

RATIONAL NUMBERS

PERIOD 5

SUBJECT : MATHEMATICS
CHAPTER NUMBER: 1
CHAPTER NAME : RATIONAL NUMBERS

CHANGING YOUR TOMORROW

Learning outcome

- Students will be able to **multiply** rational numbers
- Students will be able to understand and apply properties of multiplication.

Previous Knowledge:

- 1) $\frac{1}{6}$ of the class students are above average, $\frac{1}{4}$ are average and rests are below average. If there are 48 students in all, how many students are below average in the class?
- 2) One fruit salad recipe requires $\frac{1}{2}$ cup of sugar. Another recipe for the same fruit salad requires 2 tablespoons of sugar. If 1 tablespoon is 1 equivalent to $\frac{1}{16}$ cup, how much more sugar does the first recipe require?

Properties of multiplication of Rational Numbers

Closure property of multiplication :

Closure property of multiplication of rational numbers:

The product of two rational numbers is always a rational number.

If a/b and c/d are any two rational numbers then $(a/b \times c/d)$ is also a rational number.

Consider the rational numbers $-3/7$ and $5/14$. Then

$(-3/7 \times 5/14) = \{(-3) \times 5\}/(7 \times 14) = -15/98$, is a rational number .

Commutative property of multiplication

Two rational numbers can be multiplied in any order.

Thus, for any rational numbers a/b and c/d , we have:

$$(a/b \times c/d) = (c/d \times a/b)$$

Let us consider the rational numbers $-2/5$ and $6/7$. Then,

$$\{(-2)/5 \times 6/7\} = \{(-2) \times 6\}/(5 \times 7) = -12/35 \text{ and } (6/7 \times -2/5)$$

$$= \{6 \times (-2)\}/(7 \times 5) = -12/35$$

$$\text{Therefore, } (-2/5 \times 6/7) = (6/7 \times (-2)/5)$$

Associative property of multiplication:

While multiplying three or more rational numbers, they can be grouped in any order.

Thus, for any rationals a/b , c/d , and e/f we have:

$$(a/b \times c/d) \times e/f = a/b \times (c/d \times e/f)$$

Consider the rationals $-5/2$, $-7/4$ and $1/3$ we have

$$\begin{aligned} (-5/2 \times (-7)/4) \times 1/3 &= \{(-5) \times (-7)\}/(2 \times 4) \times 1/3 = (35/8 \times 1/3) \\ &= (35 \times 1)/(8 \times 3) = 35/24 \end{aligned}$$

$$\begin{aligned}(-5)/2 \times (-7/4 \times 1/3) &= -5/2 \times \{(-7) \times 1\}/(4 \times 3) = (-5/2 \times -7/12) \\ &= \{(-5) \times (-7)\}/(2 \times 12) = 35/24\end{aligned}$$

Therefore, $(-5/2 \times -7/4) \times 1/3 = (-5/2) \times (-7/4 \times 1/3)$

Existence of multiplicative identity

For any rational number a/b , we have $(a/b \times 1) = (1 \times a/b) = a/b$

1 is called the multiplicative identity for rationals.

Consider the rational $-9/13$. Then, we have

$$(-9/13 \times 1) = (-9/13 \times 1/1) = \{(-9) \times 1\}/(13 \times 1) = -9/13$$

$$\text{and } (1 \times (-9)/13) = (1/1 \times (-9)/13) = \{1 \times (-9)\}/(1 \times 13) = -9/13$$

$$\text{Therefore, } \{(-9)/13 \times 1\} = \{1 \times (-9)/13\} = (-9)/13$$

Existence of multiplicative inverse property:

Every nonzero rational number a/b has its multiplicative inverse b/a .

$$\text{Thus, } (a/b \times b/a) = (b/a \times a/b) = 1$$

b/a is called the **reciprocal** of a/b .

Clearly, zero has no reciprocal.

Reciprocal of 1 is 1 and the reciprocal of (-1) is (-1)

Reciprocal of $-8/9$ is $-9/8$, since $(-8/9 \times -9/8) = (-9/8 \times -8/9) = 1$.

Distributive property of multiplication over addition:

For any three rational numbers a/b , c/d and e/f , we have :

$$a/b \times (c/d + e/f) = (a/b \times c/d) + (a/b \times e/f)$$

For example:

Consider the rational numbers $-3/4$, $2/3$ and $-5/6$ we have

$$(-3)/4 \times \{2/3 + (-5)/6\} = (-3/4) \times \{4 + -5/6\} = (-3/4) \times (-1)/6$$

$$= \{(-3) \times (-1)\}/(4 \times 6) = 3/24 = 1/8$$

$$\text{again, } (-3/4) \times 2/3 = \{(-3) \times 2\}/(4 \times 3) = -6/12 = -1/2$$

$$\text{again, } (-3/4) \times 2/3 = \{(-3) \times 2\}/(4 \times 3) = -6/12 = -1/2$$

Multiplication of Rational Numbers, Properties of multiplication

<https://www.youtube.com/watch?v=JMYr1iAnH0w> (7:28)

Exercise- 1(C)

$$1.(v) -16/5 \times 20/8$$
$$= -8$$

$$2.(v) -7/10 \times -8/15$$
$$= 28/75$$

$$3. (i) (2/-3 \times 5/4) + (5/9 \times 3/-10)$$
$$= 5/-6 + 1/-6$$
$$= -5/6 - 1/6$$
$$= -5 - 1/6$$
$$= -6/6$$
$$= -1$$

$$\begin{aligned} 4. (v) \quad & -6/-7 \times 1 \\ & = 6/7 \times 1 \\ & = 6/7 \end{aligned}$$

5.(i) rational numbers $-1/5$ **and** $2/9$.Then,

$$\begin{aligned} \{(-1)/5 \times 2/9\} &= \{(-1) \times 2\}/(5 \times 9) = -2/45 \text{ and } (2/9 \times -1/5) \\ &= \{2 \times (-1)\}/(9 \times 5) = -2/45 \end{aligned}$$

Therefore, $(-1/5 \times 2/9) = (2/9 \times (-1)/5)$

6.(v) Multiplicative inverse of $-8/-7 = 7/8$

Home assignment

Exercise 1(C) - 7 to 10

1. Can you find a rational number whose multiplicative inverse is -1 ?
2. Find the two rational numbers whose absolute value is 15
3. From a rope 40 m long, pieces of equal size are cut. If the length of one piece is $\frac{10}{3}$ m, find the number of such pieces.
4. Find the product of additive inverse and multiplicative inverse of $-\frac{1}{3}$.

THANKING YOU
ODM EDUCATIONAL GROUP

