

Q1. What is uniform circular motion? How is uniform circular motion regarded as an accelerated motion? Explain.

→ The circular motion in which the body covers equal distance in equal interval of time in the circular path is called uniform circular motion.

Eg: Motion of earth, hands of clock, cycling around a circular path of constant speed, blades of fan etc.

→ In circular motion, the direction of the object changes continuously along the tangent. Thus, the velocity of the object changes. As the velocity changes, it is called regarded as accelerated motion.

Q2. An object is moving with uniform speed in a circle of radius r . Calculate the distance & displacement

a) when it completely half the circle.

→ Distance: πr

Displacement: diameter.

b) when it completes full circle

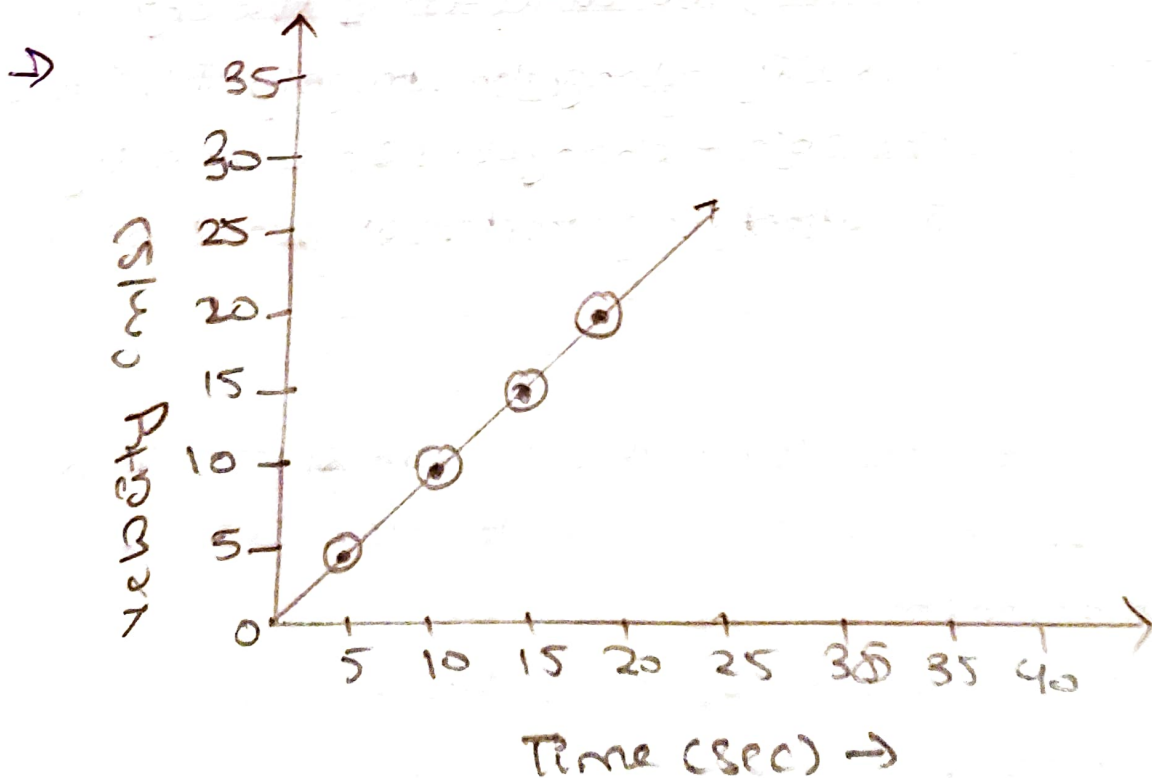
→ distance: $2\pi r$

displacement: 0

c) what type of motion does the object possess?

→ Circular motion.

3. Draw Velocity-time graph for an uniformly accelerated object. Using Velocity-time graph, derive $v = u + at$.



Equation - 1 $v = u + at$ (Velocity time relation)

Let us consider an object moves with velocity u at 'A' with uniform acceleration 'a', after 't' second it reach of 'B' with velocity 'v' after covering a distance 's'.

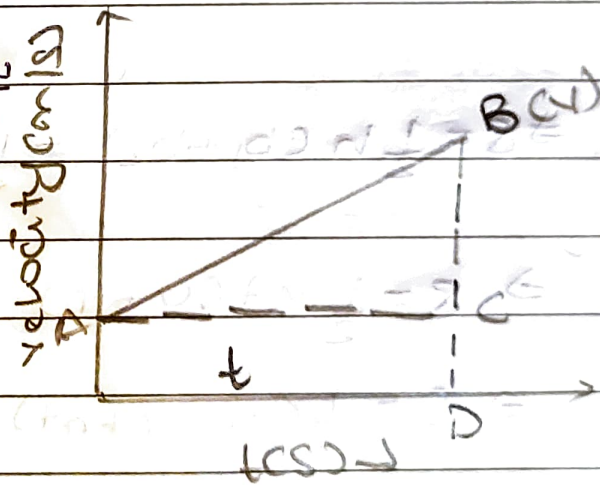
We know that, slope of $v \sim t$ graph stands for acceleration.

\rightarrow slope of $v \sim t$ graph = $\tan \theta = \frac{p}{b}$

$\rightarrow a = \frac{BD - CD}{AC} = \frac{v - u}{t}$

$\Rightarrow at = v - u$

$\Rightarrow v = u + at$



Q4. Write the three equations for the uniformly accelerated motion. Also derive the second & third equations by graphical method.

\rightarrow (i) $v = u + at$

(ii) $s = ut + \frac{1}{2}at^2$

(iii) $v^2 - u^2 = 2as$

Equation 2: $S = ut + \frac{1}{2}at^2$ (graphically)

let us consider an object moves with velocity u at 'A' with uniform acceleration 'a', after t second it reach at 'B' with velocity v after covering a distance 'S'.

We know that area under $v \sim t$ graph stands for distance cover.

$$\Rightarrow \text{Distance cover} = \text{Area under AB} \\ = \text{In } \triangle OAB \text{ trapezium}$$

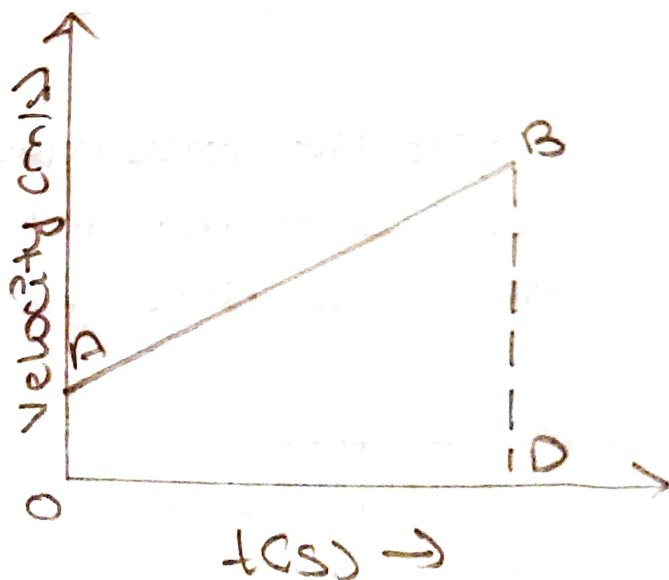
$$\Rightarrow S = \frac{1}{2}h(b_1 + b_2) = \frac{1}{2} \times OD (OA + BD)$$

$$\Rightarrow S = \frac{1}{2} \times t(u + v) \quad (\text{from eqn } v = u + at)$$

$$\Rightarrow S = \frac{1}{2}(u + v + at)$$

$$\Rightarrow S = \frac{1}{2}(2u + at)$$

$$\Rightarrow S = ut + \frac{1}{2}at^2 \\ \text{(Proved)}$$



Third equation of motion: $v^2 - u^2 = 2as$

Let us consider an object moves with velocity ' u ' as ' A ' with uniform acceleration ' a ', after ' t ' second it reach of ' B ' when velocity ' v ' after covering a distance ' s '.

We know that area under $v-t$ graph stands for distance cover.

⇒ Distance cover = Area under AB.

= Area of trapezium

$$s = \frac{1}{2} h (b_1 + b_2) = \frac{1}{2} \times t \times (OA + OB)$$

$$s = \frac{1}{2} \times t (u + v) = \frac{1}{2} \times \left(\frac{v-u}{a} \right) \times (u + v)$$

$$s = \frac{v^2 - u^2}{2a} \Rightarrow v^2 - u^2 = 2as \text{ (Proved)}$$

