

Exercise - 8 (C)

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Page

1. Using the common multiple method, find the LCM of the following:

i) 8, 12 and 24

Ans \rightarrow 8, 12 and 24

Multiples of 8 = 8, 16, 24, 32, 40

Multiples of 12 = 12, 24, 36, 48, 60

Multiples of 24 = 24, 48, 72, 96, 120

Common factors = 24

LCM = 24

ii) 10, 15 and 20

Ans \rightarrow 10, 15 and 20

Multiples of 10 = 10, 20, 30, 40, 50, 60

Multiples of 15 = 15, 30, 45, 60, 75

Multiples of 20 = 20, 40, 60, 80, 100

Common factors = 60

LCM = 60

iii) 3, 6, 9 and 12

Ans \rightarrow 3, 6, 9 and 12

Multiples of 3 = 3, 6, 9, 12, 15, 18, 21, 24, 27, 30, 33, 36

Multiples of 6 = 6, 12, 18, 24, 30, 36

Multiples of 9 = 9, 18, 27, 36, 45

Multiples of 12 = 12, 24, 36, 48, 60

Common factors = 36

LCM = 36

C.W ii)

2. i) 18, 24 and 96
Ans → 18, 24 and 96

$$\begin{array}{r|l}
 2 & 18, 24, 96 \\
 3 & 9, 12, 48 \\
 2 & 3, 4, 16 \\
 2 & 3, 2, 8 \\
 & 3, 1, 4 \\
 \hline
 \end{array}$$

$LCM = 2 \times 3 \times 2 \times 2 \times 3 \times 4 = 288$

ii)

v) 34, 85 and 51
Ans → 34, 85 and 51

$$\begin{array}{r|l}
 17 & 34, 85, 51 \\
 & 2, 5, 3 \\
 \hline
 \end{array}$$

$LCM = 17 \times 2 \times 5 \times 3 = 510$

ii)

iii) 14, 21 and 98
Ans → 14, 21 and 98

$$\begin{array}{r|l}
 7 & 14, 21, 98 \\
 2 & 2, 3, 14 \\
 & 1, 3, 7 \\
 \hline
 \end{array}$$

$LCM = 7 \times 2 \times 3 \times 7 = 294$

ii)

ii) 100, 150 and 200
Ans → 100, 150 and 200

$$\begin{array}{r|l}
 10 & 100, 150, 200 \\
 & 10 \\
 \hline
 5 & 100, 150, 200 \\
 2 & 20, 30, 40 \\
 \hline
 \end{array}$$

$$2 \mid 10, 15, 20$$

$$5 \mid 5, 3, 10$$

$$1, 3, 2$$

$$\text{LCM} = 5 \times 2 \times 2 \times 5 \times 3 \times 2 = 600$$

RELATIONSHIP BETWEEN HCF AND LCM

Q) ~~12~~ 12, 18

Ans \Rightarrow HCF of 12, 18 = $2 \times 3 = 6$

LCM of 12, 18 = $2 \times 3 \times 3 \times 2 = 36$

HCF \times LCM = $36 \times 6 = 216$

$12 \times 18 = 216$

Relationship =

HCF \times LCM = Product of the given numbers

3. HCF = 50, LCM = 300

First number = 150, Second number =

Product of 2 nos. = HCF \times LCM

$150 \times \text{Second number} = \cancel{500} \leftarrow 50 \times 300$
 $= 15000$

Second number = $15000 \div 150$
 $= 100$

$$\begin{array}{r} 100 \\ \hline 150 \overline{) 15000} \\ \underline{-1500} \\ 00 \\ \underline{-0} \\ 00 \\ \underline{-0} \\ 0 \end{array}$$

So, the second number is 100.

HW

6. The smallest number which, when divided by 12, 15, 18, 24 and 36 leaves no remainder is their LCM.

$$3 \mid 12, 15, 18, 24, 36$$

$$2 \mid 4, 5, 6, 8, 12$$

$$2 \mid 2, 5, 3, 4, 6$$

$$3 \mid 1, 5, 3, 2, 3$$

$$LCM = 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 5 =$$

$$1, 5, 1, 2, 1$$

$$LCM = 3 \times 2 \times 2 \times 3 \times 2 \times 5 = 360$$

So, the smallest number which, when divided by 12, 15, 18, 24 and 36 leaves no remainder is 360.

Q2-iv)

2. iv. ii) 22, 121 and 33

Ans \Rightarrow 22, 121 and 33

$$11 \mid 22, 121, 33$$

$$2, 11, 3$$

$$LCM = 2 \times 3 \times 11 \times 11 = 726$$

i-i) 18, 24 and 96

Ans \Rightarrow 18, 24 and 96

$$18 = 2 \times 3 \times 3$$

$$24 = 2 \times 2 \times 2 \times 3$$

$$96 = 2 \times 2 \times 2 \times 2 \times 2 \times 3$$

Common factors = 2, 3

$$LCM = 2 \times 3 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 =$$

$$LCM = 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 = 288$$

ii) 100, 150 and 200

Ans) 100, 150 and 200

$$100 = 2 \times 5 \times 5 \times 2$$

$$150 = 2 \times 3 \times 5 \times 5$$

$$200 = 2 \times 5 \times 5 \times 2 \times 2$$

Common factors = 2, 5

$$\text{LCM} = 5 \times 5 \times 3 \times 2 \times 2 \times 2 = 600$$

iii) 14, 21 and 98

Ans) 14, 21 and 98

$$14 = 7 \times 2$$

$$21 = 7 \times 3$$

$$98 = 2 \times 7 \times 7$$

Common factors = 7

$$\text{LCM} = 7 \times 7 \times 2 \times 3 = 294$$

iv) 22, 121 and 33

Ans) 22, 121 and 33

$$22 = 11 \times 2$$

$$121 = 11 \times 11$$

$$33 = 11 \times 3 \quad \text{Common factors} = 11$$

$$\text{LCM} = 11 \times 11 \times 2 \times 3 = 726$$

v) 34, 85 and 51

Ans) 34, 85 and 51

$$34 = 2 \times 17$$

$$85 = 5 \times 17$$

$$51 = 3 \times 17$$

LCM = Common factors = 17

$$\text{LCM} = 17 \times 2 \times 5 \times 3 = 510$$

4. Product of two numbers = 432

LCM = 72

HCF =

Relationship

Product of two numbers = HCF \times LCM

HCF = Product \div LCM

= 432 \div 72

= 6

$$\begin{array}{r} 6 \\ 72 \overline{) 432} \\ \underline{-432} \\ 0 \end{array}$$

So, the HCF is 6.

5. Product of two numbers = 19,200

HCF = 40

LCM =

Product of two numbers = HCF \times LCM

LCM = Product \div HCF

= 19,200 \div 40

= 480

$$\begin{array}{r} 480 \\ 40 \overline{) 19,200} \\ \underline{-160} \downarrow \\ 320 \\ \underline{-320} \downarrow \\ 00 \\ \underline{-0} \\ 0 \end{array}$$

So, the LCM is 480.

7. The smallest number which, when divided by 12, 18, 24, 32 and 40 completely is their LCM.

$$\begin{array}{r}
 2 \mid 12, 18, 24, 32, 40 \\
 2 \mid 6, 9, 12, 16, 20 \\
 2 \mid 3, 9, 6, 8, 10 \\
 3 \mid 3, 9, 3, 4, 5 \\
 \quad 1, 3, 1, 4, 5
 \end{array}$$

$$LCM = 2 \times 2 \times 2 \times 3 \times 3 \times 4 \times 5 = 1440$$

$$\begin{aligned}
 \text{The required number} &= 1440 - 1 \\
 &= 1400 - 1 \\
 &= 1440 - 1 \\
 &= 1439
 \end{aligned}$$

increased by one is

So, the smallest number which, when divided by 12, 18, 24, 32 and 40 completely is 1439.

8. The smallest number which, when divided by 18, 36, 32 and 27 completely is their LCM.

$$\begin{array}{r}
 2 \mid 18, 36, 32, 27 \\
 3 \mid 9, 18, 16, 27 \\
 3 \mid 3, 6, 16, 9 \\
 2 \mid 1, 2, 16, 3 \\
 \quad 1, 1, 8, 3
 \end{array}$$

$$LCM = 2 \times 3 \times 3 \times 2 \times 8 \times 3 = 864$$

$$\text{The required number} = 864 + 3 = 867$$

So, the smallest number which, when decreased by three is divisible by 18, 36, 32 and 27 is 867.