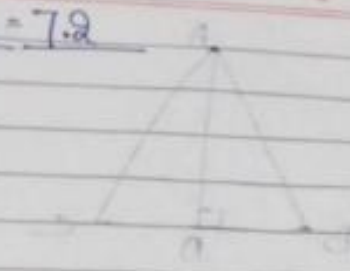
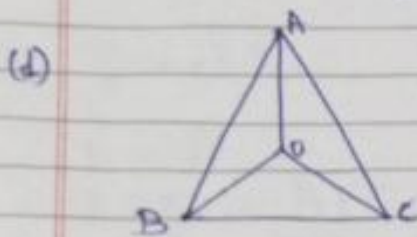


Exercise - 7.2



Given,  
 $AB = AC$  and the bisectors of  $\angle B$  and  $\angle C$   
 intersect each other at  $D$ .

(i)  $\triangle ABC$  is an isosceles with  $AB = AC$   
 $\angle B = \angle C$   
 $\frac{1}{2} \angle B = \frac{1}{2} \angle C$

$\angle OBC = \angle OCB$

$\therefore OB = OC$

(ii)  $\triangle AOB$  and  $\triangle AOC$

$AB = AC$

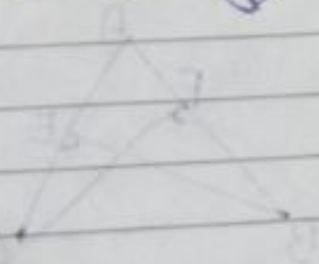
$AO = AO$

$OB = OC$

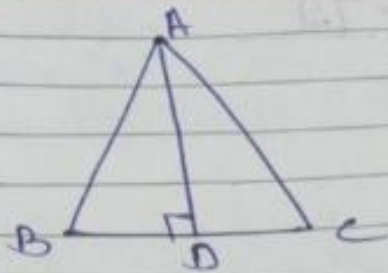
(As proved already)

$\angle BAO = \angle CAO$  (by CPCT)

Thus,  $AO$  bisects  $\angle A$ .



(2)



To prove  $AB = AC$

In  $\triangle ADB$  and  $\triangle ADC$

$$AD = AD$$

$$\angle ADB = \angle ADC$$

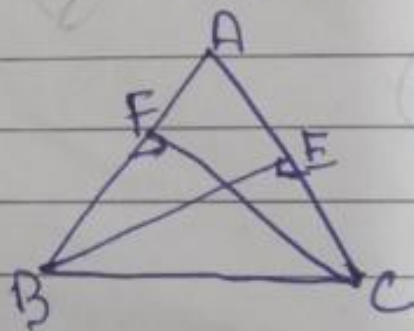
$$BD = CD$$

So,  $\triangle ADB \cong \triangle ADC$  by SAS congruency criterion.

Thus,

$$AB = AC \text{ (by CPCT)}$$

(3)



When,

(i)  $BE = CF$

(ii)  $AC = AB$

to prove  $\therefore BE = CF$

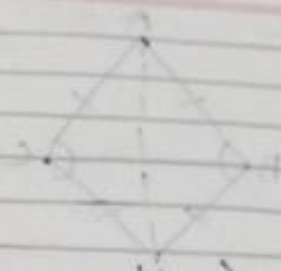
Proof:

$$A = A$$

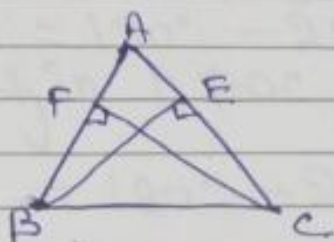
$$\angle AEB = \angle AFC$$

$$AB = AC \text{ (given in question)}$$

$\therefore \triangle AEB \cong \triangle AFC$  and so,  $BE = CF$   
(by CPCT).



(5)



Given that  $BE = CF$

(i) In  $\triangle ABE$  and  $\triangle ACF$

$$A = A$$

$$\angle AEB = \angle AFC$$

$$BE = CF$$

$\therefore \triangle ABE \cong \triangle ACF$  by AAS Congruency condition.

(ii)  $AB = AC$  by CPCT and so,  $\triangle ABC$  is an isosceles triangle.