

Exercises

- 5.3. Magnetic field strength, $B = 0.25 \text{ T}$
 Torque on the bar magnet, $T = 4.5 \times 10^{-2} \text{ J}$
 Angle ~~between~~, $\theta = 30^\circ$

$$\text{Torque, } T = MB \sin \theta$$

$$\therefore M = \frac{T}{B \sin \theta}$$

$$= \frac{4.5 \times 10^{-2}}{0.25 \times \sin 30} = \frac{4.5 \times 10^{-2}}{0.25 \times \frac{1}{2}}$$

$$= 0.36 \text{ J T}^{-1}$$

Hence magnetic moment of magnet is 0.36 J T^{-1} .

- 5.4 Magnetic moment of bar magnet, $M = 0.32 \text{ J T}^{-1}$
 External magnetic field, $B = 0.15 \text{ T}$.

a) The bar magnet aligned along the magnetic field. The system is considered as being in stable equilibrium. Hence, $\theta = 0^\circ$.

$$\begin{aligned} \text{Potential energy of the system} &= -MB \cos \theta \\ &= -0.32 \times 0.15 \cos 0^\circ \\ &= -4.8 \times 10^{-2} \text{ J} \end{aligned}$$



b) The bar magnet is oriented 180° to the magnetic field. Hence, it is in unstable equilibrium.

$$\theta = 180^\circ$$

$$\begin{aligned} P.E. &= -MB \cos \theta \\ &= -0.32 \times 0.15 \cos 180^\circ \\ &= 4.8 \times 10^{-2} \text{ J} \end{aligned}$$

5.5 Turns in the solenoid, $n = 800$
Area, $A = 2.5 \times 10^{-4} \text{ m}^2$
Current in solenoid, $I = 3.0 \text{ A}$.

A current-carrying solenoid behaves as a bar magnet because a magnetic field develops along its axis, i.e., along its length.

$$\begin{aligned} M &= nIA \\ &= 800 \times 3 \times 2.5 \times 10^{-4} \\ &= 0.6 \text{ J T}^{-1} \end{aligned}$$

5.7 a) Magnetic moment, $M = 1.5 \text{ J T}^{-1}$

Magnetic field, $B = 0.22 \text{ T}$

i) $\theta_1 = 0^\circ$

$$\theta_2 = 90^\circ$$

$$\begin{aligned} \text{Work, } W &= -MB (\cos \theta_1 - \cos \theta_2) \\ &= -1.5 \times 0.22 (\cos 90^\circ - \cos 0^\circ) \\ &= -0.33 (0 - 1) \\ &= 0.33 \text{ J} \end{aligned}$$

(i) $\theta_1 = 0^\circ$, $\theta_2 = 180^\circ$

work done, $W = -MB (\cos\theta_2 - \cos\theta_1)$
 $= -1.5 \times 0.22 (-1 - 1)$
 $= -0.33 (-1 - 1)$
 $= 0.66 \text{ J}$

b) For case (i); $\theta = \theta_2 = 90^\circ$

\therefore Torque, $T = MB \sin\theta$
 $= 1.5 \times 0.22 \sin 90^\circ$
 $= 0.33 \text{ J}$

For case (ii); $\theta = \theta_2 = 180^\circ$

\therefore Torque, $T = MB \sin\theta$
 $= 0 \text{ J}$

5.8 No. of turns in the solenoid, $n = 2000$
 Area of cross-section, $A = 1.6 \times 10^{-4} \text{ m}^2$
 Current in the solenoid, $I = 4 \text{ A}$

a) Magnetic moment, $M = nAI$
 $= 2000 \times 1.6 \times 10^{-4} \times 4$
 $= 1.28 \text{ Am}^2$

b) Magnetic field, $B = 7.5 \times 10^{-2} \text{ T}$
 $\theta = 30^\circ$

Torque, $T = MB \sin\theta$
 $= 1.28 \times 7.5 \times 10^{-2} \sin 30^\circ$
 $= 4.8 \times 10^{-2} \text{ Nm}$

Since the magnetic field is uniform, the force on the solenoid is zero. The torque = $4.8 \times 10^{-2} \text{ Nm}$

5.9. No. of turns in coil, $N = 16$.

Radius of the coil, $r = 10 \text{ cm} = 0.1 \text{ m}$

Cross-section of the coil, $A = nr^2 = n \times (0.1)^2 \text{ m}^2$

Current, $I = 0.75 \text{ A}$.

Magnetic field strength, $B = 5.0 \times 10^{-2} \text{ T}$.

Frequency, $\nu = 2.05^{-1}$

$$\begin{aligned} \therefore \text{Magnetic moment, } m &= NIA = N I \pi r^2 \\ &= 16 \times 0.75 \times \pi \times (0.1)^2 \\ &= 0.377 \text{ J T}^{-1} \end{aligned}$$

Frequency is given by the relation:

$$\nu = \frac{1}{2\pi} \sqrt{\frac{mB}{I}}$$

where, $I = \text{moment of inertia of the coil}$

$$\therefore I = \frac{mB}{4\pi^2 \nu^2}$$

$$= \frac{0.377 \times 5 \times 10^{-2}}{4\pi^2 \times (2)^2}$$

$$= 1.19 \times 10^{-4} \text{ Kg m}^2$$

$$I = 1.19 \times 10^{-4} \text{ Kg m}^2$$

5.11. Ag. Angle of declination, $\theta = 12^\circ$

Angle of dip, $\delta = 60^\circ$

Horizontal component, $B_H = 0.16 \text{ G}$

$$B_H = B \cos \delta$$

$$\therefore B = \frac{B_H}{\cos \delta}$$

$$= \frac{0.16}{\cos 60^\circ} = 0.32 \text{ G.}$$

$$B = 0.32 \text{ G}$$

5.13 Earth's magnetic field at given place, $H = 0.36 \text{ G}$

The magnetic field at a distance d ,

$$B_1 = \frac{\mu_0 2M}{4\pi d^3} = H \quad \text{--- (1)}$$

The magnetic field at the same distance d , on the equatorial line,

$$B_2 = \frac{\mu_0 M}{4\pi d^3} = \frac{H}{2}$$

Total magnetic field

$$B = B_1 + B_2$$

$$= 0.36 + 0.18 = 0.54 \text{ G.}$$

$$B = 0.54 \text{ G}$$

5.18 Current in the wire, $I = 2.5 \text{ A}$

Angle of dip, $\delta = 0^\circ$

Earth's magnetic field, $H = 0.33 \text{ G} = 0.33 \times 10^{-4} \text{ T}$.

Horizontal component of earth's magnetic field, $H_H = H \cos \delta$

$$= 0.33 \times 10^{-4} \times \cos 0^\circ = 0.33 \times 10^{-4} \text{ T}$$

Magnetic field at the neutral point at a distance R

$$H_H = \frac{\mu_0 I}{2\pi R}$$

$$\therefore R = \frac{\mu_0 I}{2\pi H_H}$$

$$= \frac{4\pi \times 10^{-7} \times 2.5}{2\pi \times 0.33 \times 10^{-4}} = 15.15 \times 10^{-3} \text{ m} = 1.51 \text{ cm}$$