

HOME ASSIGNMENT

1. The planet Neptune travels in a nearly circular orbit of radius,  $r = 4.5 \times 10^9$  km, about the sun. It takes Neptune 165y to make a complete trip around the sun. How fast (in km/h) does Neptune travel in its orbit?

Ans) Radius =  $4.5 \times 10^9$  km  
 $= \frac{4.5}{10} \times 10000000000 = 45000000000$  km.

Time = 165y =  $165 \times 365 = 60225$  days  
 $= 60225 \times 24 = 1445400$  hrs

Angular velocity =  $\omega = \frac{\theta}{t} = \frac{2\pi r}{1445400}$

$= 2 \times \frac{22}{7} \times 4500000000 \div 1445400$

$= 2 \times \frac{22}{7} \times 4500000000 \times \frac{1}{1445400}$   
 $\frac{1}{657}$

$= 19569.47$  km/h.

∴ It travels 19569.47 km/h fast.

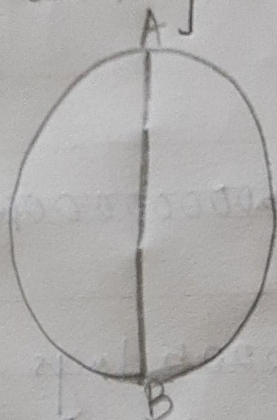
2. A circular cycle track, has a circumference of 314m with AB as one of its diameters. A cyclist travels from A to B along the circular path with a velocity of constant magnitude 15.7m/s.



Find:

- the distance moved by the cyclist
- the displacement of the cyclist if AB represents north-south direction.
- the average velocity of the cyclist.

Ans)



Given,

$$\text{Circumference} = 2\pi r = 314 \text{ m}$$

$$\therefore \text{Radius, } r = \frac{314}{2\pi} = \frac{314}{2 \times 3.14} = 50 \text{ m.}$$

$$(a) \text{ Distance moved, } s = \frac{1}{2} \times \text{circumference}$$

$$= \frac{1}{2} \times 314 = 157 \text{ m.}$$

$$(b) \text{ Displacement} = \overrightarrow{AB} = 2r = 100 \text{ m.}$$

Displacement is in north-south direction.

$$(c) \text{ Time taken in going from A to B} = \frac{157 \text{ m}}{15.7 \text{ m/s}} = 10 \text{ s}$$

$$\therefore \text{Average velocity} = \frac{\text{Displacement}}{\text{Time}} = \frac{100}{10}$$

$$= 10 \text{ m, in north-south direction}$$



3. (a) Define circular motion.

(a) The motion of a body moving around a fixed point in a circular path is known as circular motion.

(b) An artificial satellite is moving in a circular orbit of radius 42,250 km. Calculate speed, if it takes 24 hours to revolve once around the Earth.

(Ans) Radius of the orbit = 42250 km

Time taken = 24 hours

Distance travelled by the satellite

= circumference of circle

$$= 2\pi r$$

$$= 2 \times \frac{22}{7} \times 42250$$

$$= \frac{2 \times 22 \times 42250}{7} \text{ km}$$

Now,

$$\text{Average speed} = \frac{\text{Total distance}}{\text{Total time}}$$

$$= \frac{2 \times 22 \times 42250}{7}$$

$$24$$

$$= \frac{2 \times 22 \times 42250}{7 \times 24} = \frac{4814 \times 21125}{7 \times 3}$$

$$= \frac{232375}{21} = 11065.47 \text{ km/h}$$



Also, converting speed into km/s

$$\text{Average speed} = \frac{232375}{21} \text{ km/h}$$

$$= \frac{232375}{21} \times \frac{\text{km}}{3600 \text{ secs}}$$

$$= \frac{232375}{21 \times 3600} \text{ km/s}$$

$$= \frac{\cancel{232375} 9295}{21 \times 444} \text{ km/s}$$

$$= \frac{9295}{3024} \text{ km/s} = 3.07 \text{ km/s}$$