

# PAIR OF LINEAR EQUATIONS IN TWO VARIABLES

PPT6

**SUBJECT : MATHEMATICS**

**CHAPTER NUMBER: 03**

**CHAPTER NAME : PAIR OF LINEAR EQUATIONS IN TWO VARIABLES**

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## PREVIOUS KNOWLEDGE TEST

### **Substitution method**

If we have a pair of Linear Equations with two variables  $x$  and  $y$ , then we have to follow these steps to solve them with the substitution method-

**Step 1:** We have to choose any one equation and find the value of one variable in terms of other variable i.e.  $y$  in terms of  $x$ .

**Step 2:** Then substitute the calculated value of  $y$  in terms of  $x$  in the other equation.

**Step 3:** Now solve this Linear Equation in terms of  $x$  as it is in one variable only i.e.  $x$ .

**Step 4:** Substitute the calculate value of  $x$  in the given equations and find the value of  $y$ .

## Learning outcome

- Students will be able to find solution of a pair of linear equations algebraically by Substitution method.
- Students will be able to apply it to solve real life situations.

## •**Solution Using Elimination with Two Variables**

- Arrange both equations in standard form, placing like variables and constants one above the other.
- Choose a variable to eliminate, and with a proper choice of multiplication, arrange so that the coefficients of that variable are opposites of one another.
- Add the equations, leaving one equation with one variable
- Solve for the remaining variable.
- Substitute the value found in Step 4 into any equation involving both variables and solve for the other variable.
- Check the solution in both original equations

Discussion on solving a pair of linear equations using Elimination method.

<https://youtu.be/Dm1rrr6ROVU>

Solve the following pair of linear equations by the elimination method and the substitution method :  $3x - 5y - 4 = 0$  and  $9x = 2y + 7$

(iii) By Elimination Method:

Equations are

$$3x - 5y = 4 \quad \dots(i)$$

and  $9x - 2y = 7 \quad \dots(ii)$

Multiplying equation (i) by 3 and subtracting from equation (ii),

$$\begin{array}{r} 9x - 2y = 7 \\ 9x - 15y = 12 \\ \hline - \quad + \quad - \\ \hline 13y = -5 \end{array}$$

$$\Rightarrow \boxed{y = \frac{-5}{13}}$$

Putting this value of  $y$  in equation (i), we get

$$3x - 5\left(\frac{-5}{13}\right) = 4 \Rightarrow 3x + \frac{25}{13} = 4$$

$$\Rightarrow 3x = 4 - \frac{25}{13} = \frac{52 - 25}{13}$$

$$\Rightarrow 3x = \frac{27}{13} \Rightarrow \boxed{x = \frac{9}{13}}$$

By Substitution Method:

We have  $3x - 5y = 4 \quad \dots(i)$

and  $9x - 2y = 7 \quad \dots(ii)$

From equation (i),  $x = \frac{4 + 5y}{3}$

Putting this value in equation (ii), we get

$$9\left[\frac{4 + 5y}{3}\right] - 2y = 7 \Rightarrow 3[4 + 5y] - 2y = 7$$

$$\Rightarrow 12 + 15y - 2y = 7 \Rightarrow 12 + 13y = 7$$

$$\Rightarrow 13y = -5 \Rightarrow \boxed{y = \frac{-5}{13}}$$

Putting this value of  $y$  in equation (ii), we get

$$9x - 2\left(\frac{-5}{13}\right) = 7 \Rightarrow 9x + \frac{10}{13} = 7$$

$$9x = 7 - \frac{10}{13}$$

$$\Rightarrow 9x = \frac{81}{13} \Rightarrow \boxed{x = \frac{9}{13}}$$

**Solve for  $x$  and  $y$  by the method of elimination:**  
 $4x - 3y = 1$ ;  $5x - 7y = -2$

**Sol.** Given equations are

$$4x - 3y = 1 \quad \dots(i)$$

$$5x - 7y = -2 \quad \dots(ii)$$

For making coefficient of  $y$  equal in both the equations multiplying equation (i) with 7, we get

$$7 \times (4x - 3y) = 7 \times 1$$

$$\Rightarrow 28x - 21y = 7 \quad \dots(iii)$$

Multiplying equation (ii) with 3, we get

$$3 \times (5x - 7y) = 3 \times -2$$

$$\Rightarrow 15x - 21y = -6 \quad \dots(iv)$$

Subtracting equation (iv) from (iii), we get

$$\begin{array}{r} 28x - 21y = 7 \\ 15x - 21y = -6 \\ - \quad + \quad + \\ \hline 13x = 13 \end{array}$$

$$\Rightarrow x = 1$$

when  $x = 1$ , equation (i) becomes

$$4 \times 1 - 3y = 1$$

$$\Rightarrow -3y = -3 \Rightarrow y = 1$$

$$\therefore x = 1, y = 1$$

**Solve the following pair of linear equations for  $x$  and  $y$ :**

$$2(ax - by) + (a + 4b) = 0; 2(bx + ay) + (b - 4a) = 0$$

**Sol.** Consider equations:

$$2(ax - by) + (a + 4b) = 0$$

and  $2(bx + ay) + (b - 4a) = 0$

$$\Rightarrow 2ax - 2by = -a - 4b \quad \dots(i)$$

and  $2bx + 2ay = 4a - b \quad \dots(ii)$

Multiply (i) by  $a$  and (ii) by  $b$  and adding, we get

$$\begin{aligned} 2(a^2 + b^2)x &= (-a - 4b)a + b(4a - b) \\ &= -a^2 - 4ab + 4ab - b^2 \\ &= -(a^2 + b^2) \end{aligned}$$

$$\Rightarrow x = -\frac{1}{2}$$

Substituting in (i), we get

$$-a - 2by = -a - 4b$$

$$\Rightarrow -2by = -4b \Rightarrow y = 2$$

$\therefore$  solution is  $x = -\frac{1}{2}$  and  $y = 2$ .



## Home assignment

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- **Ex. 3.34Q. 1 & AHA**
  1. Solve the system of equation  $2x + y = -4$  and  $5x - 3y = 1$  by the method of elimination.
  2. Solve the system of equation  $2x + 3y = 11$ ,  $x + 2y = 7$  by the method of elimination..

**THANKING YOU**  
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