

## TRIANGLES PPT-13

## SUBJECT : MATHEMATICS CHAPTER NUMBER: 06 CHAPTER NAME :TRIANGLES

### CHANGING YOUR TOMORROW

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#### PREVIOUS KNOWLEDGE TEST

1. If a perpendicular is drawn from the vertex of the right angle of a right triangle to the hypotenuse then triangles on both sides of the perpendicular are similar to the whole triangle and to each other

2. Pythagoras Theorem ; : In a right triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides.

**3.Converse of Pythagoras** Theorem 6.9 : In a triangle, if square of one side is equal to the sum of the squares of the other two sides, then the angle opposite the first side is a right angle.

4. The ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides.

#### Ratio of areas of two similar triangles is equal to:

- 1. Ratio of the squares of their corresponding sides.
- 2. Ratio of the squares of their corresponding altitudes.
- 3. Ratio of the squares of their corresponding medians.
- 4. Ratio of the squares of their corresponding angle-bisector segments.



## **LEARNING OUTCOME**

1. Students will be able to prove and apply Thales theorem (Basic Proportionality theorem.

2.Students will be able to know relation between the ratio of the areas of two similar triangles and the ratio of their corresponding sides.

3.Students will be able to prove: The ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides

4.Students will be able to solve problems based on ratio of area of similar of triangles.

5.Students will be able to solve problems based on Pythagoras Theorem.6.. Students will be able to solve problems based on converse of Pythagoras Theorem.



1.BL and CM are medians of a triangle ABC right angled at A. Prove that 4 ( $BL^2 + CM^2$ ) = 5  $BC^2$ 



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**Solution.** In right angled  $\triangle BAL$ , we have  $BL^2 = AL^2 + AB^2$ [By Pythagoras Theorem]  $= \left(\frac{1}{2} AC\right)^2 + AB^2 \qquad \qquad \left[\because AL = \frac{1}{2} AC\right]$ М  $4BL^2 = AC^2 + 4AB^2$ ...(1) ⇒ Also, in right angled  $\Delta CAM$ , we have  $CM^2 = AC^2 + AM^2$  [By Pythagoras Theorem]  $CM^2 = AC^2 + \left(\frac{1}{2}AB\right)^2$  $4CM^2 = 4AC^2 + AB^2$ ...(2) ⇒ On adding (1) and (2), we get  $4(BL^{2} + CM^{2}) = 5AC^{2} + 5AB^{2} = 5(AC^{2} + AB^{2})$  $[:: AC^2 + AB^2 = BC^2]$  $4(BC^2 + CM^2) = 5BC^2$ Hence,



2.A ladder is placed against a wall such that its foot is at a distance of 2.5 m from the wall and its top reaches a window 6 m above the ground.



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#### 3. O is any point inside a rectangle ABCD. Prove that $OB^2 + OD^2 = OA^2 + OC^2$

Solution. Through O, draw PQII AB, so that P lies on AD and Q lies on BC. POII AB  $\Rightarrow PQ \perp BC$  and  $PQ \perp AD$ Both *ABQP* and *CDPQ* are rectangles ⇒ D AP = BQ and CQ = DP $\Rightarrow$ [Opposite sides of rectangles] Q Р From right  $\triangle OQB$ ,  $OB^2 = OQ^2 + BQ^2$ From right  $\triangle OPD$ ,  $OD^2 = OP^2 + DP^2$ В  $OB^{2} + OD^{2} = OP^{2} + OQ^{2} + BQ^{2} + DP^{2}$  ...(i) • From right  $\triangle OPA$ ,  $OA^2 = OP^2 + AP^2$ FIGURE 6.179 From right  $\triangle OQC$ ,  $OC^2 = OQ^2 + CQ^2$  $OA^{2} + OC^{2} = OP^{2} + OQ^{2} + AP^{2} + CQ^{2} = OP^{2} + OQ^{2} + BQ^{2} + DP^{2}$ ...(*ii*) .... [AP = BO, CO = DP]From (*i*) and (*ii*), we get :  $OB^2 + OD^2 = OA^2 + OC^2$ .



4. Two isosceles triangles have equal vertical angles and their areas are in the ratio16:25.Find ratio of their corresponding heights



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5. Prove that the ratio of perimeters of two similar triangles is same as the ratio of their corresponding sides





6.The perimeter of two similar triangles ABC & LMN are 60 cm and 48 cm respectively. If LM=8 cm, then what is the length of AB?

**Solution.** As the ratio of the perimeters of two similar  $\Delta s$  is same as the ratio of their orresponding sides,

$$\frac{\text{Perimeter of } \Delta ABC}{\text{Perimeter of } \Delta LMN} = \frac{AB}{LM} \implies \frac{60}{48} = \frac{AB}{8}$$
$$AB = \frac{60}{48} \times 8 = 10 \text{ cm},$$

...



6.The perimeter of two similar triangles ABC & LMN are 60 cm and 48 cm respectively. If LM=8 cm, then what is the length of AB?



7. Two poles of height p and q meters are standing vertically on a level ground, a meter apart. Prove that the height of the point of intersection of the lines joining the top of each pole to the foot of the opposite pole is pq/(p+q).





## HOME ASSIGNMENT CH-6

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