

Exercise 8(B)

1. Using common factor method, find the H.C.F of:

(i) 16 and 35

Ans - 16 = ①, 2, 4, 8 and 16

35 = ①, 5, 7 and 35

common factors = 1

H.C.F = 1

(ii) 25 and 20

Ans - 25 = ①, ⑤, 25

20 = ①, 2, 4, ⑤, 10, 20

Common factors = 1 and 5

H.C.F. = 5

(iii) 27 and 75

Ans - 27 = ①, ③, 9, 27

75 = ①, ③, 5, 15, 25 and 75

Common factors = 1, 3

H.C.F = 3

(iv) 8, 12 and 18

Ans - 8 = ①, ②, 4 and 8

12 = ①, ②, 3, 4, 6, 12

Common factors = 1, 2 and 4

18 = ①, ②, 3, 6, 9 and 18

Common factors = 1 and 2

H.C.F. = 2

v) 24, 36, 45 and 60

Ans - 24 = ①, 2, ③, 4, 6, 8, 12 and 24

36 = ①, 2, ③, 4, 6, 9, 12, 18, 36

45 = ①, ③, 5, 9, 15 and 45

60 = ①, 2, ③, 4, 5, 6, 10, 12, 15, 20, 30, and 60

Common factors = 1 and 3

$$\text{H.C.F.} = 3$$

2. Using prime factor method, find the H.C.F. of:

i) 5 and 8

$$\text{Ans} - 5 = 1 \times 5$$

$$8 = 2 \times 2 \times 2 \times 1$$

~~Common prime factor~~

$$\text{H.C.F.} = 1$$

ii) 24 and 49

$$24 = 2 \times 2 \times 2 \times 3 \times 1$$

$$49 = 7 \times 7 \times 1$$

$$\text{H.C.F.} = 1$$

iii) 40, 60, 80

$$40 = 2 \times 2 \times 2 \times 5$$

$$60 = 2 \times 2 \times 3 \times 5$$

$$80 = 2 \times 2 \times 2 \times 2 \times 5$$

$$\text{H.C.F.} = 2 \times 2 \times 5$$

$$= 20$$

iv) 48, 84 and 88

$$48 = 2 \times 2 \times 2 \times 2 \times 3$$

$$84 = 2 \times 2 \times 3 \times 7$$

$$88 = 2 \times 2 \times 2 \times 11$$

$$\text{H.C.F.} = 2 \times 2$$

$$= 4$$

v) 12, 16 and 28

$$12 = 2 \times 2 \times 3$$

$$16 = 2 \times 2 \times 2 \times 2$$

$$28 = 2 \times 2 \times 7$$

$$\text{HCF} = 2 \times 2 = 4$$

3. Using the division method, find the HCF of the following :

i) 16 and 24

$$\begin{array}{r} 16 \overline{) 24} \ 1 \\ \underline{-16} \\ 8 \end{array}$$

$$16 \overline{) 24} \ 1$$

$$\underline{-16}$$

$$8 \overline{) 16} \ 2$$

$$\underline{-16}$$

$$0$$

$$\text{H.C.F} = 8$$

ii) 18 and 30

$$18 \overline{) 30} \ 1$$

$$\underline{-18}$$

$$12 \overline{) 18} \ 1$$

$$\underline{-12}$$

$$6 \overline{) 12} \ 2$$

$$\underline{-12}$$

$$0$$

$$\text{HCF} = 6$$

iii) 7, 14 and 24

$$\begin{array}{r} 7 \overline{) 14} \ 2 \\ - 14 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 7 \overline{) 24} \ 3 \\ - 21 \\ \hline \end{array}$$

$$\begin{array}{r} 3 \overline{) 7} \ 2 \\ - 6 \\ \hline \end{array}$$

$$\begin{array}{r} 1 \overline{) 3} \ 3 \\ - 3 \\ \hline 0 \end{array}$$

HCF = 1

iv) 70, 80, 120 and 150

$$\begin{array}{r} 70 \overline{) 80} \ 1 \\ - 70 \\ \hline \end{array}$$

$$\begin{array}{r} 10 \overline{) 70} \ 7 \\ - 70 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 10 \overline{) 120} \ 12 \\ - 10 \\ \hline \end{array}$$

$$\begin{array}{r} 20 \\ - 20 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 10 \overline{) 150} \ 15 \\ - 10 \\ \hline \end{array}$$

$$\begin{array}{r} 50 \\ - 50 \\ \hline 0 \end{array}$$

HCF = 10

v) 32, 56 and 46

$$\begin{array}{r} 32 \overline{) 56} \ 1 \\ - 32 \\ \hline \end{array}$$

$$\begin{array}{r} 24 \overline{) 32} \ 1 \\ - 24 \\ \hline \end{array}$$

$$\begin{array}{r} 8 \overline{) 24} \ 3 \\ - 24 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 8 \overline{) 46} \ 5 \\ - 40 \\ \hline \end{array}$$

$$\begin{array}{r} 6 \overline{) 8} \ 1 \\ - 6 \\ \hline \end{array}$$

$$\begin{array}{r} 2 \overline{) 6} \ 3 \\ - 6 \\ \hline 0 \end{array}$$

HCF = 2

4. Use a method of your own choice to find the HCF.

i) 45, 75 and 135

Ans-

$$\begin{array}{r}
 45 \overline{) 75} \quad | \quad 1 \\
 \underline{-45} \\
 30 \overline{) 45} \quad | \quad 1 \\
 \underline{-30} \\
 15 \overline{) 30} \quad | \quad 2 \\
 \underline{-30} \\
 \hline
 0
 \end{array}$$

$$\begin{array}{r}
 15 \overline{) 135} \quad | \quad 9 \\
 \underline{-135} \\
 \hline
 0
 \end{array}$$

HCF = 15

ii) 48, 36 and 196

Ans

$$\begin{array}{r}
 36 \overline{) 196} \quad | \quad 5 \\
 \underline{-180} \\
 16 \overline{) 36} \quad | \quad 2 \\
 \underline{-32} \\
 4 \overline{) 16} \quad | \quad 4 \\
 \underline{-16} \\
 \hline
 0
 \end{array}$$

$$\begin{array}{r}
 4 \overline{) 48} \quad | \quad 12 \\
 \underline{-4} \\
 8 \\
 \underline{-8} \\
 \hline
 0
 \end{array}$$

HCF = 4

iii) 66, 33, 132

$$\begin{array}{r}
 33 \overline{) 132} \quad | \quad 4 \\
 \underline{-132} \\
 \hline
 0
 \end{array}$$

$$\begin{array}{r}
 33 \overline{) 66} \quad | \quad 2 \\
 \underline{-66} \\
 \hline
 0
 \end{array}$$

HCF = 33

iv) 24, 36, 60, 132

$$\begin{array}{r}
 24 \overline{) 36} \quad | \quad 1 \\
 \underline{-24} \\
 12 \overline{) 24} \quad | \quad 2 \\
 \underline{-24} \\
 \hline
 0
 \end{array}$$

$$\begin{array}{r}
 12 \overline{) 60} \quad | \quad 5 \\
 \underline{-60} \\
 \hline
 0
 \end{array}$$

$$\begin{array}{r}
 12 \overline{) 132} \quad | \quad 11 \\
 \underline{-12} \\
 12 \\
 \underline{-12} \\
 \hline
 0
 \end{array}$$

Ans- HCF = 12

4) 30, 60, 90, 105

$$\begin{array}{r} 30 \overline{) 60} \ 2 \\ \underline{-60} \\ 0 \end{array}$$

$$\begin{array}{r} 30 \overline{) 90} \ 3 \\ \underline{-90} \\ 0 \end{array}$$

$$\begin{array}{r} 30 \overline{) 105} \ 3 \\ \underline{-90} \\ 15 \overline{) 30} \ 2 \\ \underline{-30} \\ 0 \end{array}$$

HCF = ~~30~~ 30

5. ans - $180 \overline{) 225} \ 1$
 $\underline{-180}$

$$\begin{array}{r} 45 \overline{) 180} \ 4 \\ \underline{-180} \\ 0 \end{array}$$

HCF = 45

$$\begin{array}{r} 45 \overline{) 315} \ 7 \\ \underline{-280} \\ 35 \overline{) 45} \ 1 \\ \underline{-35} \\ 10 \overline{) 35} \ 3 \\ \underline{-30} \\ 5 \overline{) 10} \ 2 \\ \underline{-10} \\ 0 \end{array}$$

$$\begin{array}{r} 5 \overline{) 10} \ 2 \\ \underline{-10} \\ 0 \end{array}$$

6. ans - $45 = 3 \times 3 \times 5$

$56 = 2 \times 2 \times 2 \times 7$

H.C.F = 1

Therefore, 45 and 56 are co-prime

7. ans - Pairs are = 15, 16

= 28, 15

= 16, 21

= 15, 21

= 21, 28

= 28, 16

HCF of 15 and 16 = 1

HCF of 16 and 21 = 1

HCF of 21 and 28 = 7

HCF of 28 and 15 = 1

HCF of 15 and 21 = 3

HCF of 28 and 16 = 4

Hence, the co-prime pairs are 15 and 16, 16 and 21, 28 and 15.

8. ans - Since, $93 - 3 = 90$, $111 - 3 = 108$ and $129 - 3 = 126$
HCF of 90, 108 and 126

=

$$\begin{array}{r}
 90 \overline{) 108} \quad | \quad 1 \\
 \underline{-90} \\
 18 \overline{) 90} \quad | \quad 5 \\
 \underline{-90} \\
 0
 \end{array}
 \qquad
 \begin{array}{r}
 18 \overline{) 126} \quad | \quad 7 \\
 \underline{-126} \\
 0
 \end{array}$$

HCF = 18 leaving remainder 3 in each case.