

22) In the fig, lines PQ, MN and RS are intersecting each other at O

$$x:y = 1:2, z = 90^\circ$$

$$\angle MOQ = \angle PON = x$$

Now RS is a straight line

$$\therefore x + z + y = 180^\circ$$

$$\Rightarrow x + y + 90^\circ = 180^\circ$$

$$\Rightarrow x + y = 180^\circ - 90^\circ = 90^\circ$$

$$\text{But } x:y = 1:2$$

$$\text{Let } x = a \text{ then } y = 2a$$

$$\therefore a:2a = 90^\circ$$

$$\Rightarrow 3a = 90^\circ$$

$$\Rightarrow a = \frac{90^\circ}{3} = 30^\circ$$

$$\therefore x = 30^\circ \text{ and } y = 2a = 2 \times 30^\circ = 60^\circ$$

$$\text{Now, } \angle ROM = y = 60^\circ$$

$$\text{and } \angle PQR = \angle SOQ$$

$$= x = 30^\circ$$

23) In the figure,

$$5x + x + 80^\circ + 123^\circ + 85^\circ = 360^\circ$$

$$\Rightarrow 6x + 80^\circ + 123^\circ + 85^\circ = 360^\circ$$

$$\Rightarrow 6x + 288^\circ = 360^\circ$$

$$\Rightarrow 6x = 360^\circ - 288^\circ = 72^\circ$$

$$\Rightarrow x = \frac{72^\circ}{6} = 12^\circ$$

Now,  $\angle AOB = 5x = 5 \times 12^\circ = 60^\circ$

and  $\angle BOC = x = 12^\circ$

24) In the fig,

$$3 \frac{1}{2} y^\circ + 2y^\circ + 2y^\circ + 2 \frac{1}{2} y^\circ = 360^\circ$$

$$\Rightarrow \frac{7}{2} y^\circ + 2y^\circ + 2y^\circ + \frac{5}{2} y^\circ = 360^\circ$$

$$\Rightarrow \frac{7}{2} y^\circ + \frac{5}{2} y^\circ + 4y^\circ = 360^\circ$$

$$\Rightarrow \frac{12}{2} y^\circ + 4y^\circ = 360^\circ$$

$$\Rightarrow 6y^\circ + 4y^\circ = 360^\circ$$

$$\Rightarrow 10y^\circ = 360^\circ$$

$$\Rightarrow y = \frac{360^\circ}{10} = 36^\circ$$

$$\therefore \angle AOB = 3 \frac{1}{2} y^\circ = \frac{7}{2} y^\circ = \frac{7}{2} \times 36^\circ$$

$$= 126^\circ$$

$$\angle BOC = 2y^\circ = 2 \times 36 = 72^\circ$$

$$\angle COD = 2y^\circ = 72^\circ$$

$$\angle DOA = 2 \frac{1}{2} y^\circ = \frac{5}{2} y^\circ$$

$$= \frac{5}{2} \times 36^\circ = 90^\circ$$



25) AB, CD and EF are intersecting each other at O  
and  $\angle DOF = x^\circ$ ,  $\angle AOC = y^\circ$   
and  $\angle BOE = z^\circ$

But  $\angle DOB = \angle AOC = y^\circ$

Similarly,  $\angle COE = \angle DOF = x^\circ$

and  $\angle AOF = \angle BOE = z^\circ$

$\therefore$  CD is a straight line

$\therefore \angle COE + \angle BOE + \angle DOB = 180^\circ$

$$\Rightarrow x^\circ + x^\circ + y^\circ = 180^\circ$$

$$\Rightarrow x^\circ + y^\circ + z^\circ = 180^\circ$$

i) If  $y = 45^\circ$  and  $z = 90^\circ$ , then

$$\Rightarrow x^\circ + 45^\circ + 90^\circ = 180^\circ$$

$$\Rightarrow x^\circ + 135^\circ = 180^\circ$$

$$\therefore x^\circ = 180^\circ - 135^\circ = 45^\circ$$

ii) If  $x = 3a$ ,  $y = 5a$ ,  $z = 6a$ ,

then  $x + y + z = 180^\circ$

$$\Rightarrow x + 5x + 6x = 180^\circ \Rightarrow 12x = 180^\circ$$

$$\Rightarrow x = \frac{180^\circ}{12} = 15^\circ$$

But  $x = 3a$

$$\therefore 3a = 15^\circ$$

$$\Rightarrow a = \frac{15^\circ}{3} = 5^\circ$$

Hence  $a = 5^\circ$