

CHAPTER-10**SETS****STUDY NOTES**What is a Set?

- A set is a well-defined collection of **distinct objects**.

Example: $A = \{1, 2, 3, 4, 5\}$

What is an element of a Set?

- The **objects in a set** are called its elements.
 - So in case of the above Set A, the elements would be 1, 2, 3, 4, and 5. We can say, $1 \in A$, $2 \in A$ etc.
- Usually we denote Sets by CAPITAL LETTERS like **A, B, C**, etc. while their elements are denoted in small letters like **x, y, z** etc.
- If x is an element of A, then we say x belongs to A and we represent it as $x \in A$.

- If x is not an element of A , then we say that x does not belong to A and we represent it as

$$x \notin A$$

How to describe a Set?

- **Roster Method or Tabular Form**
 - In this form, we just list the elements.
 - Example $A = \{1, 2, 3, 4\}$ or $B = \{a, b, c, d, e\}$
- **Set- Builder Form or Rule Method or Description Method**
 - In this method, we list the properties satisfied by all elements of the set
 - Example $A = \{x : x \in \mathbb{N}, x < 5\}$

Some examples of Roster Form vs Set-builder Form

1	{1, 2, 3, 4, 5}	$\{x \mid x \in \mathbb{N}, x < 6\}$
2	{2, 4, 6, 8, 10}	$\{x \mid x = 2n, n \in \mathbb{N}, 1 \leq n \leq 5\}$
3	{1, 4, 9, 16, 25, 36}	$\{x \mid x = n^2, n \in \mathbb{N}, 1 \leq n \leq 6\}$

Sets of Numbers

1. Natural Numbers (N)

$$\mathbb{N} = \{1, 2, 3, 4, 5, 6, 7, \dots\}$$

2. Integers (Z)

$$\mathbb{Z} = \{\dots, -3, -2, -1, 0, 1, 2, 3, 4, \dots\}$$

3. Whole Numbers (W)

$$\mathbb{W} = \{0, 1, 2, 3, 4, 5, 6, \dots\}$$

4. Rational Numbers (Q)

$$- \quad \mathbb{Q} = \left\{ \frac{p}{q} : p \in \mathbb{Z}, q \in \mathbb{Z}, q \neq 0 \right\}$$

Finite Sets & Infinite Sets

❓ **Finite Set:** A set where the process of counting the elements of the set would surely come to an end is called finite set

- Example: All natural numbers less than 50
- All factors of the number 36

❓ **Infinite Set:** A set that consists of uncountable number of distinct elements is called infinite set.

- Example: Set containing all natural numbers
- $\{x \mid x \in \mathbb{N}, x > 100\}$

Cardinal number of Finite Set

- The **number of distinct elements** contained in a finite set A is called the cardinal number of A and is denoted by $n(A)$

- Example $A = \{1, 2, 3, 4\}$ then $n(A) = 4$

- $A = \{x \mid x \text{ is a letter in the word 'APPLE'}\}$. Therefore $A = \{A, P, L, E\}$ and $n(A) = 4$

- $A = \{x \mid x \text{ is the factor of } 36\}$, Therefore $A = \{1, 2, 3, 4, 6, 9, 12, 18, 36\}$ and $n(A) = 9$

Empty Set

- A set containing no elements at all is called an empty set or a **null set** or **void set**.
- It is denoted by φ (phai)
- In roster form you write $\varphi = \{ \}$
- Also $n(\varphi) = 0$
 - Examples: $\{x \mid x \in \mathbb{N}, 3 < x < 4\} = \varphi$
 - $\{x \mid x \text{ is an even prime number, } x > 5\} = \varphi$

Non Empty Set

- A set which has **at least one element** is called a non-empty set
 - Example: $A = \{1, 2, 3\}$ or $B = \{1\}$

Singleton Set

- A set containing **exactly one element** is called a singleton set
 - Example: $A = \{a\}$ or $B = \{1\}$

Equal Sets

Two set A and B are said to be equal sets and written as $A = B$ if **every element of A is in B and every element of B is in A.**

- Example $A = \{1, 2, 3, 4\}$ and $B = \{4, 2, 3, 1\}$
 - It is not about the number of elements. It is the elements themselves.
 - If the sets are not equal, then we write as $A \neq B$

Equivalent Sets

- Two finite sets A and B are said to be equivalent, written as $A \leftrightarrow B$, if $n(A) = n(B)$, that is they have the same number of elements.
 - Example: $A = \{a, e, i, o, u\}$ and $B = \{1, 2, 3, 4, 5\}$,
Therefore $n(A) = 5$ and $n(B) = 5$ therefore $A \leftrightarrow B$

