

FUNDAMENTAL OPERATIONS

SUBJECT : MATHEMATICS

CHAPTER NUMBER:19

CHAPTER NAME :FUNDAMENTAL OPERATIONS

SUBTOPIC : Division of a Monomial by a Monomial, and Polynomial by a Monomial.

PERIOD NO: 5 CHANGING YOUR TOMORROW

Learning outcomes

- Students will be able to divide monomial by monomial .
- Students will be able to binomial by monomial

PREVIOUS KNOWLEDGE TEST

1. Find the product of:

(i) $a + b - c$ and $2a - 3b$

(ii) $5x - 6y - 7z$ and $2x + 3y$

(iii) $5x - 6y - 7z$ and $2x + 3y + z$

Negative numbers and Integers

- Students will Learn division of monomials and polynomials with the help of a video .
- <https://www.youtube.com/watch?v=hJ9na3B1bVo>(7.24)

Division in Algebra

$$\frac{6a^2b}{-2ab^2} = \frac{-3a}{b}$$

$$\frac{6 * a * a * b}{-2 * a * b^2}$$

For example

$$\frac{8x - 2x^2}{2x}$$

$$= \frac{8x}{2x} - \frac{2x^2}{2x}$$

$$= \frac{8}{2} \frac{x}{x} - \frac{2}{2} \frac{x^2}{x}$$

$$= 4$$

Division of polynomial by monomial means dividing the polynomials which is written as numerator by a monomial which is written as denominator to find their quotient.

For example: $4a^3 - 10a^2 + 5a \div 2a$

Now the polynomials ($4a^3 - 10a^2 + 5a$) is written as numerator and the monomial ($2a$) is written as denominator.

Therefore, we get $(4a^3 - 10a^2 + 5a) / 2a$

Now we observe that there are three terms in the polynomial so, each term of the polynomial (numerator) is separately divided by the same monomial (denominator).

$$4a^3/2a - 10a^2/2a + 5a/2a = 4a^3/2a - 10a^2/2a + 5a/2a$$

Note:

The process is exactly converse of finding the L.C.M. of fractions and reducing the expression into a single fraction.

Now we will cancel out the common factor from both numerator and denominator to simplify.

$$= 4a^2 - 5a + 5/2$$

Evaluation Question EX-19 D

1. Divide:

(i) 3a by a

(ii) 15x by 3x

(iii) 16m by 4

(iv) $20x^2$ by $5x$

(v) $30p^2$ by $10p^2$

Solution:

(i) 3a by a

$$3a \div a$$

This can be written as, $3a / a = (3 \times a) / a = 3$

$$\text{Hence, } 3a \div a = 3$$

Evaluation Question EX-19 D

Solution: (ii) $15x$ by $3x$

$$15x \div 3x$$

$$15x / 3x = (15 \times x) / (3 \times x)$$

This can be written as,

$$= (3 \times 5 \times x) / (3 \times x) = 5$$

Hence, $15x \div 3x = 5$

(iii) $16m$ by 4

$$16m \div 4$$

$$16m / 4 = (16 \times m) / 4$$

This can be written as, $= (4 \times 4 \times m) / 4$

$$= 4m$$

Evaluation Question EX-19 D

Solution: (iv) $20x^2$ by $5x$

$$20x^2 \div 5x = 20x^2 / 5x = (20 \times x^2) / (5 \times x)$$

This can be written as,

$$= (4 \times 5 \times x^{2-1}) / 5 = 4 \times x$$

$$= 4x$$

Hence, $20x^2 \div 5x = 4x$

(v) $30p^2$ by $10p^2$

$$30p^2 \div 10p^2 = (30 \times p^2) / (10 \times p^2)$$

This can be written as, $(3 \times 10 \times p^{2-2}) / 10$

$$= 3 \times p^0 = 3 \times 1 = 3$$

Hence, $30p^2 \div 10p^2 = 3$

Evaluation Question EX-19 D

2. Simplify:

(i) $2x^5 \div x^2$

(ii) $6a^8 \div 3a^3$

(iii) $20xy \div -5xy$

(iv) $-24a^2b^2c^2 \div 6ab$

(v) $-5x^2y \div xy^2$

Solution: (i) $2x^5 \div x^2$

$$= (2 \times x^5) / x^2 = 2 \times x^{5-2}$$

$$= 2 \times x^3$$

$$= 2x^3$$

Hence, $2x^5 \div x^2 = 2x^3$

Evaluation Question EX-19 D

Solution: (ii) $6a^8 \div 3a^3$

$$= (6 \times a^8) / (3 \times a^3)$$

This can be written as,

$$= (2 \times 3 \times a^{8-3}) / 3$$

$$= 2 \times a^5 = 2a^5$$

Hence, $6a^8 \div 3a^3 = 2a^5$

(iii) $20xy \div -5xy$

$$= (20 \times x \times y) / (-5 \times x \times y)$$

This can be written as, $(4 \times 5) / -5$

$$= -4$$

Hence, $20xy \div -5xy = -4$

Evaluation Question EX-19 D

Solution: (iv) $-24a^2b^2c^2 \div 6ab$

$$= (-24 \times a^2 \times b^2 \times c^2) / (6 \times a \times b)$$

This can be written as,

$$= (-4 \times 6 \times a^{2-1} \times b^{2-1} \times c^2) / 6$$

$$= -4 \times a \times b \times c^2 = -4abc^2$$

Hence, $-24a^2b^2c^2 \div 6ab = -4abc^2$

(v) $-5x^2y \div xy^2$

$$= (-5 \times x^2 \times y) / (x \times y^2)$$

This can be written as, $(-5 \times x^{2-1}) / y^{2-1}$

$$= (-5 \times x) / y = -5x / y$$

Hence, $-5x^2y \div xy^2 = -5x / y$

Evaluation Question EX-19 D

3. Divide:

(i) $(- 3m / 4)$ by $2m$

(ii) $- 15p^6q^8$ by $- 5p^6q^7$

(iii) $- 21m^5n^7$ by $14m^2n^2$

(iv) $36a^4x^5y^6$ by $4x^2a^3y^2$

(v) $20x^3a^6$ by $5xy$

Solution: (i) $(- 3m / 4)$ by $2m$

$$= - 3m / 4 \div 2m = - 3m / 4 \times 1 / 2m$$

$$= - (3 \times m) / (4 \times 2 \times m)$$

$$= - 3 / 8$$

Hence, $(- 3m / 4) \div 2m = - 3 / 8$

Evaluation Question EX-19 D

Solution: (ii) $-15p^6q^8$ by $-5p^6q^7$

$$-15p^6q^8 \div -5p^6q^7 = (-15 \times p^6 \times q^8) / (-5 \times p^6 \times q^7)$$

This can be written as,

$$= (3 \times 5 \times q^{8-7}) / 5 = 3 \times q$$

$$= 3q$$

Hence, $-15p^6q^8 \div -5p^6q^7 = 3q$

(iii) $-21m^5n^7$ by $14m^2n^2$

$$-21m^5n^7 \div 14m^2n^2 = (-21 \times m^5 \times n^7) / (14 \times m^2 \times n^2)$$

This can be written as, $(-3 \times 7 \times m^{5-2} \times n^{7-2}) / (2 \times 7)$

$$= (-3 \times m^3 \times n^5) / 2 = -3m^3n^5 / 2$$

Hence, $-21m^5n^7 \div 14m^2n^2 = -3m^3n^5 / 2$

Evaluation Question EX-19 D

Solution: (iv) $36a^4x^5y^6$ by $4x^2a^3y^2$

$$36a^4x^5y^6 \div 4x^2a^3y^2 = (36 \times a^4 \times x^5 \times y^6) / (4 \times x^2 \times a^3 \times y^2)$$

This can be written as,

$$= (4 \times 9 \times a^{4-3} \times x^{5-2} \times y^{6-2}) / 4$$

$$= 9 \times a^1 \times x^3 \times y^4 = 9ax^3y^4$$

$$\text{Hence, } 36a^4x^5y^6 \div 4x^2a^3y^2 = 9ax^3y^4$$

(v) $20x^3a^6$ by $5xy$

$$20x^3a^6 \div 5xy = (20 \times x^3 \times a^6) / (5 \times x \times y)$$

This can be written as,

$$= (4 \times 5 \times x^{3-1} \times a^6) / (5 \times y) = (4 \times x^2 \times a^6) / y = 4x^2a^6 / y$$

$$\text{Hence, } 20x^3a^6 \div 5xy = 4x^2a^6 / y$$

Additional Homework

1. Divide:

(i) $-16ab^2c$ by $6abc$

(ii) $25x^2y$ by $-5y^2$

(iii) $8x + 24$ by 4

(iv) $4a^2 - a$ by $-a$

(v) $8m - 16$ by -8

HW
Ex.19 D Q .No 1 to 3

THANKING YOU
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