

Chapter - 5 - Magnetism and Matter

- 3 Magnetic field strength $B = 0.25 \text{ T}$
Torque on the bar magnet = $4.5 \times 10^{-2} \text{ J}$
 $\theta = 30^\circ$

$$T = MB \sin \theta$$

$$M = \frac{T}{B \sin \theta} = \frac{4.5 \times 10^{-2}}{0.25 \times \sin 30^\circ} = 0.36 \text{ J T}^{-1}$$

- 4 a The bar magnet of magnetic moment $M = 0.22 \text{ J T}^{-1}$ is placed in a uniform magnetic field of 0.15 T

The bar magnet is aligned along the magnetic field. The system is considered as being in stable equilibrium. Hence the angle θ between the bar magnet and field is 0°

$$\begin{aligned} \text{Potential energy} &= +MB \cos \theta \\ &= 0.22 \times 0.15 \cos 180^\circ \\ &= 4.8 \times 10^{-2} \text{ J} \end{aligned}$$

5 $n = 800$ $A = 2.5 \times 10^{-4} \text{ m}^2$ $I = 3.0 \text{ A}$

A current-carrying solenoid behaves as a bar magnet because a magnetic field develops along its axis i.e. along its length.

$$\begin{aligned} M &= nIA \\ &= 800 \times 3 \times 2.5 \times 10^{-4} \\ &= 0.6 \text{ J T}^{-1} \end{aligned}$$

8

a $M = nIA$
 $= 2000 \times 1.6 \times 10^{-4} \times 4$
 $= 1.28 \times 10^{-1} \text{ Am}^2$

b

$B = 7.5 \times 10^{-2} \text{ T}$
 $\theta = 30^\circ$
 $\tau = MB \sin \theta$
 $1.28 \times 7.5 \times 10^{-2} \sin 30^\circ$
 $\Rightarrow 4.8 \times 10^{-2} \text{ Nm}$

\Rightarrow Since the magnetic field is uniform the force of rotation is zero.

9

$N = 16, r = 10 \text{ cm}, A = \pi r^2 = \pi \times (0.1)^2 \text{ m}^2$
 $I = 0.75 \text{ A}, B = 5.0 \times 10^{-2} \text{ T}, \nu = 2.0 \text{ s}^{-1}$

Magnetic moment = $M = NIA = N I \pi r^2$
 $= 16 \times 0.75 \times \pi \times (0.1)^2$
 $\Rightarrow 0.377 \text{ JT}^{-1}$

Frequency $\nu = \frac{1}{2\pi} \sqrt{\frac{MB}{I}}$

Where

$I =$ moment of inertia of the coil

$\therefore I = \frac{MB}{4\pi^2 \nu^2} = \frac{0.377 \times 5 \times 10^{-2}}{4\pi^2 \times 2^2}$
 $= 1.19 \times 10^{-4} \text{ kg m}^2$

11 $\theta = 12^\circ$ Angle of dip $= 60^\circ$ $B_H = 0.16 \text{ G}$

$$B_H = B \cos \theta$$

$$\therefore B = \frac{B_H}{\cos \theta} = \frac{0.16}{\cos 60^\circ} = 0.32 \text{ G}$$

13 $H = 0.36 \text{ G}$

$$B_1 = \frac{\mu_0}{4\pi} \frac{2M}{d^3} = H$$

where

μ_0 = Permeability of free space

M = magnetic field

$$B_2 = \frac{\mu_0 M}{4\pi d^3} = \frac{H}{2}$$

$$\text{Total } B = B_1 + B_2$$

$$= H + \frac{H}{2}$$

$$= 0.36 + 0.18$$

$$= 0.54 \text{ G}$$

18 $I = 2.5 \text{ A}$ $\theta = 0^\circ$ $H = 0.33 \text{ G} = 0.33 \times 10^{-4} \text{ T}$

$$H_H = H \cos \theta = 0.33 \times 10^{-4} \cos 0^\circ = 0.33 \times 10^{-4} \text{ T}$$

$$H_H = \frac{\mu_0 I}{2\pi R}$$

where,

$$\mu_0 = \text{Permeability of free space} = 4\pi \times 10^{-7} \text{ TmA}^{-1}$$

$$\therefore R = \frac{4\sigma T^4}{2\pi h \nu}$$

$$= \frac{4\pi \times 10^{-7} \times 2.05}{2\pi \times 0.33 \times 10^{-4}} = 15.15 \times 10^{-3} = 1.51 \text{ cm}^{-1}$$