

Morice on Addition and Subtraction.

Addition of Polynomials (Row method)

Exercise 19(B)

1. Find the sum of:

i $3a+4b+7c,$ $-5a+3b-6$

$a-2b-4c$

Ans: $= 3a+4b+7c-5a+3b-6c+4a-2b$
 $= (3a-5a+4a) + (4b+3b-2b) + (7c-6c)$
 $= 2a+5b+7c-10c$
 $= 2a+5b-3c$

ii $2x^2+xy-y^2,$ $-x^2+2xy+3y^2$ and $3x^2-10xy+4y^2$

Ans: $= 2x^2+xy-y^2 + (-x^2+2xy+3y^2) + 3x^2-10xy+4y^2$
 $= (2x^2+3x^2-x^2) + (xy+2xy-10xy) + (-y^2+3y^2+4y^2)$

Sol: $(2x^2+xy-y^2) + (-x^2+2xy+3y^2) + (3x^2-10xy+4y^2)$
 $= 2x^2-x^2+3x^2+xy+2xy-10xy-1y^2+3y^2+4y^2$
 $= 4x^2-7xy+6y^2$

iii $x^2-x+1,$ $-5x^2+2x-2$ and $3x^2-3x+1$

Sol: $= (x^2-x+1) + (-5x^2+2x-2) + (3x^2-3x+1)$
 $= x^2-5x^2+3x^2-x+2x-3x+1-2+1$
 $= -4x^2+x-2$
 $= -4x^2+x-2$

iv $a^2-ab+bc,$ $2ab+bc-2a^2$ and $3bc+3a^2+ab$

Sol: $= (a^2-ab+bc) + (2ab+bc-2a^2) + (3bc+3a^2+ab)$
 $= a^2-2a^2+3a^2-ab+2ab+ab+bc+bc-3bc$
 $= -a^2+3a^2+ab+ab-3bc$

v $4x^2+7-3x,$ $4x-x^2+8$ and $-10+5x-2x^2$

Sol: $= (4x^2+7-3x) + (4x-x^2+8) + (-10+5x-2x^2)$
 $= 4x^2-x^2-2x^2+7+8-10-3x+4x+5x$
 $= 3x^2+15-10+3x+5x$
 $= 3x^2+5+8x$

2. Add the following expressions:

i) $-17x^2 - 2xy + 23y^2$, $-9y^2 + 15x^2 + 7xy$ and $13x^2 + 3y^2 - 4xy$

$$\begin{aligned} \text{Soln:} &= (-17x^2 - 2xy + 23y^2) + (-9y^2 + 15x^2 + 7xy) + (13x^2 + 3y^2 - 4xy) \\ &= -17x^2 + 15x^2 + 13x^2 - 2xy + 7xy - 4xy + 23y^2 - 9y^2 + 3y^2 \\ &= -2x^2 + 13x^2 + 5xy - 4xy + 14y^2 + 3y^2 \\ &= 11x^2 + 9xy + 17y^2 \end{aligned}$$

ii) $-x^2 - 3xy + 3y^2 + 8$, $3x^2 - 5y^2 - 3 + 4xy$ and $-6xy + 2x^2 - 2y^2$

$$\begin{aligned} \text{Soln:} &= (-x^2 - 3xy + 3y^2 + 8) + (3x^2 - 5y^2 - 3 + 4xy) + (-6xy + 2x^2 - 2y^2) \\ &= -x^2 + 3x^2 + 2x^2 - 3xy + 4xy - 6xy + 3y^2 - 5y^2 + 2y^2 + 8 - 3 \\ &= 4x^2 - 7xy - 4y^2 + 5 \end{aligned}$$

iii) $a^3 - 2b^3 + a$, $b^3 - 2a^3 + b$ and $-2b + 2b^3 - 5a + 4a^3$

$$\begin{aligned} \text{Soln:} &= (a^3 - 2b^3 + a) + (b^3 - 2a^3 + b) + (-2b + 2b^3 - 5a + 4a^3) \\ &= a^3 - 2a^3 + 4a^3 - 2b^3 + b^3 + 2b^3 + a + b - 2b - 5a \\ &= 3a^3 + b^3 - 4a - b \end{aligned}$$

3. Evaluate

i) $3a - (a + 2b)$

$$\begin{aligned} \text{Soln:} &= 3a - a - 2b \\ &= 2a - 2b \end{aligned}$$

iv) $(8x + 7y) - (4y - 3x)$

$$\begin{aligned} \text{Soln:} &= 8x + 7y - 4y + 3x \\ &= 8x + 3x + 7y - 4y \end{aligned}$$

ii) $(5x - 3y) - (9x + y)$

$$\begin{aligned} \text{Soln:} &= 5x - 3y - 9x - y \\ &= 5x - 9x - 3y - y \\ &= 4x + 2y \end{aligned}$$

$$= 11x + 3y$$

v) $7 - (4a - 5)$

$$\begin{aligned} \text{Soln:} &= 7 - 4a + 5 \\ &= 7 + 5 - 4a \end{aligned}$$

iii) $(8a + 15b) - (3b - 7a)$

$$\begin{aligned} \text{Soln:} &= 8a + 15b - 3b + 7a \\ &= 8a + 7a + 15b - 3b \\ &= 15a + 12b \end{aligned}$$

$$= 12 - 4a$$

vi) $(6y - 13) - (4 - 7y)$

$$\begin{aligned} \text{Soln:} &= (6y - 13) - 4 + 7y \\ &= 6y + 7y - 13 - 4 \\ &= -y - 17 \end{aligned}$$

• Subtract

③ $5a - 3b + 2c$ from $a - 4b - 2c$

$$\begin{aligned}\text{Sol: } & (a - 4b - 2c) - (5a - 3b + 2c) \\ & = (a - 4b - 2c) - 5a + 3b - 2c \\ & = a - 5a - 4b + 3b - 2c - 2c \\ & = -4a - b - 4c\end{aligned}$$

④ $4x - 6y + 3z$ from $12x + 7y - 2z$

$$\begin{aligned}\text{Sol: } & (12x + 7y - 2z) - (4x - 6y + 3z) \\ & = (12x + 7y - 2z) - 4x + 6y - 3z \\ & = 12x - 4x + 7y + 6y - 2z - 3z \\ & = 8x + 13y - 5z\end{aligned}$$

⑤ $5a - 3b + 2c$ from $5a - 7b + 2c$

$$\begin{aligned}\text{Sol: } & (5a - 7b + 2c) - (5a - 3b + 2c) \\ & = (5a - 7b + 2c) - 5a + 3b - 2c \\ & = 5a - 5a - 7b + 3b + 2c - 2c \\ & = -4b\end{aligned}$$

⑥ $5a - a - 4b + 4c$ from $5a - 7b + 2c$

$$\begin{aligned}\text{Sol: } & (5a - 7b + 2c) - (5a - a - 4b + 4c) \\ & = (5a - 7b + 2c) - 5a + a + 4b - 4c \\ & = 5a - 5a - 7b + 4b + 2c - 4c + a \\ & = -3b - 2c + a\end{aligned}$$

⑦ $-8x - 12y + 17z$ from $x - y - z$

$$\begin{aligned}\text{Sol: } & (x - y - z) - (-8x - 12y + 17z) \\ & = (x - y - z) + 8x + 12y - 17z \\ & = x + 8x - y + 12y - z - 17z \\ & = 9x + 11y - 18z\end{aligned}$$

⑧ $2ab + cd + ac - 2bd$ from $ab - 2cd + 2ac + bd$

$$\begin{aligned}\text{Sol: } & (ab - 2cd + 2ac + bd) - (2ab + cd - ac - 2bd) \\ & = ab - 2cd + 2ac + bd - 2ab - cd + ac + 2bd \\ & = ab - 2ab - 2cd - cd + 2ac + ac + bd + 2bd \\ & = -ab - 3cd + 3ac + 3bd\end{aligned}$$

5, i) Take $-ab+bc-ca$ from $bc-ca+ab$

$$\begin{aligned}\text{Ans:} &= (bc-ca+ab) - (-ab+bc+ca) \\ &= bc-ca+ab+ab-bc+ca \\ &= bc-bc-ca+ca+ab+ab \\ &= 2ab\end{aligned}$$

ii) Take $5x+6y-3z$ from $3x+5y-4z$

$$\begin{aligned}\text{Sol:} &= (3x+5y-4z) - (5x+6y-3z) \\ &= (3x+5y-4z) - 5x - 6y + 3z \\ &= 3x - 5x + 5y - 6y - 4z + 3z \\ &= -2x - y - z\end{aligned}$$

iii) Take $-\frac{3}{2}p+q-r$ from $\frac{1}{2}p-\frac{1}{3}q-\frac{2}{9}r$

$$\begin{aligned}\text{Sol:} &= (\frac{1}{2}p - \frac{1}{3}q - \frac{2}{9}r) - (-\frac{3}{2}p + q - r) \\ &= (\frac{1}{2}p - \frac{1}{3}q - \frac{2}{9}r) + \frac{3}{2}p - q + r \\ &= \frac{1}{2}p - \frac{1}{3}q - \frac{2}{9}r + \frac{3}{2}p - q + r \\ &= \frac{4}{2}p - \frac{4}{3}q - \frac{1}{9}r \\ &= 2p - \frac{4}{3}q - \frac{1}{9}r\end{aligned}$$

iv) Take $1-a+a^2$ from a^2+a+1

$$\begin{aligned}\text{Sol:} &= (a^2+a+1) - (1-a+a^2) \\ &= (a^2+a+1) - 1+a-a^2 \\ &= a^2-a^2+a+a+1-1 \\ &= 0+2a+0 \\ &= 2a\end{aligned}$$

6. From the sum of $x+y-2z$ and $2x-y+z$ subtract $x+y+z$.

$$\begin{aligned}\text{Sol:} &= \text{The sum of } x+y-2z \text{ and } 2x-y+z \\ &= x+y-2z + 2x-y+z \\ &= \overset{+2x}{x} + y - 2z + z \\ &= 3x - z\end{aligned}$$

6. From the sum of $x+y-z$ and $2x-y+z$ subtract $x+y+z$.

Solⁿ: The sum of $x+y-z$ and $2x-y+z$

$$\begin{aligned} &= x+y-z+2x-y+z \\ &= x+2x+y-y-z+z \\ &= 3x-0-z \\ &= 3x-z \end{aligned}$$

Subtract $x+y+z$ from $3x-z$

$$\begin{aligned} &= (3x-z) - (x+y+z) \\ &= 3x-z-x-y-z \\ &= 3x-x-z-z-y \\ &= 2x-2z-y \end{aligned}$$

7. From sum of $3a-2b+4c$ and $3b-2c$ subtract $a-b-c$

Solⁿ: The sum of $3a-2b+4c$ and $3b-2c$

$$\begin{aligned} &= 3a-2b+4c+3b-2c \\ &= 3a-2b+3b+4c-2c \\ &= 3a+b+2c \end{aligned}$$

Subtract $a-b-c$ from $3a+b+2c$

$$\begin{aligned} &= (3a+b+2c) - (a-b-c) \\ &= 3a+b+2c-a+b+c \\ &= 3a-a+b+b+2c+c \\ &= 2a+2b+3c \end{aligned}$$

8. Subtract $x-2y-z$ from the sum of $3x-y+z$ and $x+y-3z$

Solⁿ: The sum of $3x-y+z$ and $x+y-3z$

$$\begin{aligned} &= 3x-y+z+x+y-3z \\ &= 3x+x-3x-y+y+z \\ &= 4x-3x-y+y+z \\ &= x+z \end{aligned}$$

9. Subtract the sum of $x+y$ and $x-z$ from the sum of $x-2z$ and $x+y+z$

Solⁿ: The sum of $x+y$ and $x-z$

$$\begin{aligned} &= x+y+x-z \\ &= x+x+y-z \end{aligned}$$

$$= 2x + y - z$$

The sum of $x - 2z$ and $x + y + z$

$$= x - 2z + x + y + z$$

$$= x + x - 2z + z + y$$

$$= 2x - z + y$$

Subtract $2x + y - z$ from $2x - z + y$

$$= (2x - z + y) - (2x + y - z) - (2x + y - z)$$

$$= (2x - z + y) - (2x + y - z)$$

$$= 2x - 2x - z + z + y - y$$

$$= 0$$

Exercise 19(c)

3. Find the value of:

i $3x^3 \times 5x^4$

Soln: =

1. Fill in the blanks.

i $6 \times 3 = 18$

and

$$6x \times 3x = 18x^2$$

ii $6 \times 3 = 18$

and

$$6x^2 \times 3x^3 = 18x^5$$

iii $5 \times 4 = 20$

and

$$5x \times 4y = 20xy$$

iv $4 \times 7 = 28$

and

$$4ax \times 7x = 28ax^2$$

v $6 \times 2 = 12$

and

$$6xy \times 2xy = 12x^2y^2$$

vi $12 \times 4 = 48$

and

$$12ax^2 \times 4ax = 48a^2x^3$$

vii $1 \times 8 = 8$

and

$$a^2xy^2 \times 8a^3x^2y = 8a^5x^3y^3$$

viii $15 \times 3 = 45$

and

$$15x \times 3x^5y^2 = 45x^6y^2$$