

Exercise

Q3  $\theta = 30^\circ$  (Angle the axis of the magnet makes with the ext field?)  
 $B = 0.25 \text{ T}$  (Uniform external field)  
 $M = ??$   
 $\tau = 4.5 \times 10^{-2} \text{ J}$

$$\tau = BM \sin \theta$$

$$= 0.25 \times x \times \sin 30^\circ$$

$$4.5 \times 10^{-2} = 0.25 \times \frac{1}{2} \times x$$

$$x = \frac{4.5 \times 10^{-2} \times 2}{0.25}$$

$$M = \underline{0.36 \text{ T}^{-1}} \text{ (Ans)}$$

4)  $M = 0.32 \text{ T}^{-1}$   
 $B = 0.15 \text{ T}$

(a) stable  $\rightarrow \theta = 0^\circ$  (Angle betn magnetic moment & magnetic field)  
 unstable  $\rightarrow \theta = 180^\circ$  (Angle betn  $\vec{M}$  &  $\vec{B}$ )

b) P.E. : In stable  $\rightarrow -MB \cos \theta$  ( $\theta = 0^\circ$ )  
 $= -MB = -0.32 \times 0.15 = -4.8 \times 10^{-2} \text{ J}$

: Unstable  $\rightarrow -MB \cos \theta$  ( $\theta = 180^\circ$ )  $= +4.8 \times 10^{-2} \text{ J}$   
 $= \underline{+MB}$



Q5) <sup>ans</sup> A current-carrying solenoid behaves as a bar magnet because a magnetic field develops along its axis, i.e., along its length.

~~ans~~  $N = 800$  turns

$$I = 3.0 \text{ A}$$

$$A = 2.5 \times 10^{-4} \text{ m}^2$$

$$M = NIA$$

$$= 800 \times 3 \times 2.5 \times 10^{-4}$$

$$= 0.6 \text{ J T}^{-1}$$

Q6)  $M = 1.5 \text{ J T}^{-1}$

$$B = 0.22 \text{ T}$$

$$\text{Initial Angle} = 0^\circ$$

( $\theta_1$ )

} given in the Q

a) Work req. to ~~real~~ turn the magnet so as to align its magnetic moment:

i) normal to the field direction

ans)  $\theta_2 = 90^\circ$

$$\text{Work} = -MB [\cos \theta_2 - \cos \theta_1]$$

$$= -MB [\cos 90^\circ - \cos 0]$$

$$= +MB$$

$$= 1.5 \times 0.22$$

$$= \underline{0.33 \text{ J}}$$

ii) opposite to the electric field

$$\theta_2 = 180^\circ$$



Work:  $-MB [\cos 0_2 - \cos 0_1]$   
 $= -MB [\cos 180^\circ - \cos 0^\circ]$   
 $= +2MB$   
 $= 2V \cdot 0.33$   
 $= 0.66 \text{ J}$

(b) For case (i):  
 $\tau = MB \sin \theta$   
 $= MB \sin 90^\circ$   
 $= 1.5 \times 0.22$   
 $= \underline{0.33 \text{ J}}$

For case (ii):  
 $\tau = MB \sin \theta$   
 $= 1.5 \times 0.22 \times \sin 180^\circ$   
 $= \underline{0 \text{ J}}$

Q8  $N = 2000$  turns  
 $A = 1.6 \times 10^{-4} \text{ m}^2$   
 $I = 4 \text{ A}$

a) Magnetic moment ( $M$ ) =  $NIA$   
 $= 2000 \times 1.6 \times 10^{-4} \times 4$   
 $= 128 \times 10^2 \times 10^{-4}$   
 $= 128 \times 10^{-2}$   
 $= \underline{1.28 \text{ A m}^2}$

b) Uniform magnetic field:  
Net force = 0



$$\begin{aligned}\text{Net Torque} &= \cancel{m} \times B \sin \theta \\ &= 1.28 \times 7.5 \times 10^{-3} \sin 30 \\ &= 9.984 \times \frac{1}{2} \times 10^{-2} \\ &= \underline{4.8 \times 10^{-2} \text{ Nm}}\end{aligned}$$

9)  $N = 16$   
 $R = 10 \times 10^{-2} \text{ m}$        $A = \pi R^2 = \pi \times (0.1)^2 \text{ m}^2$   
 $I = \underline{0.75 \text{ A}}$

$$B = 5.0 \times 10^{-2} \text{ T}$$

$$\text{frequency } (\nu) = 2.0 \text{ s}^{-1}$$

$$\begin{aligned}\text{Magnetic moment} &= NIA \\ &= 16 \times 0.75 \times \pi \times (0.1)^2 \\ &= \underline{0.377 \text{ J T}^{-1}}\end{aligned}$$

Frequency:

$$\nu = \frac{1}{2\pi} \sqrt{\frac{MB}{I}}$$

$$I = \frac{MB}{4\pi^2 \nu^2}$$

$$= \frac{0.377 \times 5 \times 10^{-2}}{4\pi^2 \times (2)^2}$$

$$= \underline{1.19 \times 10^{-4} \text{ kg m}^2}$$

ii)  $B_H = 0.35 \text{ G} \quad 0.16 \text{ G}$   
 Angle of dip =  $\delta = 60^\circ$   
 Angle of declination,  $\theta = 12^\circ$

$$B_H = B \cos \delta$$

$$B = \frac{B_H}{\cos \delta}$$

$$= \frac{0.16}{\cos 60^\circ} = 0.32 \text{ G}$$

The earth's ~~axis~~ magnetic field lies in the vertical plane  $12^\circ$  west of the geographic meridian making an angle of  $60^\circ$  <sup>upwards</sup> with the horizontal direction.

iii)  $M = 0.36 \text{ G}$

$$B_1 = \frac{\mu_0}{4\pi} \cdot \frac{2M}{d^3} = M$$

$B_2$  at the normal bisector =  $\frac{B_1}{2} = \frac{\mu_0}{4\pi} \frac{M}{d^3} = \frac{M}{2}$

$$\text{Total magnetic field} = \frac{M}{2} + B_1$$

$$= M + \frac{M}{2}$$

$$= 0.36 + 0.18$$

$$= 0.54 \text{ G}$$



18)  $I = 2.5 \text{ A}$

$\theta = 0^\circ$

$B_H = B \cos \theta$

$= 0.33 \times 10^{-4} \times \cos 0^\circ$

$= 0.33 \times 10^{-4} \text{ T}$

$B_H = \frac{\mu_0 I}{2\pi R}$  (Magnetic field at a distance R from a straight wire)

$R = \frac{\mu_0 I}{2\pi B_H}$

$= \frac{4\pi \times 10^{-7} \times 2.5}{2\pi \times 0.33 \times 10^{-4}} = 15.15 \times 10^{-3} \text{ m} = 1.51 \text{ cm}$

Ans) Parallel to & above the cable at a distance of 1.5 cm.