

Exercise 19 (B)

i) ~~(3a + 4b + 7c)~~ $3a + 4b + 7c + (-5a) + 3b + (-6c) + 4a + (-2b) +$

$(-4c)$

$$= \cancel{3a} + 3a - 5a + 4a + 4b + 3b - 2b + 7c - 6c - 4c$$

$$= \cancel{3a} (3 - 5 + 4)a + (4 + 3 - 2)b + (7 - 6 - 4)c$$

$$= 2a + 5b - 3c$$

ii) $2x^2 + xy - y^2 - x^2 + 2xy + 3y^2 + 3x^2 - 10xy + 4y^2$

$$= \cancel{2x^2} (2 - 1 + 3)x^2 + (\cancel{1} + 2 - 10)xy + (-1 + 3 + 4)y^2$$

$$= \cancel{2x^2} (2 - 1 + 3)x^2 + (1 + 2 - 10)xy + (-1 + 3 + 4)y^2$$

$$= \cancel{4x^2} - 7xy + 6y^2$$

iii) $x^2 - x + 1 - 5x^2 + 2x - 2 + 3x^2 - 3x + 1$

$$= (1 - 5 + 3)x^2 + (1 + 2 - 3)x + (1 - 2 + 1)$$

$$= -x^2 + 0x + 0$$

$$= -x^2$$

iv) $a^2 - ab + bc + 2ab + bc - 2a^2 - 3bc + 3a^2 + ab$

$$= (a^2 - 2a^2 + 3a^2) + (1ab + 2ab + ab) + (1bc + 1bc - 3bc)$$

$$= (1 - 2 + 3)a^2 + (1 + 2 + 1)ab + (1 + 1 - 3)bc$$

$$= 2a^2 + 4ab - bc$$

v) $4x^2 + 7 - 3x + 4x - x^2 + 8 + -10 + 5x - 2x^2$

$$= (4 - 1 - 2)x^2 + (7 + 8 - 10) + (-3 + 4 + 5)x$$

$$= 1x^2 + 5 + 6x$$

$$\begin{aligned} \text{v)} \quad & 4x^2 + 7 - 3x + 4x - x^2 + 8 - 10 + 5x - 2x^2 \\ & = x^2 + 5x + 6 \end{aligned}$$

$$\begin{aligned} \text{vi)} \quad & 3x + 4xy - y^2 + xy - 4x + 2y^2 + 3y^2 - xy + 6x \\ & = (3x - 4x + 6x) + (4 + 1 - 1)xy + (-1 + 2 + 3)y^2 \\ & = 5x + 4xy + 4y^2 \end{aligned}$$

$$\begin{aligned} \text{2. i)} \quad & -17x^2 - 2xy + 23y^2 + (-9y^2) + 15x^2 + 7xy + 13x^2 + 3y^2 - 4xy \\ & = (-17 + 15 + 13)x^2 + (-2 + 7 - 4)xy + (23 - 9 + 3)y^2 \\ & = 11x^2 + xy + 17y^2 \end{aligned}$$

$$\begin{aligned} \text{ii)} \quad & -x^2 - 3xy + 3y^2 + 8 + 3x^2 - 5y^2 - 3 + 4xy - 6xy + 2x^2 - 2 + y^2 \\ & = (-1 + 3 + 2)x^2 + (-3 + 4 - 6)xy + (3 - 5 + 1)y^2 + (8 - 3 - 2) \\ & = 4x^2 - 5xy - y^2 + 3 \end{aligned}$$

$$\begin{aligned} \text{3) i)} \quad & 3a - (a + 2b) \\ & = 3a - a - 2b \\ & = 2a - 2b \end{aligned}$$

$$\begin{aligned} \text{i)} \quad & (5x - 3y) - (x + y) \\ & = 5x - 3y - x - y \\ & = 5x - x - 3y - y \\ & = 4x - 4y \end{aligned}$$

$$\begin{aligned} \text{ii)} \quad & (8a + 15b) - (3b - 7a) \\ & = 8a + 7a + 15b - 3b \\ & = 15a + 12b \end{aligned}$$

$$\begin{aligned} \text{iv)} \quad & (8x + 7y) - (4y - 3x) \\ & = 8x + 3x - 7y - 4y \\ & = 11x - 11y \end{aligned}$$

$$v) 7 - (4a - 5)$$

$$= 7 + 5 - 4a$$

$$= 12 - 4a$$

$$vi) (6y - 13) - (4 - 7y)$$

$$= 6y + 7y - 13 - 4$$

$$= 13y - 17$$

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$$2. i) a^3 - 2b^3 + a + b^3 - 2a^3 + b - 2b + 2b^3 - 5a + 4a^3$$

$$= (1 - 2 + 4)a^3 + (-2 + 1 + 2)b^3 + \cancel{a} - 5a + (1 - 2)b$$

$$= 3a^3 + b^3 - 4a - b$$

$$4. i) a - 4b - 2c - (5a - 3b + 2c)$$

$$= \cancel{a} - 4b - 2c - 5a + 3b - 2c$$

$$= (1 - 5)a - (4 - 3)b - (2c + 2c)$$

$$= -4a - b - 4c$$

$$ii) 4x - 6y + 3z \text{ from } 12x + 7y - 2z$$

$$= 12x + 7y - 2z - (4x - 6y + 3z)$$

$$= 12x + 7y - 2z - 4x + 6y - 3z$$

$$= 12x - 4x + 7y + 6y + \cancel{2z} - 3z$$

$$= 8x + 13y - z$$

$$\begin{aligned}
 4.ii) \quad & 4x - 6y + 3z \text{ from } 12x + 7y - 21z \\
 & - (12x + 7y - 21z) - (4x - 6y + 3z) \\
 & = 12x + 7y - 21z - 4x + 6y - 3z \\
 & = (12x - 4x) - (7y + 6y) - (21z - 3z) \\
 & = 12x - 4x + 6y + 7y - 21z + 3z \\
 & = 8x + 13y - 18z
 \end{aligned}$$

$$5.ii) \quad \frac{1}{2}p - \frac{1}{3}q - \frac{3}{2}r - (-\frac{3}{2}p + q - r)$$

$$= \frac{1}{2}p - \frac{1}{3}q - \frac{3}{2}r + \frac{3}{2}p - q + r$$

$$= (\frac{1}{2} + \frac{3}{2})p - (\frac{1}{3} + 1)q - (\frac{3}{2} - 1)r$$

$$= \frac{4}{2}p - \frac{4}{3}q - \frac{1}{2}r = 2p - \frac{4}{3}q - \frac{1}{2}r$$

$$= 2p - \frac{4}{3}q - \frac{1}{2}r + \frac{4}{3}q + \frac{1}{2}r$$

$$= \frac{4p}{2} + \frac{(-4q - 3q)}{-3} + \frac{2r - 3r}{2} = 2p + \frac{-4q}{3} + \frac{-r}{2}$$

$$= 2p - \frac{4q}{3} - \frac{r}{2}$$

$$4.iii) \quad 5a - 7b + 2c - (5 - a - 4b + 4c)$$

$$= (5 - 1)a - (-7b + 4b) + 2c - 4c - 5$$

$$= 5a + a - 7b + 4b + 2c - 4c - 5$$

$$= 6a - 3b - 2c - 5$$

$$= 6a - 3b - 2c - 5$$

$$\begin{aligned}
 \text{iv)} \quad & x - y - 2 - (-8x - 12y + 17) \\
 & = x - y - 2 + 8x + 12y - 17 \\
 & = (1+8)x - (1+12)y - (2+17) \\
 & = 9x - 13y - 19
 \end{aligned}$$

$$\begin{aligned}
 \text{v)} \quad & ab - 2cd + 2ac + bd - (2ab + cd - ac - 2bd) \\
 & = ab - 2cd + 2ac + bd - 2ab - cd + ac + 2bd \\
 & = (ab - 2ab) + (-2cd - cd) + (2ac + ac) + (bd + 2bd) \\
 & = -ab - 3cd + 3ac + 3bd
 \end{aligned}$$

$$\text{5. i)} \quad bc - ca + ab - (ab + bc - ca)$$

$$\begin{aligned}
 & = bc - ca + ab - ab - bc + ca \\
 & = (bc - bc) + (-ca + ca) + (ab - ab) \\
 & = 0 + 0 + 0 \\
 & = 0
 \end{aligned}$$

$$\text{5. i)} \quad bc - ca + ab - (-ab + bc - ca)$$

$$\begin{aligned}
 & = bc - ca + ab + ab - bc + ca \\
 & = (bc - bc) + (-ca + ca) + (ab + ab) \\
 & = 0 + 0 + 2ab \\
 & = 2ab
 \end{aligned}$$

ii)

$$5. i) 3x + 5y - 4z - (5x + 6y - 3z)$$

$$= 3x + 5y - 4z - 5x - 6y + 3z$$

$$= 3x - 5x + 5y - 6y + 3z - 4z$$

$$= -2x - y - z$$

$$10) a^2 + a + 1 - (1 - a + a^2)$$

$$= a^2 + a + 1 - 1 + a - a^2$$

$$= a^2 - a^2 + a + a + 1 - 1$$

$$= 0 + 2a + 0$$

$$= 2a$$

$$6. \text{ Sum of } x + y - 2z \text{ and } 2x - y + z$$

$$= x + y - 2z + 2x - y + z$$

$$= (1+2)x + (1-1)y + (-2+1)z$$

$$= 3x + 0y - 1z$$

$$= 3x - z$$

$$= 3x - z$$

$$\cancel{3x - z} - (x + y + z) = 3x - z - x - y - z$$

$$= 3x - x - z - z - y - z$$

$$= 2x - y - 3z$$

$$= 2x - y - 3z$$

$$7. 3a - 2b + 4c + 3b - 2c$$

$$= 3a + (3b - 2b) + (4c - 2c)$$

$$= 3a + b + 2c$$

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$$3a + 1b + 2c - (a - b - c)$$

$$= 3a + b + 2c - a + b + c$$

$$= 3a - a + b + b + 2c + c$$

$$= 2a + 2b + 3c$$

$$\begin{aligned} 8) \quad & 3x - y + 2z + x + y - 3z \\ & = (3+1)x + (-1+1)y + (2-3)z \\ & = 4x + 0y - z \end{aligned}$$

$$\begin{aligned} & 4x + 0y - z - (x - 2y - z) \\ & = 4x + 0y - z - x + 2y + z \\ & = 4x - x + 0y + 2y - z + z \\ & = 3x + 2y \end{aligned}$$

$$\begin{aligned} 9) \quad & x + y + x - z \\ & = (1+1)x + y - z \\ & = 2x + y - z \end{aligned}$$

$$\begin{aligned} & x - z + x + y + z \\ & = (1+1)x + (-1+1)z + y \\ & = 2x - z + y \end{aligned}$$

$$\begin{aligned} & 2x - z + y - (2x + y - z) \\ & = 2x - z + y - 2x - y + z \\ & = 2x - 2x + z - z + y - y \\ & = 0x + 0z + 0y \\ & = 0 \end{aligned}$$