

CHAPTER - 4 - MOVING CHARGES AND MAGNETISM

- 1 Number of turns on the circular coil $n = 100$
Radius of each turn $r = 8.0 \text{ cm} = 0.08 \text{ m}$
 $I = 0.4 \text{ A}$

$$|B| = \frac{\mu_0}{4\pi} \frac{2\pi n i}{r}$$

where

$$\mu_0 = \text{permeability of free space} \\ = 4\pi \times 10^{-7} \text{ TmA}^{-1}$$

$$|B| = \frac{4\pi \times 10^{-7}}{4\pi} \times \frac{2\pi \times 100 \times 0.4}{0.08} \\ = 3.14 \times 10^{-4} \text{ Tesla}$$

- 2 $I = 35 \text{ A}$ $r = 0.2 \text{ m}$ $B = \frac{\mu_0}{4\pi} \frac{2i}{r}$

$$\mu_0 = 4\pi \times 10^{-7} \text{ TmA}^{-1} \\ B = \frac{4\pi \times 10^{-7} \times 2 \times 35}{4\pi \times 0.2} \\ = 3.5 \times 10^{-5} \text{ T}$$

- 6 $l = 3 \text{ cm} = 0.03 \text{ m}$

$$I = 10 \text{ A}$$

$$B = 0.27 \text{ T}$$

$$\theta = 90^\circ$$

$$F = BIl \sin \theta$$

$$= 0.27 \times 10 \times 0.03 \sin 90^\circ$$

$$= 8.1 \times 10^{-2} \text{ N}$$

7 $I_A = 8A$ $I_B = 50A$ $r = 0.04m$ $l = 0.1m$

$$B = \frac{\mu_0 2 I_A I_B l}{4\pi r}$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ TMA}^{-1}$$

$$B = \frac{4\pi \times 10^{-7} \times 2 \times 8 \times 5 \times 0.1}{4\pi \times 0.04}$$

$$= 2 \times 10^{-5} \text{ N}$$

8 $l = 80cm = 0.8m$

$$N = 5 \times 400 = 2000$$

$$D = 0.0018m$$

$$I = 8.00A$$

$$B = \frac{\mu_0 NI}{D}$$

$$B = \frac{4\pi \times 10^{-7} \times 2000 \times 8}{0.0018} = 2.512 \times 10^{-3} \text{ T}$$

11 $B = 6.5G = 6.5 \times 10^{-4} \text{ T}$

$$v = 4.8 \times 10^6 \text{ m/s}$$

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$m_e = 9.1 \times 10^{-31} \text{ kg}$$

$$\theta = 90^\circ$$

$$F = evB \sin \theta$$

$$F_c = \frac{mv^2}{r}$$

$$F_c = F$$

$$\frac{mv^2}{r} = evB \sin \theta$$

$$r = \frac{mv}{Be \sin \theta}$$

$$= \frac{9.1 \times 10^{-31} \times 4.0 \times 10^6}{6.5 \times 10^{-4} \times 1.6 \times 10^{-19} \times \sin 90^\circ}$$

$$\Rightarrow 4.2 \times 10^{-2} \text{ m} = 4.2 \text{ cm}$$

12 a

$$n = 30$$

$$r = 0.08 \text{ m}$$

$$\text{Area of coil} = \pi r^2 = \pi (0.08)^2 = 0.0201 \text{ m}^2$$

$$I = 6.0 \text{ A}$$

$$B = 1 \text{ T}$$

$$\theta = 60^\circ$$

$$\tau = n I B A \sin \theta$$

$$= 30 \times 6 \times 1 \times 0.0201 \times \sin 60^\circ$$

$$= 3.133 \text{ Nm}$$

b It can be inferred from relation that the magnitude of the applied force torque is not dependent on the shape of the coil. It depends on area of coil. Hence the answer would not change if the circular coil in the above case is replaced by a planar coil of some irregular shape that encloses the same area.

14 $r_1 = 0.16 \text{ m}$ $r_2 = 10 \text{ cm}$ $n_1 = 20$ $n_2 = 25$ $I_1 = 16 \text{ A}$
 $I_2 = 18 \text{ A}$

$$B_1 = \frac{\mu_0 n_1 I_1}{2r_1} = \frac{4\pi \times 10^{-7} \times 20 \times 16}{2 \times 0.16} = 4\pi \times 10^{-4} \text{ T}$$

(towards east)

$$B_2 = \frac{\mu_0 n_2 I_2}{2r_2} = \frac{4\pi \times 10^{-7} \times 85 \times 18}{2 \times 0.10}$$

$$\Rightarrow 9\pi \times 10^{-4} \text{ T (towards west)}$$

$$\begin{aligned} B &= B_2 - B_1 \\ &= 9\pi \times 10^{-4} - 4\pi \times 10^{-4} \\ &= 5\pi \times 10^{-4} \text{ T} \\ &= 1.57 \times 10^{-3} \text{ T (towards West)} \end{aligned}$$

15 $B = 100 \text{ G} = 100 \times 10^{-4} \text{ T}$

$n = 1000 \text{ turns m}^{-1}$

$I = 1 \text{ A}$

$\mu_0 = 4\pi \times 10^{-7} \text{ T m A}^{-1}$

$$B = \mu_0 n I$$

$$\frac{100 \times 10^{-4}}{4\pi \times 10^{-7}} = 7957.47$$

$$= 8000 \text{ A/m}$$

If the length of the coil is taken as 50 cm radius 4 cm turns 400 and $I = 10 \text{ A}$ then these values are not unique.

17 $r_1 = 0.25 \text{ m}$ $r_2 = 0.26 \text{ m}$ $N = 3500$

$I = 11 \text{ A}$

a) Magnetic field outside a toroid is zero. It is non-zero only inside the core of a toroid.

b $B = \frac{\mu_0 N I}{l}$

$$= 2\pi \left[\frac{r_1 + r_2}{a} \right]$$

$$= 2\pi (0.25 + 0.26)$$

$$= 0.51\pi$$

$\therefore B = \frac{4\pi \times 10^{-7}}{0.51\pi} \times 3500 \text{ A}$

$$= 3.0 \times 10^{-2} \text{ T}$$

c It is zero

18

a) The initial velocity of the particle is either parallel or anti parallel to the magnetic field. Hence it travels along a straight path without suffering any deflection in the field.

b) Yes it will be equal because magnetic force can change the direction of velocity but not its magnitude.

c) An electron travelling from west to east enters a chamber having a uniform electrostatic field in the N-S direction. The moving electron can remain undeflected if the electric force acting on it is equal and opposite of $B \cdot v$. Magnetic force is directed towards the south. According to Fleming's left hand rule, magnetic field should be applied in a vertically downward direction.

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$$B = 0.15 \text{ T}$$

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$m = 9.1 \times 10^{-31} \text{ kg}$$

$$V = 2.0 \text{ kV} = 2 \times 10^3 \text{ V}$$

ev

$$\Rightarrow eV = \frac{1}{2} m v^2$$

$$v = \sqrt{\frac{2eV}{m}}$$

a Magnetic force on the electron provides the required centripetal force of the electron. Hence, the electron traces a circular path of radius r .
Magnetic force on the electron is given by the relation

$$Bev$$

$$\text{Centripetal force} = \frac{mv^2}{r}$$

$$\therefore Bev = \frac{mv^2}{r}$$

$$r = \frac{mv}{Be}$$

$$r = \frac{m}{Be} \left[\frac{2eV}{m} \right]^{\frac{1}{2}}$$

$$= \frac{9.1 \times 10^{-31}}{0.15 \times 1.6 \times 10^{-19}} \times \left(\frac{2 \times 1.6 \times 10^{-19} \times 2 \times 10^3}{9.1 \times 10^{-31}} \right)^{\frac{1}{2}}$$

$$= 100.55 \times 10^{-5}$$

$$= 1.01 \times 10^{-3} \text{ m}$$

$$= 1 \text{ mm}$$

b

$$r_1 = v \sin \theta$$

$$r_1 = \frac{mv_1}{Be} = \frac{mv \sin \theta}{Be} = \frac{9.1 \times 10^{-31} \times 2 \times 10^6 \times \sin 30^\circ}{0.15 \times 1.6 \times 10^{-19} \times 9 \times 10^{-31}}$$

$$= 0.5 \times 10^{-3} \text{ m}$$

$$= 0.5 \text{ mm}$$

q0

$$B = 0.75 \text{ T}$$

$$V = 15 \text{ kV} = 15 \times 10^3 \text{ V}$$

$$E = 9 \times 10^5 \text{ V m}^{-1}$$

$$\Rightarrow \frac{1}{2} mv^2 = eV$$

$$\therefore \frac{e}{m} = \frac{v^2}{2V}$$

Since the particle remains undeflected by electric and magnetic fields, we can infer that the electric field is balancing the magnetic field.

$$\therefore eE = evB$$

$$v = \frac{E}{B}$$

$$\Rightarrow \frac{e}{m} = \frac{1}{2} \frac{\left(\frac{E}{B}\right)^2}{V} = \frac{E^2}{2VB^2}$$

$$= \frac{(9.0 \times 10^5)^2}{2 \times 15000 \times (0.75)^2} = 4.8 \times 10^7 \text{ C/kg}$$

Q7

$$G_g = 12 \Omega$$

$$I_g = 3 \text{ mA} = 3 \times 10^{-3} \text{ A}$$

$$V = 18 \text{ V}$$

$$R = \frac{V}{I_g} - G_g$$

$$= \frac{18}{3 \times 10^{-3}} - 12 = 6000 - 12 = 5988 \Omega$$

Hence a resistor 5988Ω is to be connected in the series with galvanometer.

Q8

$$G_g = 15 \Omega$$

$$I_g = 4 \text{ mA} = 4 \times 10^{-3} \text{ A}$$

$$I = 6 \text{ A}$$

$$S = \frac{I_g G_g}{I - I_g} = \frac{4 \times 10^{-3} \times 15}{6 - 4 \times 10^{-3}}$$

$$S = \frac{6 \times 10^{-2}}{6 - 0.004} = \frac{0.06}{5.996}$$

$$= 0.01 \Omega = 10 \text{ m}\Omega$$