

# **CIRCLES**

## **PPT-3**

**SUBJECT : MATHEMATICS**  
**CHAPTER NUMBER: 10**  
**CHAPTER NAME : CIRCLES**

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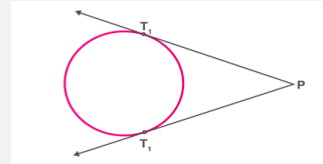
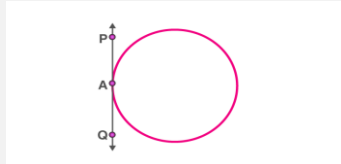
**CHANGING YOUR TOMORROW**

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## PREVIOUS KNOWLEDGE TEST

i) If the point is in an **interior region of the circle**, any line through that point will be a secant. So, **no tangent** can be drawn to a circle which passes through a point that lies inside it.

ii) When a point of tangency lies on the circle, there is **exactly one tangent** to a circle that passes through it.



iii) When the point lies outside of the circle, there are **accurately two tangents** to a circle through it

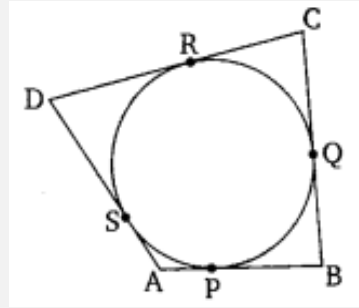
The length of the segment of the tangent from the external point and the point of contact with the circle is called the length of the tangent.

## LEARNING OUTCOME

1. Students will be able to prove that the tangent at any point of a circle is perpendicular to the radius through the point of contact
2. Students will be able to prove that the lengths of tangents drawn from an external point to a circle are equal.
3. Students will be able to apply the knowledge of above theorem in solving questions

Problem solving on Theorem 10.1 & Theorem 10.2  
<https://youtu.be/bHWzFLD0qNc> (11.04)

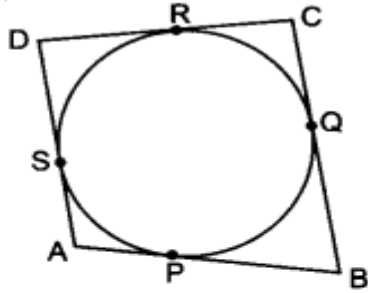
1. Quadrilateral ABCD is drawn to circumscribe a circle . Prove that  $AB + CD = AD + BC$ .



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$$AP = AS \dots(i)$$

[Lengths of tangents from an external point are equal]



$$BP = BQ \dots(ii)$$

$$CR = CQ \dots(iii)$$

$$DR = DS \dots(iv)$$

Adding equations (i), (ii), (iii) and (iv), we get

$$AP + BP + CR + DR = AS + BQ + CQ + DS$$

$$\Rightarrow (AP + BP) + (CR + DR) = (AS + DS) + (BQ + CQ)$$

$$\Rightarrow AB + CD = AD + BC$$

Hence proved.

2. Prove that the parallelogram circumscribing a circle is a rhombus.

## 2. Prove that the parallelogram circumscribing a circle is a rhombus.

**Solution.** *Given.*  $ABCD$  is a quadrilateral touching a circle at  $P, Q, R$  and  $S$ .

*To Prove.*  $AB + CD = AD + BC$ .

**Proof.** The lengths of the two tangents drawn from an external point to a circle are equal. Therefore,

$$AP = AS \quad \dots(i)$$

$$BP = BQ \quad \dots(ii)$$

$$CR = CQ \quad \dots(iii)$$

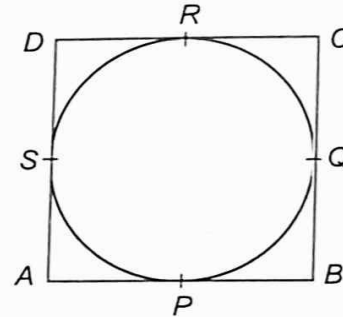
$$DR = DS \quad \dots(iv)$$

On adding (i) to (iv), we get

$$(AP + BP) + (CR + DR) = (AS + DS) + (CQ + BQ)$$

Hence,

$$AB + CD = AD + BC.$$





3. Prove that the angle between the two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line-segment joining the points of contact at the Centre.

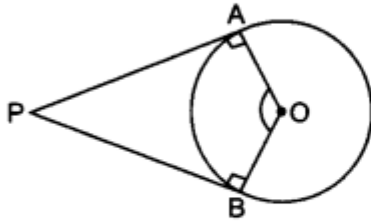
3. Prove that the angle between the two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line-segment joining the points of contact at the Centre.

PA and PB are two tangents, A and B are the points of contact of the tangents.

$OA \perp AP$  and  $OB \perp BP$

$\angle OAP = \angle OBP = 90^\circ$

[Radius and tangent are perpendicular to each other]



p In quadrilateral OAPB

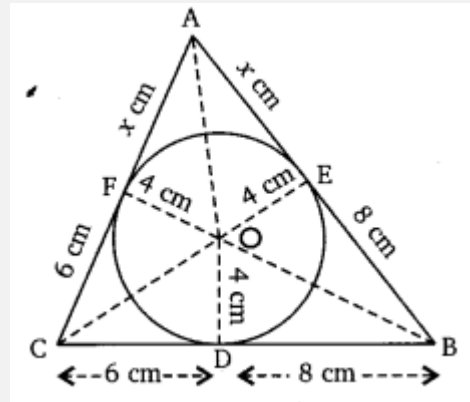
$\angle OAP + \angle OBP + \angle APB + \angle AOB = 360^\circ$

$\Rightarrow 90^\circ + 90^\circ + \angle APB + \angle AOB = 360^\circ$

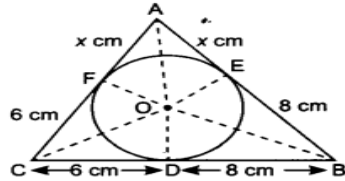
$\angle APB + \angle AOB = 360^\circ - 180^\circ = 180^\circ$

Hence,  $\angle APB$  and  $\angle AOB$  are supplementary angles.

4. A triangle ABC is drawn to circumscribe a circle of radius 4 cm such that the segments BD and DC into which BC is divided by the point of contact D are of lengths 8 cm and 6 cm respectively . Find the sides AB and AC



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$BD = 8 \text{ cm}$  and  $DC = 6 \text{ cm}$

$BE = BD = 8 \text{ cm}$

$CD = CF = 6 \text{ cm}$

Let  $AE = AF = x \text{ cm}$

In  $\triangle ABC$ ,  $a = 6 + 8 = 14 \text{ cm}$

$b = (x + 6) \text{ cm}$

$c = (x + 8) \text{ cm}$

$$s = \frac{a + b + c}{2} = \frac{14 + x + 6 + x + 8}{2} = \frac{2x + 28}{2} = (x + 14) \text{ cm}$$

$$\begin{aligned} \text{ar}(\triangle ABC) &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{(x+14) \times x \times 8 \times 6} = \sqrt{48x \times (x+14)} \text{ cm}^2 \end{aligned} \quad \dots(i)$$

Again,

$$\begin{aligned} \text{ar}(\triangle ABC) &= \text{ar}(\triangle OBC) + \text{ar}(\triangle OCA) + \text{ar}(\triangle OAB) \\ &= \frac{1}{2} \times 4 \times a + \frac{1}{2} \times 4 \times b + \frac{1}{2} \times 4 \times c \\ &= 2a + 2b + 2c = 2(a + b + c) = 2 \times 2(x + 14) \end{aligned} \quad \dots(ii)$$

From (i) and (ii), we get

$$\begin{aligned} \Rightarrow \sqrt{48x(x+14)} &= 4(x+14) & \Rightarrow & 48x(x+14) = 4^2(x+14)^2 \\ \Rightarrow 48x(x+14) &= 16(x+14)^2 & \Rightarrow & 3x(x+14) = (x+14)^2 \\ \Rightarrow 3x &= x+14 & \Rightarrow & 2x = 14 \Rightarrow x = 7 \\ \text{AB} &= x + 8 = 7 + 8 = 15 \text{ cm} \\ \text{AC} &= x + 6 = 7 + 6 = 13 \text{ cm} \end{aligned}$$

5. Prove that opposite sides of a quadrilateral circumscribing a circle subtend supplementary angles at the centre of the circle.

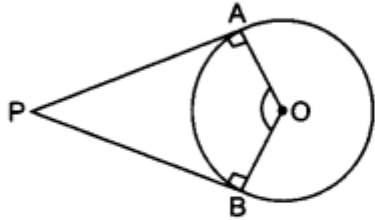
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[Radius and tangent are perpendicular to each other]



p In quadrilateral OAPB

$\angle OAP + \angle OBP + \angle APB + \angle AOB = 360^\circ$

$\Rightarrow 90^\circ + 90^\circ + \angle APB + \angle AOB = 360^\circ$

$\angle APB + \angle AOB = 360^\circ - 180^\circ = 180^\circ$

Hence,  $\angle APB$  and  $\angle AOB$  are supplementary angles.

## HOME ASSIGNMENT Ex. 10.2 Q. No 8 TO Q13.

1. Prove that the angle between the two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line-segment joining the points of contact at the centre.

**THANKING YOU**  
**ODM EDUCATIONAL GROUP**