \quad (\text{From (1) \& (2)})$$

$$(\angle ACB + \angle ACD) + \angle BCD = 180^\circ$$

$$(\angle BCD) + \angle BCD = 180^\circ$$

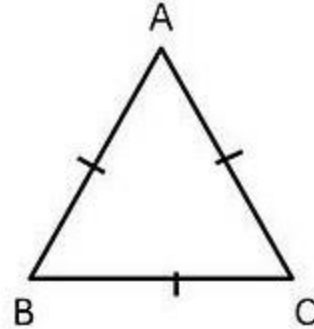
$$2\angle BCD = 180^\circ$$

$$\angle BCD = \frac{180^\circ}{2}$$

$$\angle BCD = 90^\circ$$

Hence proved

Show that the angles of an equilateral triangle are 60° each.

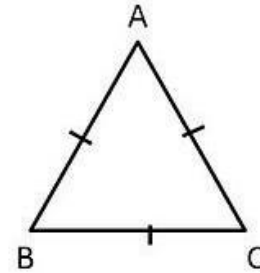


Show that the angles of an equilateral triangle are 60° each.

Given:

ΔABC be an equilateral triangle.

$\therefore AB = BC = AC$ (All sides of equilateral triangle are equal)



To prove: $\angle A = \angle B = \angle C = 60^\circ$

Proof:

$AB = AC$

$\Rightarrow \angle C = \angle B$ (Angles opposite to equal sides are equal) ... (1)

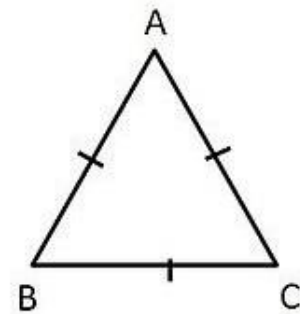
Also, $AC = BC$

$\Rightarrow \angle B = \angle A$ (Angles opposite to equal sides are equal) ... (2)

From (1) & (2)

$$\angle A = \angle B = \angle C$$

...(3)



In $\triangle ABC$,

$$\angle A + \angle B + \angle C = 180^\circ$$

(Angle sum property of triangle)

$$\Rightarrow \angle A + \angle A + \angle A = 180^\circ$$

(From (3))

$$\Rightarrow 3\angle A = 180^\circ$$

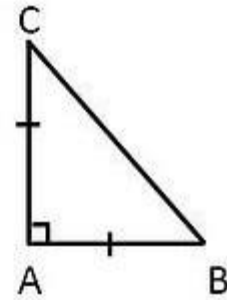
$$\Rightarrow \angle A = \frac{180^\circ}{3}$$

$$\Rightarrow \angle A = 60^\circ$$

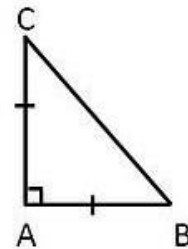
$$\therefore \angle A = \angle B = \angle C = 60^\circ$$

Hence proved

ABC is a right angled triangle in which $\angle A = 90^\circ$ and $AB = AC$. Find $\angle B$ and $\angle C$.



ABC is a right angled triangle in which $\angle A = 90^\circ$ and $AB = AC$. Find $\angle B$ and $\angle C$.



Given

$$AB = AC$$

$$\Rightarrow \angle C = \angle B \quad (\text{Angles opposite to equal sides are equal}) \quad \dots(1)$$

In $\triangle ABC$,

$$\angle A + \angle B + \angle C = 180^\circ \quad (\text{Angle sum property of triangles})$$

$$\Rightarrow 90^\circ + \angle B + \angle C = 180^\circ \quad (\text{Given that } \angle A = 90^\circ)$$

$$\Rightarrow 90^\circ + \angle B + \angle B = 180^\circ \quad (\text{From (1)})$$

$$\Rightarrow 2 \angle B = 90^\circ$$

$$\Rightarrow \angle B = 45^\circ$$

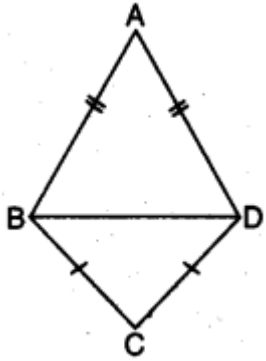
$$\therefore \angle B = \angle C = 45^\circ$$

HOMEWORK ASSIGNMENT

Exercise 7.2
Question number 5,6,7,8.

AHA

In the given figure, $\triangle ABD$ and $\triangle CBD$ are isosceles triangles on the same base BD . Prove that $\angle ABC = \angle ADC$.



THANKING YOU
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