

CIRCLES

PPT-4

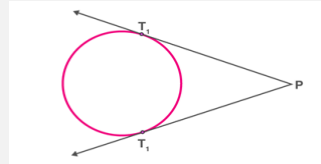
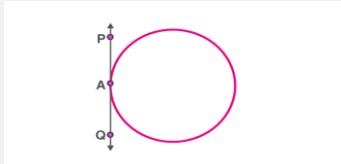
SUBJECT : MATHEMATICS
CHAPTER NUMBER: 10
CHAPTER NAME : CIRCLES

CHANGING YOUR TOMORROW

PREVIOUS KNOWLEDGE TEST

i) If the point is in an **interior region of the circle**, any line through that point will be a secant. So, **no tangent** can be drawn to a circle which passes through a point that lies inside it.

ii) When a point of tangency lies on the circle, there is **exactly one tangent** to a circle that passes through it.



iii) When the point lies outside of the circle, there are **accurately two tangents** to a circle through it

The length of the segment of the tangent from the external point and the point of contact with the circle is called the length of the tangent.

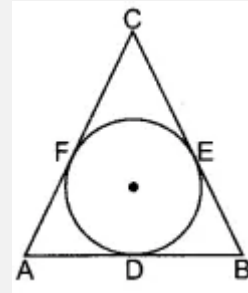
LEARNING OUTCOME

1. Students will be able to prove that the tangent at any point of a circle is perpendicular to the radius through the point of contact
2. Students will be able to prove that the lengths of tangents drawn from an external point to a circle are equal.
3. Students will be able to apply the knowledge of above theorem in solving questions

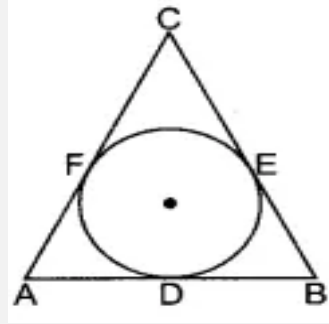
Quick revision on Circles

https://youtu.be/JZ2cEB4_aAA (11.04)

1. A circle is inscribed in a ΔABC , such that it touches the sides AB , BC and CA at points D , E and F respectively. If the lengths of sides AB , BC and CA are 12 cm, 8 cm and 10 cm respectively, find the lengths of AD , BE and CF .



1. A circle is inscribed in a ΔABC , such that it touches the sides AB, BC and CA at points D, E and F respectively. If the lengths of sides AB, BC and CA are 12 cm, 8 cm and 10 cm respectively, find the lengths of AD, BE and CF.



Given, AB = 12 cm, CA = 10 cm, BC = 8 cm

Let $AD = AF = x$ [\because Tangent drawn from external point to circle are equal]

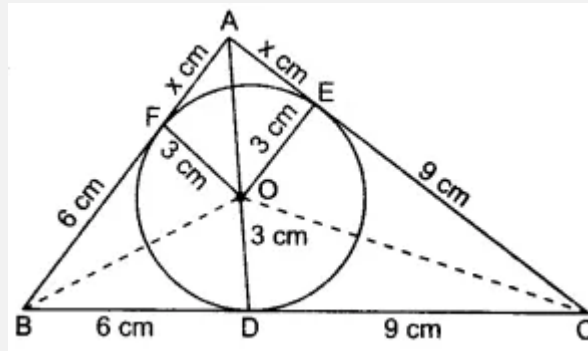
$$\therefore DB = BE = 12 - x \text{ and } CF = CE = 10 - x$$

$$BC = BE + EC \Rightarrow 8 = 12 - x + 10 - x$$

$$\Rightarrow x = 7$$

$\therefore AD = 7$ cm, $BE = 5$ cm and $CF = 3$ cm

2. A triangle ABC is drawn to circumscribe a circle of radius 3 cm, such that the segments BD and DC are respectively of lengths 6 cm and 9 cm. If the area of ΔABC is 54 cm^2 , then find the lengths of sides AB and AC.



2. A triangle ABC is drawn to circumscribe a circle of radius 3 cm, such that the segments BD and DC are respectively of lengths 6 cm and 9 cm. If the area of ΔABC is 54 cm^2 , then find the lengths of sides AB and AC

Let $AF = x \text{ cm}$, $BC = (6 + 9) = 15 \text{ cm}$

$\therefore AF = AE$

[tangents drawn from an external point are equal]

$\therefore AE = x \text{ cm}$

Also $BD = BF = 6 \text{ cm}$

and $CD = CE = 9 \text{ cm}$

$\therefore AB = (x + 6) \text{ cm}$

In ΔABC , $AC = (x + 9) \text{ cm}$

$\text{Area } \Delta ABC = \text{Area } \Delta BOC + \text{Area } \Delta COA + \text{Area } \Delta AOB$

$$\Rightarrow 54 = \frac{1}{2} BC \times OD + \frac{1}{2} AC \times OE + \frac{1}{2} AB \times OF$$

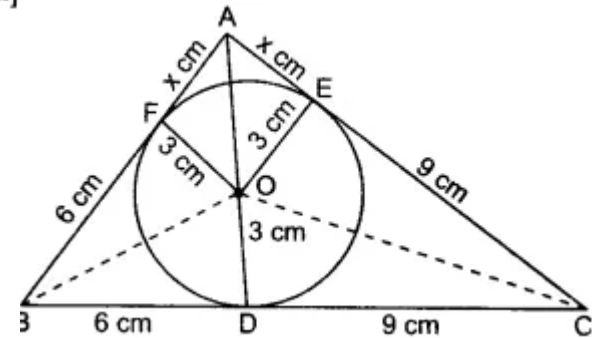
$$\Rightarrow 54 \times 2 = 15 \times 3 + (9 + x) \times 3 + (6 + x) \times 3$$

$$108 = 45 + 18 + 3x + 27 + 3x$$

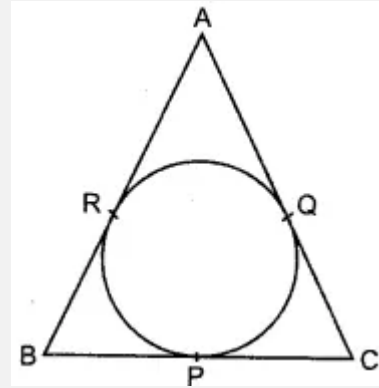
$$6x = 18 \Rightarrow x = 3$$

$$\Rightarrow AB = 6 + x = 6 + 3 = 9 \text{ cm}$$

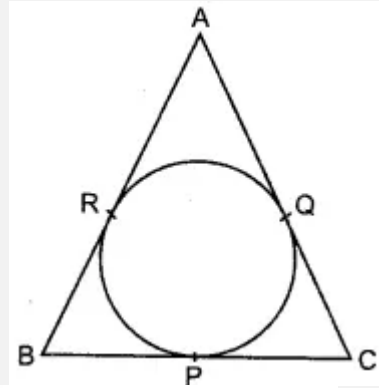
$$AC = 9 + x = 9 + 3 = 12 \text{ cm}$$



3. A circle inscribed in ΔABC , touches its sides BC, CA and AB at the points P, Q and R respectively. If $AB = AC$, then prove that $BP = CP$.



3. A circle inscribed in $\triangle ABC$, touches its sides BC, CA and AB at the points P, Q and R respectively. If $AB = AC$, then prove that $BP = CP$.



$$\begin{aligned} & \therefore AB = AC \\ & AR + BR = AQ + CQ \\ & AR + BR = AR + CQ \\ & \quad [AQ = AR, \text{ equal tangents}] \\ \Rightarrow & BR = CQ \\ \text{Now,} & BR = BP \text{ [Length of equal tangents]} \\ & CQ = CP \\ \Rightarrow & BP = CP \end{aligned}$$

4..Prove that the parallelogram circumscribing a circle is a rhombus.

4..Prove that the parallelogram circumscribing a circle is a rhombus.

Given: ABCD is parallelogram circumscribing a circle.

To prove: ABCD is a rhombus

Proof: We have, $DR = DS$...*(i)*

[Lengths of tangents drawn from an external point to a circle are equal]

Also, $AP = AS$...*(ii)*

$BP = BQ$...*(iii)*

$CR = CQ$...*(iv)*

Adding *(i)*, *(ii)*, *(iii)* and *(iv)*,

$$(DR + CR) + (AP + BP) = (DS + AS) + (BQ + CQ)$$

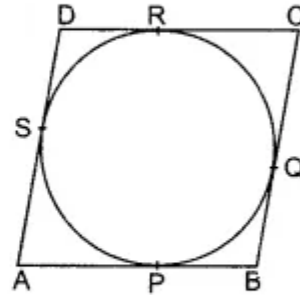
$$\Rightarrow CD + AB = AD + BC$$

$$\Rightarrow 2AB = 2AD \quad [\because \text{In parallelogram, opposite sides are equal} \\ AB = CD \text{ and } AD = BC]$$

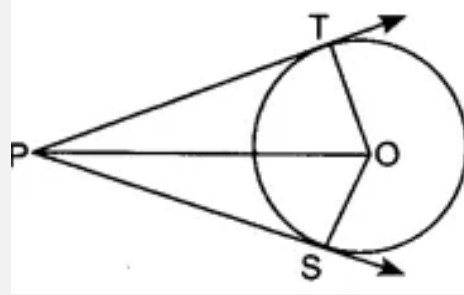
$$\Rightarrow AB = AD$$

$$\therefore AB = AD = BC = CD$$

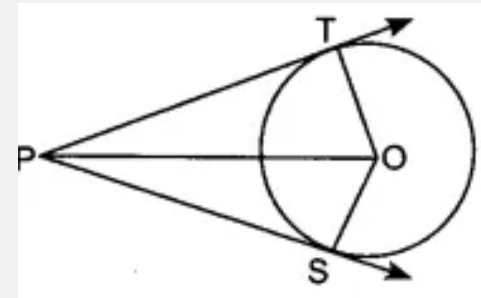
Hence, ABCD is a rhombus as all sides are equal in rhombus.



5. From a point P, two tangents PT and PS are drawn to a circle with centre O such that $\angle SPT = 120^\circ$, Prove that $OP = 2PS$



5. From a point P, two tangents PT and PS are drawn to a circle with centre O such that $\angle SPT = 120^\circ$; Prove that $OP = 2PS$



Let $PT = x = PS$ [\because Tangent drawn from external point to circle are equal]

In $\triangle OTP$ and $\triangle OSP$,
 $\angle SPT = 120^\circ$
 $\angle OTP = \angle OSP$ [\because each equal to 90° , since tangent perpendicular to radius]
 $OT = OS$ [\because Equal radii]
 $OP = OP$ [common]
 $\Rightarrow \triangle OSP \cong \triangle OTP$ [\because By SAS congruence rule]
 $\therefore \angle TPO = \angle SPO$ [\because By CPCT]
 $\Rightarrow \angle TPO = \frac{1}{2} \angle SPT = \frac{1}{2} \times 120 = 60^\circ$
 In $\triangle OTP$,
 $\frac{OP}{x} = \sec 60^\circ$
 $\Rightarrow \frac{OP}{x} = 2 \Rightarrow OP = 2x \Rightarrow OP = 2PS$
 Hence proved.

HOME ASSIGNMENT CH10.

THANKING YOU
ODM EDUCATIONAL GROUP