

Hw

S-CHAND

pg - [198-199]

1. $h_1 = 1\text{m}$, $m = 2$
 $h_2 = ?$

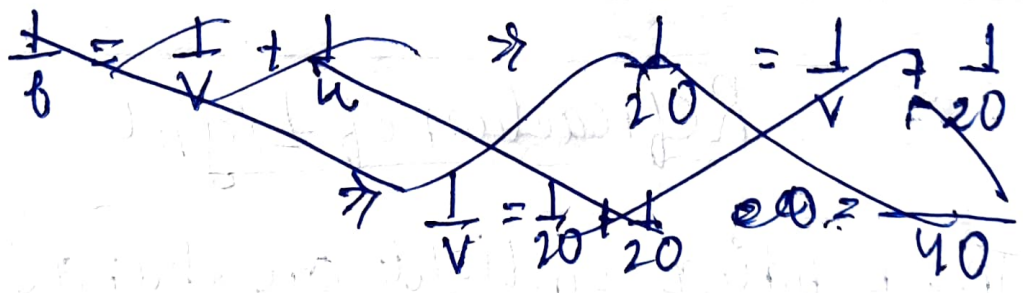
$\Rightarrow m = \frac{h_2}{h_1} \Rightarrow 2 = \frac{h_2}{1}$

$\Rightarrow h_2 = 1 \times 2 = 2\text{ cm}$

2. $f = -20\text{ cm}$

• $u =$, object distance = 20 cm

$v = ?$



$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \Rightarrow \frac{1}{-20} = \frac{1}{v} + \frac{1}{-20} \Rightarrow \frac{1}{-20} = \frac{1}{v} - \frac{1}{20}$

$\Rightarrow \frac{1}{v} = \frac{1}{20} - \frac{1}{20} = 0$

~~$\frac{1}{v} = \frac{1}{0} = \infty$~~

$v = \frac{1}{0} = \infty$

3. (i) $+4 \rightarrow$ If the magnification has $+$ sign then the nature of the image is virtual and erect,
 (ii) $-3 \rightarrow$ If the magnification has $-$ sign then the nature of the image is real & inverted

4. The Relation between image distance, object distance and focal length is -

$$\frac{1}{\text{image distance}} + \frac{1}{\text{object distance}} = \frac{1}{\text{focal length}}$$

$$\Rightarrow \frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

5.
$$\frac{1}{\text{image distance}} + \frac{1}{\text{object distance}} = \frac{1}{\text{focal length}}$$

$$\Rightarrow \frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

Where, u = distance of object from mirror
 v = distance of image from mirror
 f = focal length.

6. The ratio of height of an image ^{to} ~~and~~ the height of object is called linear magnification.

7. The ratio of height of an image to the height of object is called linear magnification.

8. a) $m = \frac{h_2}{h_1}$

b) $m = -\frac{v}{u}$

9. $u = -20 \text{ cm}$
 $f = -10$

$v = ?$

CP

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \Rightarrow \frac{1}{v} + \frac{1}{-20} = \frac{1}{-10}$$

$$= \frac{1}{v} - \frac{1}{20} = \frac{1}{-10} \Rightarrow \frac{1}{v} = \frac{1}{-10} + \frac{1}{20}$$

$$\Rightarrow \frac{1}{v} = \frac{-2 + 1}{20} = \frac{-1}{20}$$

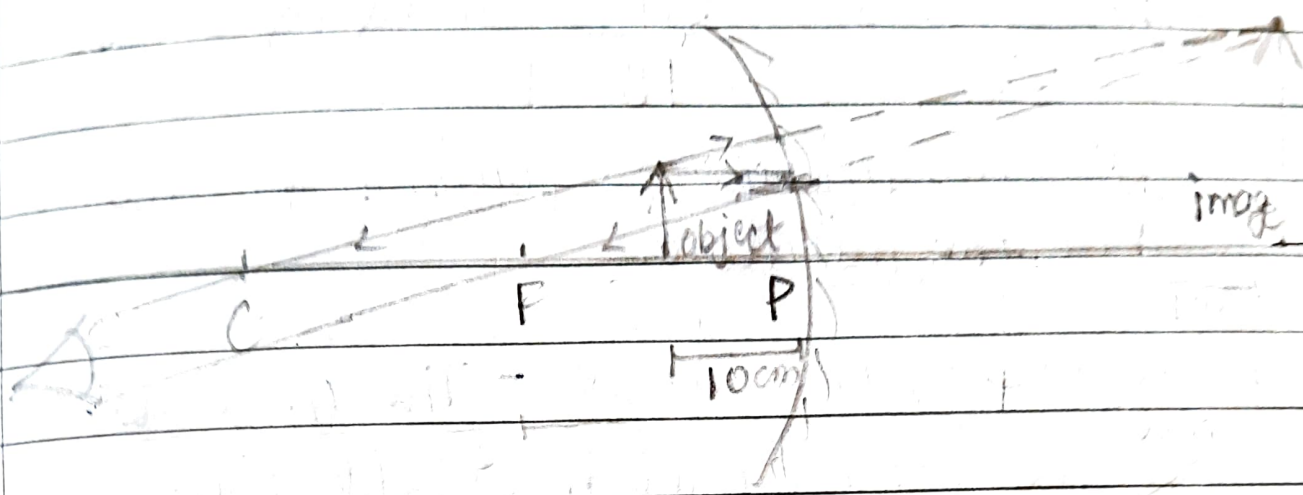
$$\Rightarrow v = -20$$

\therefore The image is real & inverted.

10. a) If the magnification has a plus sign then image is Virtual & Erect.

b) If the magnification has a negative sign then image is Real & Inverted.

11. Object distance = -10 cm, $f = -20$ cm



$$(b) \frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \frac{1}{-20} = \frac{1}{v} + \frac{1}{-10}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{-20} + \frac{1}{10} = \frac{-1+2}{20}$$

$$\Rightarrow \frac{1}{v} = \frac{2}{20} = \frac{1}{10}$$

$$\Rightarrow v = +10$$

(c) As, image distance is +, So the image is virtual and erect.
 It's 2 characteristics ^{of the image} are -
 → It is larger than the object
 → It is formed behind the mirror.

12. $h_1 = 10 \text{ cm}$
 $u = -36 \text{ cm}$
 $f = -12 \text{ cm}$

(i) Position of image.

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \frac{1}{-12} = \frac{1}{v} + \frac{1}{-36}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{-12} + \frac{1}{36} = \frac{-3+1}{36} = \frac{-2}{36}$$

$$\Rightarrow \frac{1}{v} = \frac{-2}{36} = \frac{-1}{18} \Rightarrow v = -18 \text{ cm}$$

So, the image is formed at the left side of the mirror.

(ii) Nature of the image - As, ~~image~~ image is formed at the left side of the mirror, the image will be 'Real & Inverted'.

(iii) Height of the image -

$$\frac{-v}{u} = \frac{h_2}{h_1} \Rightarrow \frac{-(-18)}{-36} = \frac{h_2}{10}$$

$$\Rightarrow -36 h_2 = 180$$

$$\Rightarrow h_2 = -\frac{180}{36} = -5 \text{ cm}$$

13. $f = 10 \text{ cm}$

$h_1 = 2 \text{ cm}$

$h_2 = 6 \text{ cm}$

$u = ?$

$$\frac{-v}{u} = \frac{h_2}{h_1}$$

$$\frac{-v}{u} = \frac{6}{2} \Rightarrow \frac{-v}{u} = 3$$

$$\Rightarrow +v = -3u$$

$$\frac{1}{f} = \frac{1}{u} + \frac{1}{v} \Rightarrow \frac{1}{10} = \frac{1}{u} + \frac{1}{-3u}$$

$$\Rightarrow \frac{1}{10} = \frac{1}{u} - \frac{1}{3u} \Rightarrow \frac{1}{10} = \frac{3-1}{3u} = \frac{2}{3u}$$

$$\Rightarrow \frac{1}{10} = \frac{2}{3u} \quad \Rightarrow 3u = 20 \quad \Rightarrow u = \frac{20}{3}$$

14. $u = 15 \text{ cm}$
 $v = 10 \text{ cm}$
 $f = ?$

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \frac{1}{f} = \frac{1}{10} + \frac{1}{15}$$

$$= \frac{1}{10} + \frac{1}{15} = \frac{3-2}{30}$$

$$\Rightarrow \frac{1}{f} = \frac{1}{30}$$

$$\Rightarrow f = 30 \text{ cm}$$

15. $h_1 = 3 \text{ cm}$
 $u = -8 \text{ cm}$

(i) $\frac{-v}{u} = \frac{h_2}{h_1} \quad \Rightarrow \frac{-v}{-8} = \frac{4.5}{3}$

$h_2 = 4.5 \text{ cm}$

$$\Rightarrow +3v = 36$$

$$\Rightarrow v = +\frac{36}{3} = +12$$

So, the image distance will be 12 cm in the left of the mirror.

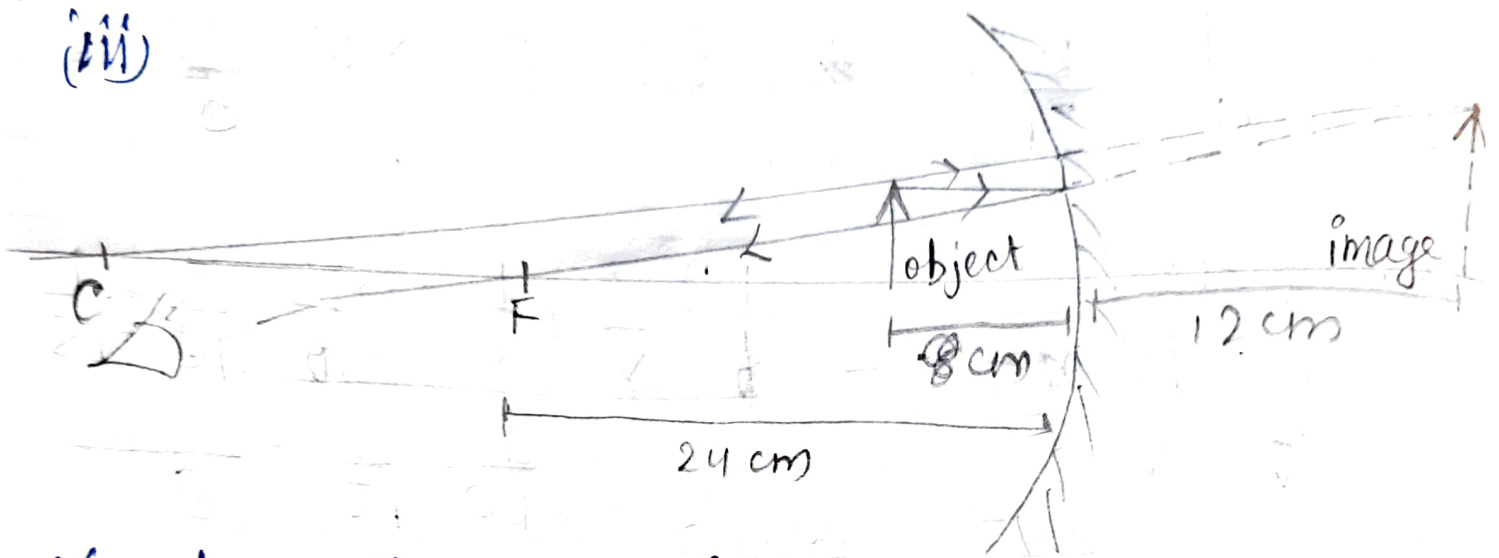
(ii) $\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \frac{1}{f} = \frac{1}{12} + \frac{1}{-8} = \frac{1}{12} - \frac{1}{8}$

$$\Rightarrow \frac{1}{f} = \frac{2-3}{24} = \frac{-1}{24}$$

$$\Rightarrow f = -24 \quad \text{or } f = 24$$

∴ focal length is 24.

(iii)



16. $h_2 = -4 \text{ cm}$

$h_1 = 1 \text{ cm}$

$u = 20 \text{ cm}$

(i) ~~ve~~

(i) $v = ?$

$$\frac{h_2}{h_1} = \frac{-v}{u}$$

$$\Rightarrow \frac{-4}{1} = \frac{-v}{20}$$

$$\Rightarrow -v = -80$$

$$\Rightarrow v = 80 \text{ cm}$$

(ii) $\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$

$$\Rightarrow \frac{1}{f} = \frac{1}{80} + \frac{1}{20} = \frac{1+4}{80} = \frac{5}{80} = \frac{1}{16}$$

$f = 16$

17. $h_1 = 7 \text{ cm}$

$u = -27 \text{ cm}$

$f = -18 \text{ cm}$

(i) $\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \Rightarrow \frac{1}{-18} = \frac{1}{v} + \frac{1}{-27}$

$$\Rightarrow \frac{1}{v} - \frac{1}{27} = -\frac{1}{18}$$

$$\Rightarrow \frac{1}{v} = -\frac{1}{18} + \frac{1}{27} = \frac{-3+2}{54} = -\frac{1}{54}$$

$$\Rightarrow v = -54 \text{ cm}$$

∴ At 54cm in front of the mirror should the screen be placed so that a sharp focused image can be obtained.

(ii) Putting the value of v in,

$$-\frac{v}{u} = \frac{h_2}{h_1} \Rightarrow \frac{+(-54)}{+27} = \frac{h_2}{7}$$

$$\Rightarrow 27 h_2 = -378$$

$$\Rightarrow h_2 = \frac{-378}{27} = \frac{189 \times 2}{63} = \frac{63}{4}$$

$$-\frac{378}{27} = -14 \text{ cm}$$

(iii) Nature of the image is Real & Inverted.

18 $h_1 = 3 \text{ cm}$
 $u = 10 \text{ cm}$
 $f = -20 \text{ cm}$

• Position of the image

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \Rightarrow \frac{1}{-20} = \frac{1}{v} + \frac{1}{10}$$

$$\Rightarrow \frac{1}{-20} = \frac{1}{v} - \frac{1}{10}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{-20} + \frac{1}{10} = \frac{-1+2}{20}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{20}$$

$$\Rightarrow v = 20 \text{ cm}$$

∴ The image formed is 20cm behind the mirror.

• Nature of the image - As the image is formed behind the mirror then it is 'Virtual and Erect'

• Size of the image - $\frac{h_2}{h_1} = -\frac{v}{u}$

$$\Rightarrow \frac{h_2}{3} = \frac{+20}{+10}$$

$$\Rightarrow \frac{h_2}{3} = 2 \quad \Rightarrow h_2 = 6 \text{ cm}$$

19. $f = -4 \text{ cm}$
 $h_1 = 2 \text{ cm}$
 $u = -9 \text{ cm}$

• Position of the image

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \frac{1}{-4} = \frac{1}{v} + \frac{1}{-9}$$

$$\Rightarrow \frac{1}{-4} = \frac{1}{v} - \frac{1}{9}$$

$$\Rightarrow \frac{1}{v} = -\frac{1}{4} + \frac{1}{9} = \frac{-9+4}{36} =$$

$$\Rightarrow \frac{1}{v} = \frac{-5}{36} \quad \Rightarrow -5v = 36$$

$$\Rightarrow v = \frac{36}{-5} = -7.2 \text{ cm}$$

$$\frac{-5}{36}$$

in front of the concave mirror. • The image formed is 7.2 cm

• Nature of the Image -

As the image formed is in front of the

mirror, the nature of the image would be 'Real & Inverted.'

• size of the image - $\frac{h_2}{h_1} = \frac{-v}{u}$

$$\Rightarrow \frac{h_2}{2} = \frac{+(-7.2)}{+9} \quad \Rightarrow \quad 9h_2 = -14.4$$

$$\Rightarrow \quad h_2 = \frac{-14.4}{9}$$

$$= -1.6 \text{ cm}$$

∴ The image formed is 1.6 cm below the principal axis.

20. $u = -20 \text{ cm}$

$m = -3$ [Image is real]

$$m = \frac{-v}{u} \quad \Rightarrow \quad -3 = \frac{+v}{+20} \quad \Rightarrow \quad v = -60 \text{ cm}$$

∴ The image is formed 60 cm in front of the mirror

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \quad \frac{1}{f} = \frac{1}{-60} + \frac{1}{-20}$$

$$\Rightarrow \frac{1}{f} = \frac{1}{-60} - \frac{1}{20} = \frac{-1-3}{60} = \frac{-4}{60} = -\frac{1}{15}$$

∴ The focal length is 15 cm

$$b) \quad m = 3 \quad , \quad b = -15$$

$$m = \frac{-v}{u} \quad \Rightarrow \quad 3 = \frac{-v}{u} \quad \Rightarrow \quad 3u = -v$$

$$\frac{1}{b} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \quad \frac{1}{-15} = \frac{1}{-3u} + \frac{1}{u}$$

$$\Rightarrow \frac{1}{-15} = \frac{-1+3}{3u} \quad \Rightarrow \quad \frac{1}{15} = \frac{2}{3u}$$

$$\rightarrow 3u = 30 \quad \rightarrow u = 10 \text{ cm}$$

21. $R = 3 \text{ cm}$ $b = -1.5 \text{ cm}$

$m = 5 \text{ cm}$

$u = ?$

$$\rightarrow m = \frac{-v}{u} \quad \rightarrow 5u = -v$$

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \rightarrow \frac{1}{-1.5} = \frac{1}{-5u} + \frac{1}{u}$$

~~$$\frac{1}{-1.5} = \frac{1}{-5u} + \frac{1}{u}$$~~

$$\frac{1}{-1.5} = \frac{-1+5}{5u} = \frac{4}{5u}$$

$$\rightarrow \frac{1}{-1.5} = \frac{4}{5u} \quad \rightarrow 5u = -6.0$$

$$\rightarrow u = \frac{-6}{5} = -1.2 \text{ cm}$$

22. $R = 1.5 \text{ m}$; $f = \frac{R}{2} = \frac{1.5}{2} = -0.75 \text{ m}$

$u = -10 \text{ m}$

$v = ?$

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \rightarrow \frac{1}{-0.75} = \frac{1}{v} + \frac{1}{-10}$$

$$\rightarrow \frac{1}{v} = \frac{1}{-0.75} + \frac{1}{10} = \frac{100}{75} + \frac{1}{10}$$

$$\rightarrow \frac{1}{f} = \frac{-200 + 15}{750} = \frac{-185}{750}$$

$$\rightarrow \frac{1}{f} = \frac{-37}{30} \quad \rightarrow -37f = 30 \quad \rightarrow f = \frac{30}{-37}$$

$= -0.81 \text{ m}$

23. $h_1 = 5 \text{ cm}$
 $u = -20 \text{ cm}$
 $b = -15 \text{ cm}$

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \frac{1}{-15} = \frac{1}{v} + \frac{1}{-20}$$

$$\Rightarrow \frac{1}{-15} = \frac{1}{v} - \frac{1}{20} \quad \Rightarrow \frac{1}{v} = \frac{1}{-15} + \frac{1}{20}$$

$$\Rightarrow \frac{1}{v} = \frac{-4 + 3}{-60} = \frac{-1}{60}$$

$$\Rightarrow v = -60 \text{ cm}$$

∴ The image will be formed 60 cm in front of the mirror.

So, the screen should be placed at a distance of 60 cm to obtain a sharp image.

24. $m = 3 \text{ cm}$
 $u = 10 \text{ cm}$
 $R = ? \Rightarrow 2f$

$$m = \frac{-v}{u} \quad \Rightarrow 3 = \frac{-v}{+10}$$

$$\Rightarrow -v = 30 \quad \text{② } -30$$

$$\Rightarrow v = +30$$

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \frac{1}{f} = \frac{1}{+30} + \frac{1}{-10}$$

$$\Rightarrow \frac{1}{f} = \frac{1}{30} - \frac{1}{10} = \frac{1-3}{30} = \frac{-2}{30}$$

$$\Rightarrow \frac{1}{f} = -\frac{1}{15} \quad \Rightarrow f = -15$$

$$R = 2f \quad \Rightarrow R = 2 \times 15 = 30 \text{ cm}$$

25. $h_1 = 50 \text{ mm}$
 $f = -100 \text{ mm}$
 $u = -300 \text{ mm}$
 $h_2 = ?$

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$$

$$\Rightarrow \frac{1}{-100} = \frac{1}{v} + \frac{1}{-300}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{-100} + \frac{1}{300}$$

$$\Rightarrow \frac{1}{v} = \frac{-3 + 1}{300} = \frac{-2}{300}$$

$$\Rightarrow \frac{1}{v} = -\frac{1}{150} \Rightarrow v = -150$$

$$\frac{h_2}{h_1} = -\frac{v}{u} \Rightarrow \frac{h_2}{50} = \frac{-(-150)}{-300}$$

$$\Rightarrow 300 h_2 = -7500$$

$$\Rightarrow h_2 = \frac{-7500}{300} = -25 \text{ cm}$$

26. $u = ?$
 $f = 20 \text{ cm}$

$$h_2 = -\frac{1}{4} h_1$$

$$\frac{h_2}{h_1} = -\frac{v}{u} \Rightarrow -\frac{1}{4} = -\frac{v}{u}$$

$$\Rightarrow \frac{-\frac{1}{4} h_1}{h_1} = -\frac{v}{u} \Rightarrow \frac{-\frac{1}{4} h_1}{h_1} = -\frac{v}{u}$$

$$\Rightarrow +\frac{1}{4} = +\frac{v}{u} \Rightarrow 4v = u \Rightarrow v = \frac{u}{4}$$

$$\frac{1}{b} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \frac{1}{-20} = \frac{1}{u} + \frac{1}{u}$$

~~$$\frac{1}{-20} = \frac{1}{4u} + \frac{1}{u} = \frac{1+4}{4u} = \frac{5}{4u}$$

$$\frac{1}{-20} = \frac{5}{4u} \Rightarrow 4u = -100$$~~

$$\Rightarrow \frac{1}{-20} = \frac{4}{u} + \frac{1}{u} = \frac{5}{u}$$

$$\Rightarrow \frac{1}{-20} = \frac{5}{u} \Rightarrow u = -100 \text{ cm}$$

21. $u = -50 \text{ cm}$

$$m = -\frac{1}{2}$$

~~$$h = 0$$~~

$$m = -\frac{v}{u} \Rightarrow m = \frac{-v}{-50} \Rightarrow -\frac{1}{2} = \frac{v}{50}$$

$$\Rightarrow 2v = -50 \Rightarrow v = \frac{-50}{2} = -25$$

$$\frac{1}{b} = \frac{1}{v} + \frac{1}{u} \Rightarrow \frac{1}{b} = \frac{1}{-25} + \frac{1}{-50} = \frac{-2-1}{50}$$

$$\Rightarrow \frac{1}{b} = -\frac{3}{50}$$

$$\Rightarrow -3b = 50$$

$$\Rightarrow b = -\frac{50}{3} \quad \text{6.6}$$

Q7 If $m = -\frac{1}{5}$ $m = -\frac{v}{u}$ ~~$\frac{1}{5}$~~

$$-\frac{1}{5} = -\frac{v}{u}$$

$$\Rightarrow f u = 5v \quad \Rightarrow v = \frac{u}{5}$$

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \frac{1}{-50} = \frac{1}{\frac{u}{5}} + \frac{1}{u}$$

$$\Rightarrow \frac{3}{-50} = \frac{5}{u} + \frac{1}{u} \quad \Rightarrow \frac{3}{-50} = \frac{6}{u}$$

$$\Rightarrow 3u = -300$$

$$\Rightarrow u = -100 \text{ cm}$$

28 (i) $u = -20 \text{ cm}$

$f = -12 \text{ cm}$

• Position of image -

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \frac{1}{-12} = \frac{1}{v} + \frac{1}{-20}$$

$$\Rightarrow \frac{1}{-12} = \frac{1}{v} - \frac{1}{20}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{-12} + \frac{1}{20} = \frac{-5+3}{60}$$

$$\Rightarrow \frac{1}{v} = -\frac{2}{60} \Rightarrow v = -30$$

• Nature of the image

As, the image is formed in front of the mirror the nature of the image is 'Real & Inverted'

$u =$
 b) $u = 4 \text{ cm}$
 $b = 12 \text{ cm}$

• Position of the image

$$\frac{1}{b} = \frac{1}{v} + \frac{1}{u} \Rightarrow \frac{1}{-12} = \frac{1}{v} + \frac{1}{-4}$$

$$\Rightarrow \frac{1}{v} = -\frac{1}{12} + \frac{1}{4} = \frac{-1+3}{12} = \frac{2}{12} = \frac{1}{6}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{6} \Rightarrow v = 6 \text{ cm}$$

∴ The image formed is at a distance of 6 cm behind the mirror.

• Nature of the image - As, the image formed is behind the concave mirror so, the nature of the image is **Virtual & Erect**.

39. $h_2 = -1 \text{ cm}$
 $u = -5 \text{ cm}$
 $h_1 = 0.25 \text{ cm}$
 $v = ?$
 $f = ?$

$$\frac{h_2}{h_1} = \frac{-v}{u}$$

$$\Rightarrow \frac{-1}{0.25} = \frac{-v}{-5}$$

$$\Rightarrow -0.25v = 5$$

$$\Rightarrow v = \frac{5}{-0.25} = \frac{500}{-25} = -20$$

$$\frac{1}{b} = \frac{1}{v} + \frac{1}{u}$$

$$\Rightarrow \frac{1}{b} = \frac{1}{-20} + \frac{1}{-5}$$

$$\Rightarrow \frac{1}{b} = \frac{-1-4}{20} = \frac{-5}{20}$$

$$\Rightarrow \frac{1}{b} = \frac{-1}{4}$$

$$\Rightarrow f = 4 \text{ cm}$$

30.

$$R = 60\text{cm}$$

$$f = -30\text{cm}$$

$$u = 15\text{cm}$$

• Position of the image.

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u} \quad \Rightarrow \quad \frac{1}{-30} = \frac{1}{v} + \frac{1}{15}$$

$$\Rightarrow \frac{1}{-30} = \frac{1}{v} - \frac{1}{15} \quad \Rightarrow \quad \frac{1}{v} = \frac{1}{-30} + \frac{1}{15} = \frac{-1 + 2}{30}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{30} \quad \Rightarrow \quad v = 30$$

The image formed is at a distance 30cm behind the mirror.

$$m = -\frac{v}{u} \quad \Rightarrow \quad \frac{-30}{-15} = +2$$