

PERIOD 6

MATHEMATICS

CHAPTER NUMBER :~ 7

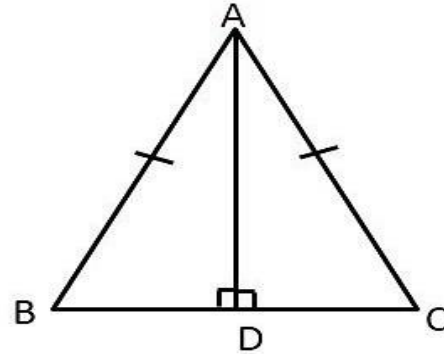
CHAPTER NAME :~ TRIANGLES

CHANGING YOUR TOMORROW

PREVIOUS KNOWLEDGE TEST

AD is an altitude of an isosceles triangle ABC in which $AB = AC$.
Show that

(i) AD bisects BC , (ii) AD bisects $\angle A$.

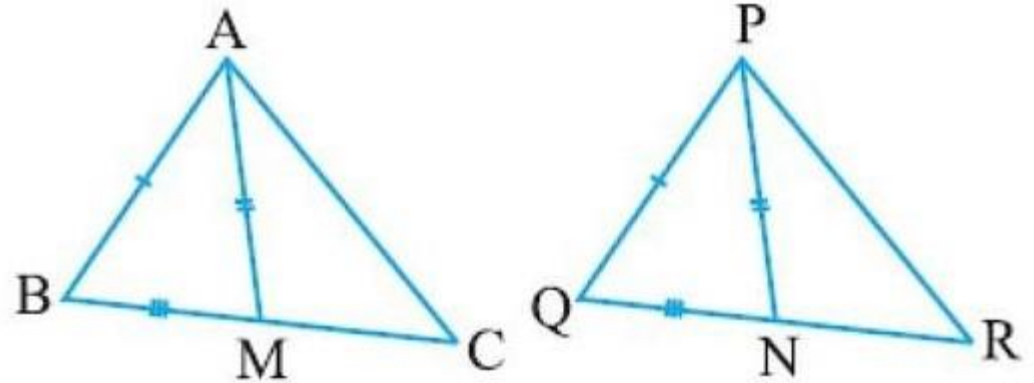


LEARNING OUTCOME:~

1. Students will be able to learn applications of Theorem 7.2 and 7.3.

Two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ and QR and median PN of $\triangle PQR$ (see figure).Show that :

(i) $\triangle ABM \cong \triangle PQN$



Two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ and QR and median PN of ΔPQR (see figure).Show that :

(i) $\Delta ABM \cong \Delta PQN$

Given:

$$AB = PQ \quad \dots(1)$$

$$BC = QR \quad \dots(2)$$

$$\& AM = PN \quad \dots(3)$$

Also, AM is the median of ΔABC

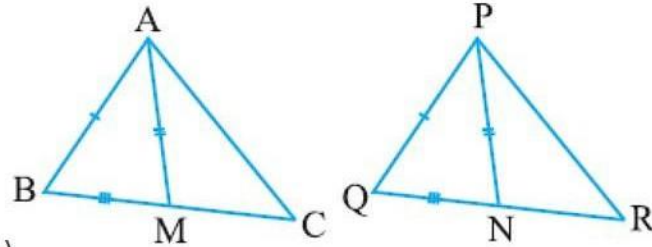
$$\text{So, } BM = CM = \frac{1}{2} BC$$

Also, PN is the median of ΔPQR

$$\text{So, } QN = RN = \frac{1}{2} QR$$

To prove: $\Delta ABM \cong \Delta PQN$

Proof



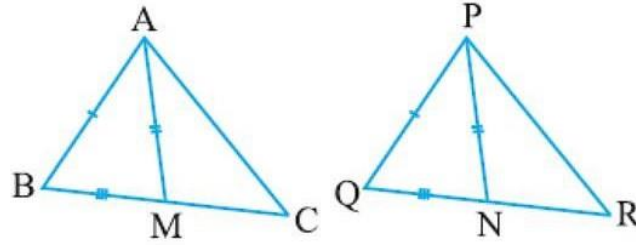
Since

$$BC = QR$$

$$\frac{1}{2} BC = \frac{1}{2} QR$$

$$BM = QN$$

...(4)



In ΔABM & ΔPQN

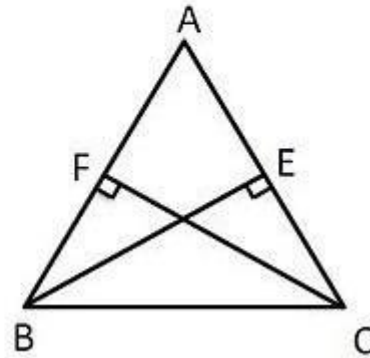
$$AB = PQ \quad (\text{From (1)})$$

$$AM = PN \quad (\text{From (3)})$$

$$BM = QN \quad (\text{From (6)})$$

So, $\Delta ABM \cong \Delta PQN$ (SSS congruence rule)

BE and CF are two equal altitudes of a triangle ABC . Using RHS congruence rule , prove that the triangle ABC is isosceles .



BE and CF are two equal altitudes of a triangle ABC . Using RHS congruence rule , prove that the triangle ABC is isosceles .

Given:

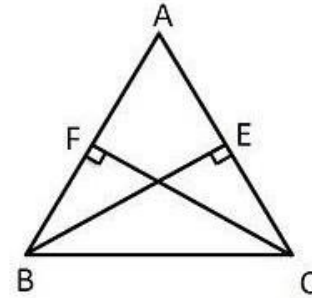
Given BE is a altitude,

So, $\angle AEB = \angle CEB = 90^\circ$... (1)

Also, CF is a altitude,

So, $\angle AFC = \angle BFC = 90^\circ$... (2)

Also, $BE = CF$... (3)



To prove: Δ ABC is isosceles

Proof:

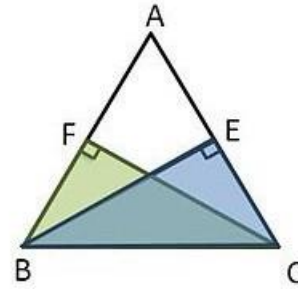
In $\triangle BCF$ and $\triangle CBE$

$$\angle BFC = \angle CEB = 90^\circ \quad (\text{Both } 90^\circ)$$

$$BC = CB \quad (\text{Common})$$

$$FC = EB \quad (\text{From (3)})$$

$$\triangle BCF \cong \triangle CBE \quad (\text{RHS congruence rule})$$



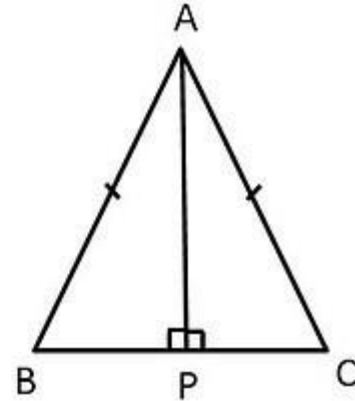
$$\therefore \angle FBC = \angle ECB \quad (\text{CPCT})$$

$$\text{So, } \angle ABC = \angle ACB$$

$$AB = AC \quad (\text{Sides opposite to equal angles is equal})$$

So, $\triangle ABC$ is an isosceles triangle

ABC is an isosceles triangle with $AB = AC$. Draw $AP \perp BC$ to show that $\angle B = \angle C$.



ABC is an isosceles triangle with $AB = AC$. Draw $AP \perp BC$ to show that $\angle B = \angle C$.

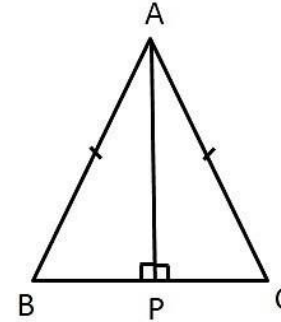
Given:

Since ΔABC is isosceles

$AB = AC$... (1)

Given $AP \perp BC$,

So, $\angle APB = \angle APC = 90^\circ$... (2)



To prove: $\angle B = \angle C$

Proof:

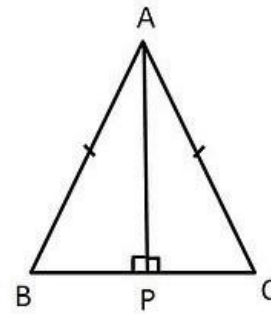
In $\triangle ABP$ and $\triangle ACP$

$$\angle APB = \angle APC = 90^\circ \quad (\text{From (2)})$$

$$AB = AC \quad (\text{From (1)})$$

$$AP = AP \quad (\text{Common})$$

$$\triangle ABP \cong \triangle ACP \quad (\text{RHS congruence rule})$$

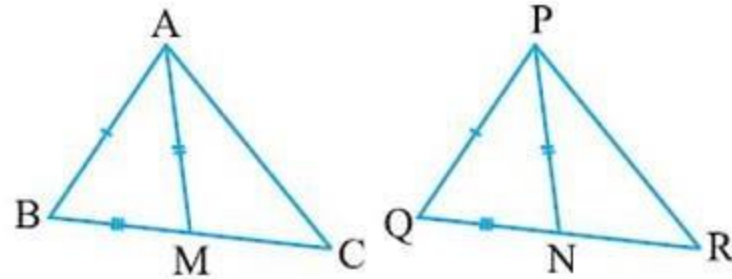


$$\text{So, } \angle B = \angle C \quad (\text{CPCT})$$

Hence proved

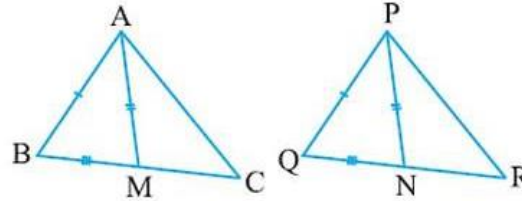
Two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ and QR and median PN of ΔPQR (see figure).Show that :

(ii) $\Delta ABC \cong \Delta PQR$



Two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ and QR and median PN of ΔPQR (see figure).Show that :

(ii) $\Delta ABC \cong \Delta PQR$



From part (i), $\Delta ABM \cong \Delta PQN$

$$\angle B = \angle Q \quad (\text{CPCT}) \quad \dots(1)$$

In ΔABC & ΔPQR

$$AB = PQ \quad (\text{Given})$$

$$\angle B = \angle Q \quad (\text{From (1)})$$

$$BC = QR \quad (\text{Given})$$

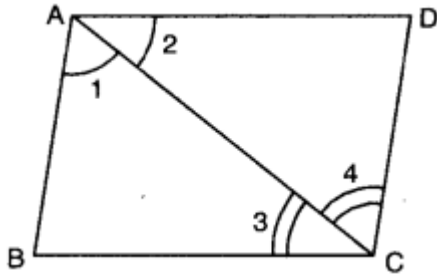
So, $\Delta ABC \cong \Delta PQR$ (SAS congruence rule)

HOMEWORK ASSIGNMENT

Exercise 7.3
Question number 3

AHA

In the given figure, if $\angle 1 = \angle 2$ and $\angle 3 = \angle 4$, then prove that $BC = CD$.
Solution:



THANKING YOU
ODM EDUCATIONAL GROUP