

# **CUBES AND CUBE ROOTS**

## PERIOD 4

**SUBJECT : MATHEMATICS**  
**CHAPTER NUMBER: 4**  
**CHAPTER NAME : CUBES AND CUBE ROOTS**

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**CHANGING YOUR TOMORROW**

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## Previous concept

$$(i) -216 = \sqrt[3]{-216} = \sqrt{-6 \times -6 \times -6} = -6$$

$$(ii) -512 = \sqrt[3]{-512} = \sqrt{-8 \times -8 \times -8} = -8$$

$$(iii) -1331 = \sqrt[3]{-1331} \\ = \sqrt{-11 \times -11 \times -11} = -11$$

$$(iv) -\frac{27}{125} = -\frac{\sqrt{27}}{\sqrt{125}} = -\frac{\sqrt{3 \times 3 \times 3}}{\sqrt{5 \times 5 \times 5}} = -\frac{3}{5}$$

$$(v) \frac{-64}{343} = \frac{\sqrt[3]{-64}}{\sqrt[3]{343}} = \frac{\sqrt[3]{-4 \times -4 \times -4}}{\sqrt[3]{7 \times 7 \times 7}} = \frac{-4}{7}$$

$$(vi) -\frac{512}{343} = -\sqrt[3]{\frac{512}{343}} = -\sqrt[3]{\frac{8 \times 8 \times 8}{7 \times 7 \times 7}} = -\frac{8}{7}$$

# Learning outcome

- Students will be able to know about properties of cubes
- Students will be able to find the cube root of a perfect cube using prime factorization method.
- Students will be able to find the cube root of a negative perfect cube using prime factorization method.

# Recapitulation

1. By what smallest number should 3600 be multiplied, so that the quotient is a perfect cube? Also, find the cube root of the quotient.

**Sol:** Prime factors of 3600 =  $2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 5$

We know that, if a number is to be a perfect cube, then each of its prime factors must occur thrice.

We find that 2 occurs once 3 and 5 occurs twice only.

Hence, the smallest number, by which the given number must be multiplied in order that the product is a perfect cube =  $2 \times 2 \times 3 \times 5 = 60$

Also, product =  $3600 \times 60 = 216000$

Now, arranging into triplets of equal prime factors, we have

$$216000 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{3 \times 3 \times 3} \times \underline{5 \times 5 \times 5}$$

Taking one factor from each triplets, we get

$$\sqrt[3]{216000} = 2 \times 2 \times 3 \times 5 = 60$$

# Evaluation Questions

## Exercise-4(B)

5. Find the smallest number by which 26244 may be divided so that the quotient is a perfect cube.

$$\begin{aligned}\text{Sol: } 26244 &= 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3 \\ &= 3^3 \times 3^3 \times 3^2 \times 2^2\end{aligned}$$

Clearly, 26244 must be divided by  $3^2 \times 2^2 = 9 \times 4 = 36$

7)

$$(iv) -\frac{27}{343} = \frac{3 \times 3 \times 3}{7 \times 7 \times 7} = -\frac{3}{7}$$

$$(v) \frac{729}{-1331} = \frac{(9 \times 9 \times 9)}{-(11 \times 11 \times 11)} = -\frac{9}{11}$$

$$(vi) 250.047 = \frac{250047}{1000}$$

$$\begin{array}{r|l} 3 & 250047 \\ \hline 3 & 83349 \\ \hline 3 & 27783 \\ \hline 3 & 9261 \\ \hline 3 & 3087 \\ \hline 3 & 1029 \\ \hline 7 & 343 \\ \hline 7 & 49 \\ \hline 7 & 7 \\ \hline & 1 \end{array}$$

$$= \frac{(3 \times 3 \times 3) \times (3 \times 3 \times 3) \times (7 \times 7 \times 7)}{(10 \times 10 \times 10)}$$

$$= \frac{3 \times 3 \times 7}{10} = \frac{63}{10} = 6.3$$

# Home assignment

## Exercise 4(B)

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1. Using prime factorisation, find the cube root of 5832.
2. If the surface area of a cube is  $486 \text{ cm}^2$ , find its volume.

**THANKING YOU**  
**ODM EDUCATIONAL GROUP**

