

Homework - force on moving charge in uniform magnetic and electric field

13.7.20

1
$$\vec{F} = q\vec{v} \times \vec{B}$$

$$\vec{v} = v\hat{k} \quad \vec{B} = B\hat{i}$$

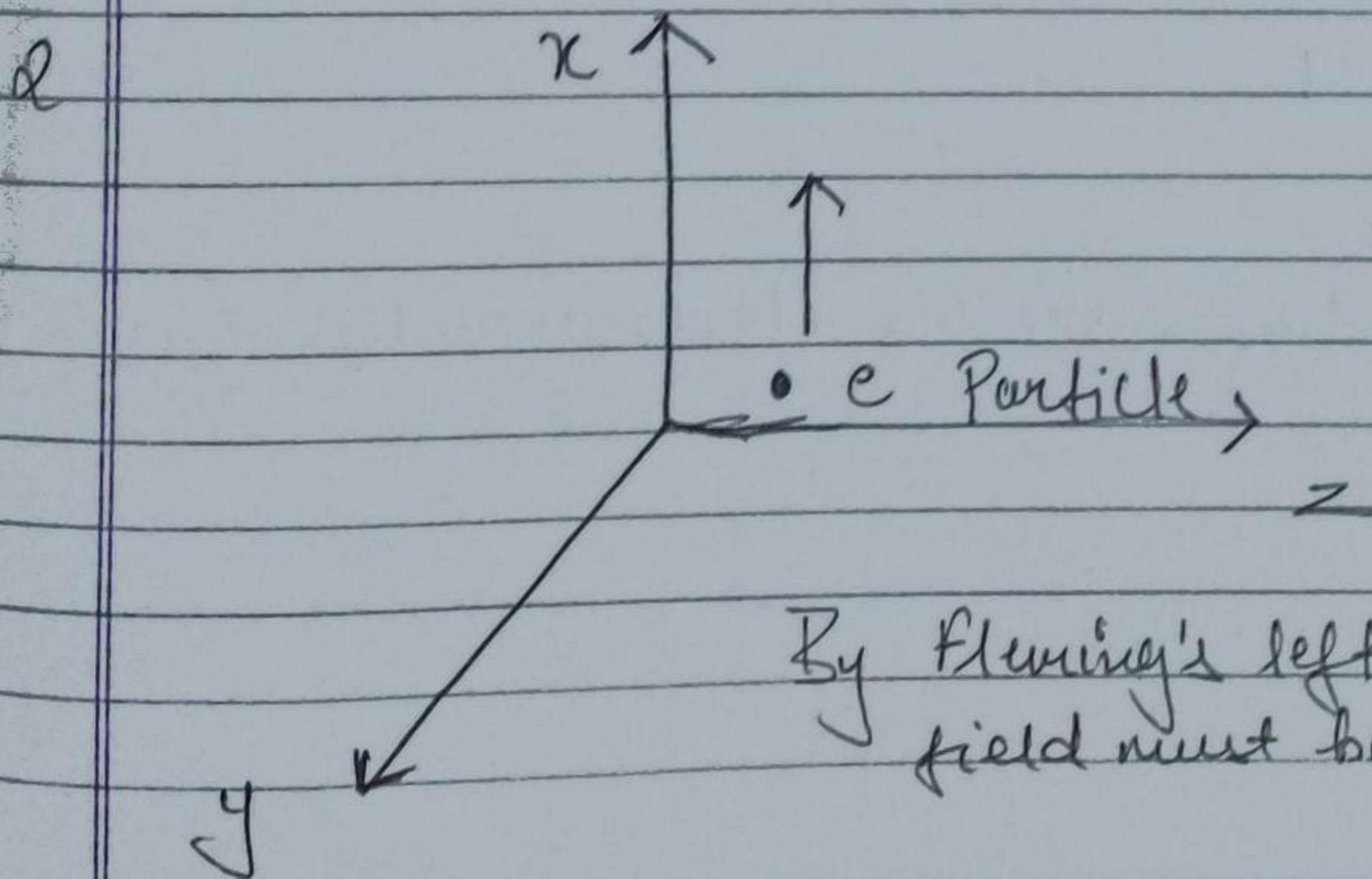
$$\vec{F} = q(v\hat{k}) \times (B\hat{i}) = qvB\hat{j}$$

i for a Beam of charged particles to pass undeflected crossed electric and magnetic fields, the condition is that electric and magnetic forces on the beam must be equal and opposite.

Given $E = 50 \text{ kV/m} = 50 \times 10^3 \text{ V/m}$, $B = 50 \text{ mT} = 50 \times 10^{-3} \text{ T}$

$$v = \frac{50 \times 10^3}{50 \times 10^{-3}} = 1 \times 10^6 \text{ m s}^{-1}$$

ii The beam strikes the target with a constant velocity so force exerted on the target is zero. However if proton beam come to rest it exerts a force on the target, equal to rate of change of linear momentum of the beam.



By Fleming's left hand rule magnetic field must be along negative z-axis

3 One Tesla is the magnetic field in which a charge of 1C moving with a velocity of 1ms^{-1} normal to the magnetic field, experiences a force of 1N

$$B = \frac{F}{qv \sin \theta}$$

If $F = 1\text{N}$, $q = 1\text{C}$, $v = 1\text{ms}^{-1}$, $\theta = 90^\circ$

then SI unit of $B = \frac{1\text{N}}{1\text{C} \cdot 1\text{ms}^{-1} \cdot \sin 90^\circ}$
 $= 1\text{NA}^{-1}\text{m}^{-1} = 1\text{tesla}$

4 When a charge particle enters a region of uniform magnetic field, perpendicular to their path they move in a circular path.

And the time period of their motion is given by

$$T = \frac{2\pi m}{qB}$$

But $f = \frac{1}{T}$

$$f = \frac{qB}{2\pi m}$$

Since B and q is same for electron and proton
 so $f \propto \frac{1}{m}$

§ We know that when a charged particle enters a uniform magnetic field the force exerted on it.

$$F = q(v \times B) = qvB \sin \theta$$

Case I when the particle enters perpendicular $\theta = 90^\circ$

In this case since $\sin \theta = 1$ is the maximum value and the direction of motion of particle hence the particle hence the particle starts moving in a circular path with radius.

$$r = mv / bq$$

Case II : the particle enters at an angle of 30°

In this case the force acting on it has two components one parallel to the motion which will cause a linear motion the other component will act perpendicular to motion which will cause circular motion.

Hence due to resultant of these two components the particle will move along a Helical Path.