

ARITHMETIC PROGRESSOINS INTRODUCTION

SUBJECT : MATHEMATICS CHAPTER NUMBER: 05 CHAPTER NAME : ARITHMETIC PROGRESSIONS

CHANGING YOUR TOMORROW

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LEARNING OUTCOME



1. Students will be able to know AP as list of numbers in which successive term is obtained by adding a fixed number to previous term.

- 2.Students will be able to observe geometric patterns and know the concept of AP
- 3.Students will be able to identify situations in daily life where the AP is observed.
- 4.Students will be able to identify the first term & common difference.
- 5.Students will be able to calculate the required term.



Introduction to AP ; https://youtu.be/dv3lcYhxZEM (9.53)



- An arrangement of numbers in a definite order according to some rule is called a Sequence.
- In other words, a pattern of numbers in which succeeding terms are obtained from the preceding term by adding/subtracting a fixed number or by multiplying with/dividing by a fixed number, is called sequence or list of numbers.
 e.g. 1,2,3,4,5
- An **arithmetic progression** is a list of numbers in which each term is obtained by adding afixed number to the preceding term except the first term.
- This fixed number is called the common difference of the AP. It can be positive, negative or zero.
- Let us denote the first term of an AP by a₁, second term by a₂, ..., nth term by a a_n and the common difference by d. Then the AP becomes a₁, a₂, a₃, ..., a_n So, a₂ -a₁= a₃ a₂ = ... = a_n a_{n-1} = d.
- The general form of an arithmetic progression is given by *a*, *a* + *d*, *a* + 2*d*, *a* + 3*d*, . . .where *a* is the first term and *d* the common difference.



- : .In the following situation, does the list of numbers involved make an arithmetic progression, and why?
- progression, and why?
 (i) The taxi fare after each km when the fare is `15 for the first km and `8 for each additional km.
- (ii) The amount of air present in a cylinder when a vacuum pump removes 1/4 of the air remaining in the cylinder at a time.

:In the following situation, does the list of numbers involved make an arithmetic progression, and why?

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(i) Given, $a_1 = ₹ 15$, $a_2 = ₹ 15 + ₹ 8 = ₹ 23$, *a*₃ = ₹ 23 + ₹ 8 = ₹ 31 ∴ List of fares is ₹ 15, ₹ 23, ₹ 31 Now, $a_2 - a_1 = \mathbf{E} 23 - \mathbf{E} 15 = \mathbf{E} 8$ $a_3 - a_2 = ₹ 31 - ₹ 23 = ₹ 8$ Here, $a_2 - a_1 = a_2 - a_2$ Thus, the list forms an AP. (*ii*) Let $a_1 = x; \ a_2 = x - \frac{1}{4}x = \frac{3}{4}x;$ $a_{3} = \frac{3}{4}x - \frac{1}{4}(\frac{3}{4}x)$ $=\frac{3}{4}x-\frac{3}{16}x=\frac{9}{16}x$ The list of numbers is $x, \frac{3}{4}x, \frac{9}{16}x$ $a_2 - a_1 = \frac{3}{4}x - x = -\frac{1}{4}x;$ $a_3 - a_2 = \frac{9}{16}x - \frac{3}{4}x = -\frac{3x}{16}$ $a_{2} - a_{1} \neq a_{3} - a_{2}$ Here, ... It is not an AP.





Which of the following list of numbers form an AP? If they form an AP, write the next two terms : (i) 2, 4, 8, 16, . . . (ii) 2, 5/2, 3, 7/2,



Which of the following list of numbers form an AP? If they form an AP, write the next two terms :

(i) 2, 4, 8, 16, . . . (ii) 2, 5/2, 3, 7/2,

.

Here,

$$a_2 - a_1 = 4 - 2 = 2$$
; $a_3 - a_2 = 8 - 4 = 4$
 \Rightarrow $a_2 - a_1 \neq a_3 - a_2$

Hence, the given list of numbers does not form an AP.

(*ii*) 2,
$$\frac{5}{2}$$
, 3, $\frac{7}{2}$
Here, $a_2 - a_1 = \frac{5}{2} - 2 = \frac{5 - 4}{2} = \frac{1}{2}$; $a_3 - a_2 = 3 - \frac{5}{2} = \frac{6 - 5}{2} = \frac{1}{2}$; $a_4 - a_3 = \frac{7}{2} - 3 = \frac{7 - 6}{2} = \frac{1}{2}$
 $\Rightarrow \quad a_2 - a_1 = a_3 - a_2 = a_4 - a_3$

 $a_{k+1} - a_k$ is same in each case ⇒ Hence, the given list of numbers forms an AP with common difference, $d = \frac{1}{2}$ The next three terms are :

$$a_5 = a_4 + d = \frac{7}{2} + \frac{1}{2} = 4$$
, $a_6 = a_5 + d = 4 + \frac{1}{2} = \frac{9}{2}$, $a_7 = a_6 + d = \frac{9}{2} + \frac{1}{2} = 5$.



Write first four terms of the AP, when the first term a and the common difference d are given as follows: (i) a = 10, d = 10(ii) a = -2, d = 0(iii) a = 4, d = -3,



Write first four terms of the AP, when the first term a and the common difference d are given as follows:

(i) a = 10, d = 10(ii) a = -2, d = 0(iii) a = 4, d = -3

(i) Given, a = 10, d = 10 $a_1 = 10, a_2 = 10 + 10 = 20$ $a_3 = 20 + 10 = 30;$ $a_4 = 30 + 10 = 40$

Thus, the first four terms of the AP are 10, 20, 30 and 40 respectively.

(*ii*) Given, a = -2, d = 0The first four terms of the AP are -2, -2, -2 and -2. (*iii*) $a_1 = 4, d = -3$ and $a_2 = 4 + d = 4 - 3 = 1$ $a_3 = 1 + d = 1 - 3 = -2$ and $a_4 = -2 + d = -2 - 3 = -5$ \therefore The first four terms are 4, 1, -2 and -5.



Which of the following list of numbers form an AP? If they form an AP, write the next two terms : (i)-10,-6,-2,2,.....

(ii) $\sqrt{2}$, $\sqrt{8}$, $\sqrt{18}$, $\sqrt{32}$, ...

4.Which of the following list of numbers form an AP? If they form an AP, write the next two terms :

(iv)-10,-6,-2,2,..... (viii) $\sqrt{2}$, $\sqrt{8}$, $\sqrt{18}$, $\sqrt{32}$, ... (iv) -10, -6, -2, 2, ... $a_2 - a_1 = -6 - (-10) = 4$ and $a_3 - a_2 = -2 - (-6) = 4$ $a_{2} - a_{2} = a_{2} - a_{1}$... The given sequence is an AP. Here, $a_1 = a = -10$, d = 4:. $a_5 = 2 + 4 = 6$; $a_6 = 6 + 4 = 10$; $a_7 = 10 + 4 = 14$ $\sqrt{2}, \sqrt{8}, \sqrt{18}, \sqrt{32}, \dots$ Here, $a_2 - a_1 = \sqrt{8} - \sqrt{2}$ $= 2\sqrt{2} - \sqrt{2} = \sqrt{2}$ $a_3 - a_2 = \sqrt{18} - \sqrt{8}$ and $= 3\sqrt{2} - 2\sqrt{2} = \sqrt{2}$

 $a_3 - a_2 = a_2 - a_1$

: The given sequence is an AP.

Next three terms are

$$a_{5} = \sqrt{32} + d = \sqrt{16 \times 2} + d$$

= $4\sqrt{2} + \sqrt{2} = 5\sqrt{2} = \sqrt{50}$
 $a_{6} = 5\sqrt{2} + \sqrt{2} = 6\sqrt{2} = \sqrt{72}$
 $a_{7} = 6\sqrt{2} + \sqrt{2} = 7\sqrt{2} = \sqrt{98}$

and





HOME ASSIGNMENT Ex. 5.1 Q. No 1 to Q4 AHA

• Which of the following are APs? If they form an AP, find the common difference d and write three more terms

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• (i) 2, 4, 8, 16, (ii) – 1.2, – 3.2, – 5.2, – 7.2, . . .



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