

## EXERCISE 8 (B)

1. Using the common factor method, find the H.C.F. of :

(i) 16 and 35 :- 1

factors of 16 - 1, 2, 4, 8 and 16.

factors of 35 - 1, 5, 7 and 35.

H.C.F. of 16 and 35 is 1

(ii) 25 and 20.

factors of 25 - 1, 5 and 25

factors of 20 - 1, 2, 4, 5, 10 and 20

H.C.F. of 25 and 20 = 5.

(iii) 27 and 75

factors of 27 = 1, 3, 9 and 27

" " 75 = 1, 3, 5, 15, 25 and 75

HCF of 27 and 75 = 3

(iv) 8, 12, 18

factors of 8 = 1, 2, 4 and 8

" " 12 = 1, 2, 3, 4, 6 and 12

" " 18 = 1, 2, 3, 6, 9, and 18

Hcf of 8, 12 and 18 = 2

(v) 24, 36, 45, 60

factors of 24 = 1, 2, 3, 4, 6, 8, 12 and 24

" " 36 = 1, 2, 3, 4, 6, 9, 12, 18 and 36

" " 45 = 1, ~~2~~, 3, 5, 9, 15 and 45

" " 60 = 1, 2, 3, 4, 5, 6, 10, 12, 15, 20, 30 and 60

2. Using the prime factor method, find the ~~prime~~ H.C.F. of:

(i) 5 and 8.

The prime factors of 5 and 8 are as follows:

$$P_5 = 5 \times \boxed{1}$$

$$P_8 = 2 \times 2 \times \boxed{1} \times 2$$

~~The~~ So, the H.C.F. of 5 and 8 is 1.

(ii) 24 and 49.

The prime factors of 24 and 49 are as follows:

$$P_{24} = \boxed{1} \times 2 \times 2 \times 2 \times 3$$

$$P_{49} = \boxed{1} \times 7 \times 7$$

So, the H.C.F. of 24 and 49 is 1.

(iii) 40, 60 and 80

The prime factors of 40, 60, 80 are as follows:

$$P_{40} = \boxed{2} \times \boxed{2} \times 2 \times \boxed{5}$$

$$P_{60} = \boxed{2} \times \boxed{2} \times 3 \times \boxed{5}$$

$$P_{80} = \boxed{2} \times \boxed{2} \times \boxed{2} \times \boxed{5} \times 2$$

So, the HCF of 40, 60, and 80 is ~~8~~ 20.

(v) 30, 60, 90, 105

The prime factors of 30, 60, 90, 105 are as follows.

$$P_{30} = 2 \times 3 \times 5$$

$$P_{60} = 2 \times 2 \times 3 \times 5 \times 2$$

$$P_{90} = 2 \times 3 \times 3 \times 5 \times 3$$

$$P_{105} = 3 \times 5 \times 7$$

So, the prime factors of 30, 60, 90 and 105 are ~~as~~ follows is 5.

Ex: (i) 16 and 24 -

$$\begin{array}{r} 16 \cancel{) 24} \\ \underline{-16} \\ 8 \end{array}$$

$$\begin{array}{r} 8 \cancel{) 16} \\ \underline{-16} \\ 0 \end{array}$$

So, the H.C.F of 24 and 16 = 8.

(ii) 18 and 30

$$\begin{array}{r} \cancel{18) 30} \\ \cancel{18} \\ \cancel{12} \\ \cancel{0} \\ \cancel{120} \end{array} \quad \begin{array}{r} 18) 30 (1 \\ \underline{18} \\ 12) 18 (1 \\ \underline{12} \\ 6) 18 (3 \\ \underline{18} \\ 0 \end{array}$$

So, the H.C.F. of 18 and 30 is 6.

(iii) 7, 14 and 24.

$$\begin{array}{r} 7) 14 (2 \\ \underline{14} \\ 0 \end{array} \quad \begin{array}{r} 7) 24 (3 \\ \underline{21} \\ 3) 24 (8 \\ \underline{24} \\ 0 \end{array}$$

$$\begin{array}{r} 3) 7 (2 \\ \underline{6} \\ 1) 3 (3 \\ \underline{3} \\ 0 \end{array}$$

So, the H.C.F. of 7, 14 and 24 is 1.

(iv) 70, 80, 120 and 150

$$\begin{array}{r|l} 70 & 80 \\ \hline - 70 & \\ \hline 10 & \end{array}$$
$$\begin{array}{r|l} 120 & 150 \\ \hline - 120 & \\ \hline 30 & 120 \\ \hline - 120 & \\ \hline 0 & \end{array}$$
$$\begin{array}{r|l} 10 & 30 \\ \hline - 30 & \\ \hline 0 & \end{array}$$

So, the H.C.F. of 70, 80, 120 and 150 = 10.

(v) 32, 56 and 46.

$$\begin{array}{r|l} 32 & 46 \\ \hline - 32 & \\ \hline 14 & \end{array}$$
$$\begin{array}{r|l} 14 & 32 \\ \hline - 28 & \\ \hline 4 & 14 \\ \hline - 12 & \\ \hline 2 & 4 \\ \hline - 4 & \\ \hline 0 & \end{array}$$
$$\begin{array}{r|l} 32 & 56 \\ \hline - 32 & \\ \hline 24 & 32 \\ \hline - 24 & \\ \hline 8 & 24 \\ \hline - 24 & \\ \hline 0 & \end{array}$$
$$\begin{array}{r|l} 8 & 46 \\ \hline - 40 & \\ \hline 6 & 8 \\ \hline - 6 & \\ \hline 2 & 6 \\ \hline - 6 & \\ \hline 0 & \end{array}$$

So, H.C.F. of 32, 56 and 46 = 2.

5. Find the greatest number that will divide 93, 111 and 129 leaves remainder 3 in

5. 
$$\begin{array}{r|l} 5 & 180, 225, 315 \\ 3 & 36, 45, 63 \\ 3 & 12, 15, 21 \\ & 4, 5, 3 \end{array}$$

HCF = ~~5~~  
 $3 \times 3 = 45$

So, the ~~#~~ greatest number that will divide 180, 225, 315 is  $5 \times 3 \times 3 = 45$ .

6. Prime factors of 45 =  $5 \times 3 \times 3$   
" " 56 =  $2 \times 2 \times 2 \times 7$

Yes, 45 and 56 are co-prime no.s.

7. Prime factors of 15 =  $3 \times 5$   
" " " 16 =  $2 \times 2 \times 2 \times 2$   
" " " 21 =  $3 \times 7$   
" " " 28 =  $2 \times 2 \times 7$

So, all pairs of co-prime numbers are 15 and 16; 15 and 28, 16 and 21.

8. Since there will be a remainder of 3 we have to do  $93 - 3 = 90$ , ~~108~~ and ~~129~~  $3 = 108$  and  $129 - 3 = 126$

$$2 \times 90, 108, 126$$

$$3 \times 45, 54, 63$$

$$3 \times 15, 18, 21$$

$$5, 6, 7$$

$$\text{HCF} = 2 \times 3 \times 3 = 18$$

So, the greatest no. that will divide 93, 111 and 129 leaving a remainder of 3 is ~~33~~ 18.