

1. Proof - ex-7.3
In $\triangle ABD$ and $\triangle ACD$

$AB = AC$ (given)
 $AD = DA$ (common)
 $BD = CD$ (given)

$\triangle ABD \cong \triangle ACD$ (SSS)

$\angle 1 = \angle 2$ (CPCT) — (1)

In $\triangle ABP$ and $\triangle ACP$

$AB = AC$ (given)
 $AP = PA$ (common)
 $\angle 1 = \angle 2$ (proved)

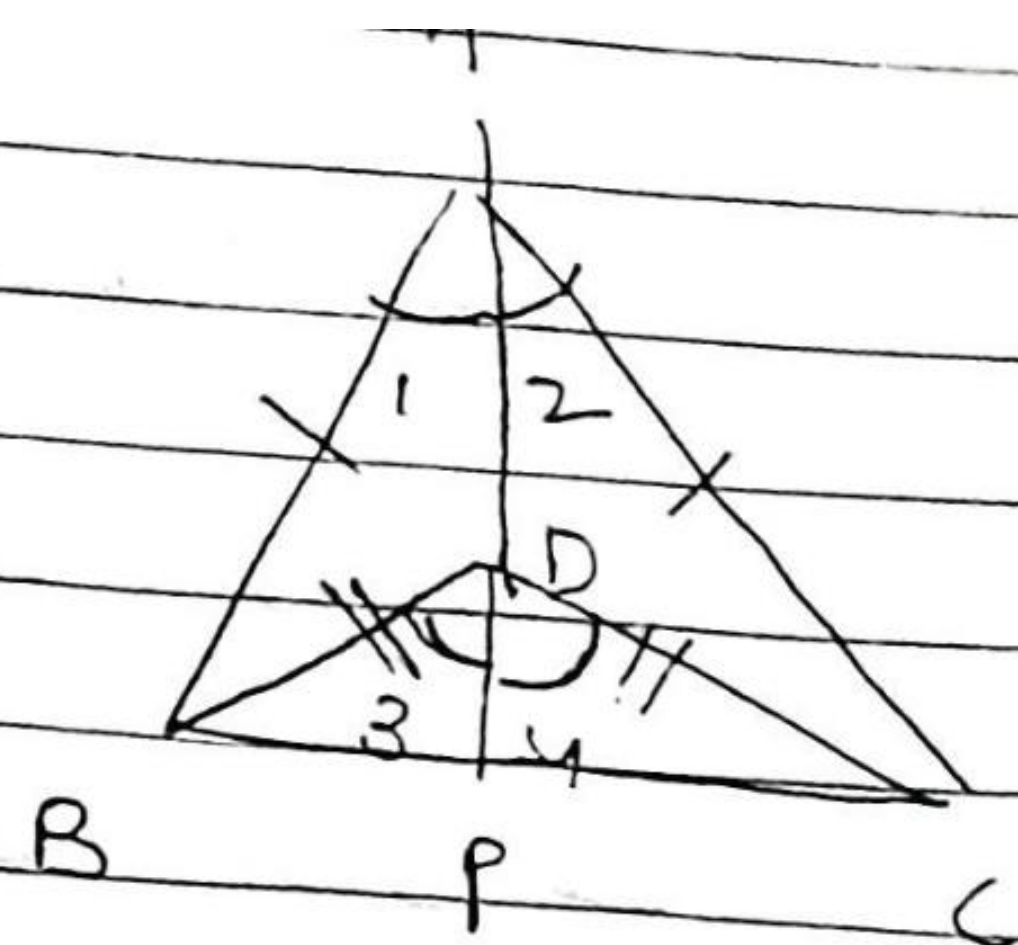
$\triangle ABP \cong \triangle ACP$ (SAS)

$\angle APB = \angle APC$ (CPCT)

$\angle APB + \angle APC = \underline{180}$ (LP)

$\angle APB = \angle APC = 90^\circ$

AP is the perpendicular bisector



In $\triangle BDP$ and $\triangle CDP$

$$BD = CD \text{ (given)}$$

$$DP = DP \text{ (common)}$$

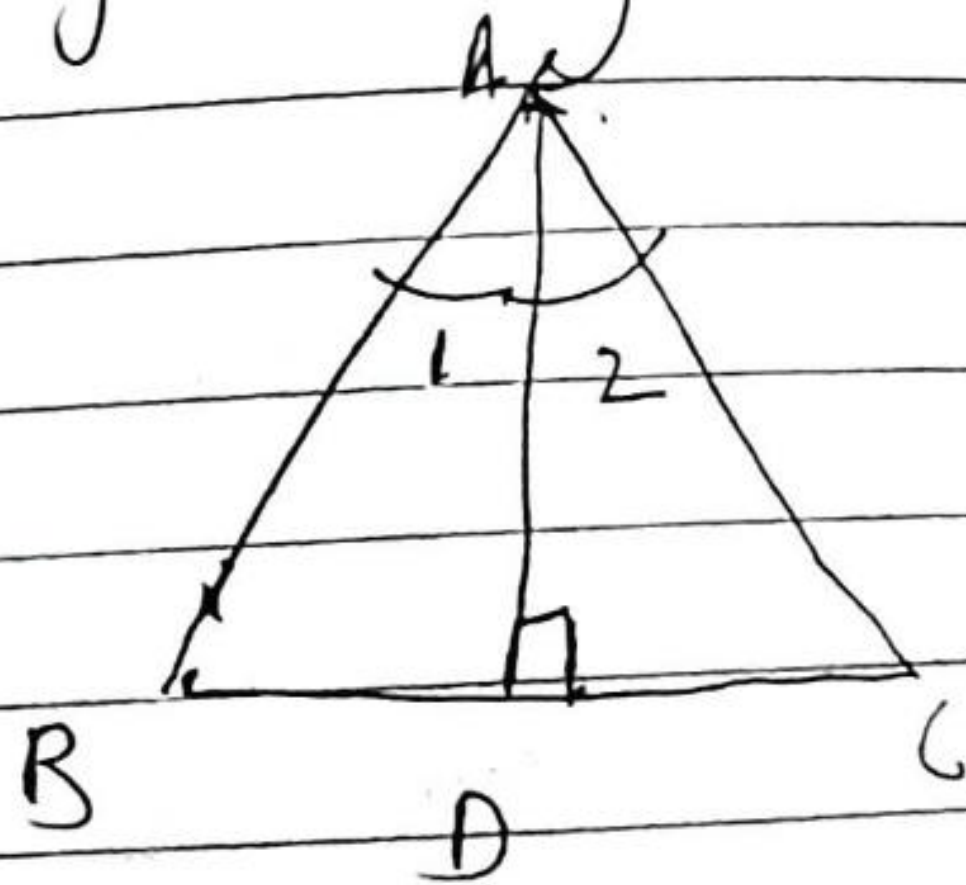
$$\angle DPB = \angle DPC \text{ (90}^\circ\text{)}$$

$$\triangle BDP \cong \triangle CDP \text{ (RHS)}$$

$$\angle 3 = \angle 4 \text{ (CPT) — (2)}$$

from (1) and (2) AP is the bisector of $\angle A$
and LD .

2^o To prove DA bisects BC
AD bisects $\angle A$



In $\triangle ABD$ and $\triangle ADC$ -

$$AB = AC \text{ (given)}$$

$$\angle ADB = \angle ADC \text{ (90}^\circ\text{)}$$

$$AD = AD \text{ (common)}$$

$$\triangle ABD \cong \triangle ADC \text{ (RHS)}$$

$$BD = DC \text{ (CPT)}$$

$$\angle 1 = \angle 2 \text{ (CPT)}$$

AD bisects $\angle A$.