

2/7/21

HOME ASSIGNMENT

Q1. A ball is thrown upward with an initial velocity of 10.0 m/s from the top of a 50.0 m tall building.

(a) With what velocity will the ball strike the ground?

Ans) Given: $y = -50.0 \text{ m}$ (displacement),

$$v_0 = +10.0 \text{ m/s}$$

Find: (a) v (b) t

$y = 50.0 \text{ m}$

The y in the kinematic equations stands for displacement from the launch point.

$$\begin{aligned} \text{(a)} \quad v^2 &= v_0^2 - 2gy = (+10.0 \text{ m/s})^2 - 2(9.80 \text{ m/s}^2)(-50.0 \text{ m}) \\ &= 1.08 \times 10^3 \text{ m}^2/\text{s}^2 \end{aligned}$$

$$\text{So, } v = \sqrt{1.08 \times 10^3 \text{ m}^2/\text{s}^2} = \pm 32.9 \text{ m/s}$$

The positive answer is discarded since the ball is falling when it lands (moving downward).

Therefore $v = -32.9 \text{ m/s}$

(b) How long does it take the ball to strike the ground.

Ans) From $v = v_0 - gt$, we have

$$t = \frac{v_0 - v}{g} = \frac{(+10.0 \text{ m/s} - (-32.9 \text{ m/s}))}{9.80 \text{ m/s}^2}$$

$$= \frac{42.9 \text{ m/s}}{9.80 \text{ m/s}^2} = 4.38 \text{ s.}$$

2. A stone is dropped freely on the river from a bridge. It takes 5s to touch the water surface in the river.

Calculate:

(i) The height of the bridge from the water level

(ii) The distance covered by stone in the last second

($g = 9.8 \text{ m/s}^2$).

Given, $u = 0$, $g = 9.8 \text{ m/s}^2$, $t = 5 \text{ s}$

Ans) (i)

From equation of motion, $h = ut + \frac{1}{2}gt^2$; $h = 0 \times 5 + \frac{1}{2} \times 9.8 \times (5)^2 = 9.8 \times \frac{25}{2} = 122.5 \text{ m}$

(ii) Distance covered in last second,

$$s(t) = u + \frac{g}{2}(2t-1) = 0 + \frac{1}{2} \times 9.8 \times (2 \times 5 - 1) = 44.1 \text{ m}$$

3. A tennis ball is struck with a racket, firing it straight upward at 22 m/sec. After how much

time will it be falling at 15 metres per second?

Ans) Case 1:-

Given: $u = 22 \text{ m/s}$, $v = 0$, $g = -9.8$;

To find: t_1

$$\Rightarrow v = u + gt_1$$

$$\Rightarrow 0 = 22 + (-9.8)t_1$$

$$\Rightarrow 0 = 22 - 9.8t_1$$

$$\Rightarrow 9.8t_1 = 22$$

$$\Rightarrow t_1 = \frac{22}{9.8} = 2.24 \text{ secs}$$

Case 2:-

Given: $u = 0$, $v = 15 \text{ m/s}$, $g = 9.8$;

To find: t_2

$$\Rightarrow v = u + gt_2$$

$$\Rightarrow 15 = 0 + 9.8t_2$$

$$\Rightarrow 15 = 9.8t_2$$

$$\Rightarrow \frac{15}{9.8} = t_2$$

$$\Rightarrow 1.53 = t_2$$

$$\Rightarrow t_2 = 1.53 \text{ secs}$$

$$\therefore t = t_1 + t_2 = (2.24 + 1.53) \text{ secs}$$

$$= 3.77 \text{ secs} = 3.8 \text{ secs.}$$

\therefore After 3.8 secs it will be falling at 15 m/s.