

Ch-8

Ex-8(C)

1) i) 18, 12 and 24

A = 18 = 18, 36, 54, 72, 90, 108
12 = 12, 24, 36, 48, 60, 72, 96, 108
24 = 24, 48, 72
LCM of 18, 12 and 24 = 72

ii) 10, 15, 20

A = 10 = 10, 20, 30, 40, 50, 60
15 = 15, 30, 45, 60
20 = 20, 40, 60
LCM of 10, 15 and 20 = 60

iii) 3, 6, 9 and 12

A = 3 = 3, 6, 9, 12, 15, 18, 21, 24, 27, 30, 33, 36
6 = 6, 12, 18, 24, 30, 36
9 = 9, 18, 27, 36
12 = 12, 24, 36
LCM of 3, 6, 9 and 12 = 36

2) i) 100, 150 and 200

2 | 100, 150, 200
2 | 50, 75, 100
5 | 25, 75, 50
5 | 5, 15, 10
5 | 1, 3, 2

2 | 100, 150, 200
2 | 50, 75, 100
5 | 25, 75, 50
5 | 5, 15, 10
5 | 1, 3, 2

$100 = 2 \times 2 \times 5 \times 5 = 2^2 \times 5^2$
 $150 = 2 \times 2 \times 5 \times 5 \times 3 = 2^2 \times 5^2 \times 3$
 $200 = 2 \times 2 \times 5 \times 5 \times 2 = 2^3 \times 5^2$
LCM = $2^3 \times 5^2 \times 3$
 $= 2 \times 2 \times 2 \times 5 \times 5 \times 3 = 600$

LCM = $2 \times 2 \times 5 \times 5 \times 3 \times 2 = 600$

iii) 14, 21 and 98

$$14 \begin{array}{l} 2 \\ 7 \end{array} \begin{array}{l} 14 \\ 21 \\ 98 \end{array}$$

$$2 \begin{array}{l} 2 \\ 3 \\ 14 \end{array}$$

$$1, 3, 7$$

$$\text{LCM} = 2 \times 2 \times 3 \times 7 = 294$$

$$14 = 2 \times 7$$

$$21 = 3 \times 7$$

$$98 = 2 \times 2 \times 7 \times 7$$

$$\text{LCM} = 2^2 \times 3 \times 7$$

$$= 2 \times 2 \times 3 \times 7 = 294$$

iv) 22, 121 and 33

$$22 \begin{array}{l} 11 \\ 2 \end{array}$$

$$121 \begin{array}{l} 11 \\ 11 \end{array}$$

$$33 \begin{array}{l} 11 \\ 3 \end{array}$$

$$\text{LCM} = 11 \times 2 \times 11 \times 3 = 726$$

$$22 = 11 \times 2$$

$$121 = 11 \times 11$$

$$33 = 11 \times 3$$

$$\text{LCM} = 11^2 \times 2 \times 3$$

$$= 11 \times 11 \times 2 \times 3 = 726$$

3) \rightarrow HCF and LCM of two numbers = 50 and 300

One number = 150

~~Other number~~ The product of HCF and LCM = 50 \times 300 = product of two numbers

Product of HCF and LCM = Product of two numbers
of two number

The other number = Product of HCF and LCM divided by one number

$$\therefore \text{The other number is} = 50 \times 300 \div 150$$

$$= 15000 \div 150$$

$$= 100$$

4)

Product of two numbers = 432

$$\text{LCM} = 72$$

And the HCF = Product of two numbers divided by LCM

$$= 432 \div 72 = 6$$

$$\therefore \text{HCF} = 6$$

5) The product of two numbers = 19,200

$$\text{HCF} = 40$$

LCM = The product of two numbers divided by HCF

$$= 19,200 \div 40$$

$$= 480$$

$$\therefore \text{LCM} = 480$$

$$\begin{array}{r|l}
 2 & 18, 24, 96 \\
 2 & 9, 12, 48 \\
 2 & 9, 6, 24 \\
 2 & 9, 3, 12 \\
 2 & 9, 3, 6 \\
 3 & 9, 3, 3 \\
 3 & 3, 1, 1 \\
 & 1, 1, 1
 \end{array}$$

$$LCM = 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 = 288$$

$$18 = 2 \times 9 = 2 \times 3 \times 3 = 2 \times 3^2$$

$$24 = 2 \times 12 = 2 \times 2 \times 3 \times 2 = 2^3 \times 3$$

$$96 = 2 \times 48 = 2 \times 2 \times 2 \times 2 \times 3 = 2^5 \times 3$$

$$= 2 \times 9 \times 12 \times 48$$

$$LCM = 2^5 \times 3^2 = 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 = 288$$

$$\begin{array}{r|l}
 2 & 12, 15, 18, 24, 36 \\
 2 & 6, 15, 9, 12, 18 \\
 3 & 3, 15, 9, 6, 9 \\
 3 & 1, 5, 3, 2, 3 \\
 & 1, 5, 1, 2, 1
 \end{array}$$

$$LCM = 2 \times 2 \times 3 \times 3 \times 5 \times 2 = 360$$

93, 111, 129, Leaving remainder 3 in each case

Required - 93 - 3, 111 - 3, 129 - 3

90, 108, 126

Remd greatest

$$\begin{array}{r}
 7) \quad 2 \mid 12, 18, 24, 32, 40 \\
 \quad 2 \mid 6, 9, 12, 16, 20 \\
 \quad 3 \mid 3, 9, 6, 8, 10 \\
 \quad 2 \mid 1, 3, 2, 8, 10 \\
 \quad 2 \mid 1, 3, 1, 4, 5 \\
 \quad 1, 3, 1, 2, 5
 \end{array}$$

$$LCM = 2 \times 2 \times 3 \times 2 \times 2 \times 3 \times 2 \times 5 = 1440$$

$$Req. no. = 1440 - 1$$

$$= 1439$$

$$\begin{array}{r}
 8) \quad 2 \mid 18, 36, 32, 27 \\
 \quad 3 \mid 9, 18, 16, 27 \\
 \quad 2 \mid 3, 6, 16, 9 \\
 \quad 3 \mid 3, 3, 8, 9 \\
 \quad 2 \mid 1, 1, 8, 3 \\
 \quad 2 \mid 1, 1, 4, 3 \\
 \quad 1, 1, 2, 3
 \end{array}$$

$$LCM = 864$$

$$\begin{aligned}
 Required &= 864 + 3 \\
 &= 867
 \end{aligned}$$

$$\begin{aligned}
 2) \quad 34 &= 2 \times 17 \\
 85 &= 5 \times 17 \\
 51 &= 3 \times 17
 \end{aligned}$$

~~$$34, 85, 51$$~~

~~$$HCF = 2 \times 3 \times 5 \times 17 = 510$$~~

$$17 \mid 34, 85, 51$$

$$2, 5, 3$$

$$= 17 \times 2 \times 5 \times 3 = 510$$