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EXERCISE 8.1



1. Ratio of angles in the quadrilateral
 $= 3:5:9:13$

Let the angles be, $3x, 5x, 9x, 13x$

According to Angle sum property of rectangle :-

$$3x + 5x + 9x + 13x = 360^\circ$$

$$\therefore \rightarrow 30x = 180^\circ$$

$$\therefore \rightarrow x = 9^\circ$$

\therefore The angles measures are $27^\circ, 45^\circ, 81^\circ, 117^\circ$

2. Let ABCD be a parallelogram such that ~~AC = DB~~ $AC = BD$

In $\triangle ABC$ & $\triangle DCB$

$$AC = DB \text{ (Given)}$$

$$AB = DC \text{ (Opposite sides of a parallelo-gram)}$$

$$BC = CB \text{ (Common)}$$

$\therefore \triangle ABC \cong \triangle DCB$ (By SSS Congruency)

$$\Rightarrow \angle ABC = \angle DCB \text{ (By CPCT) } \dots \dots (i)$$

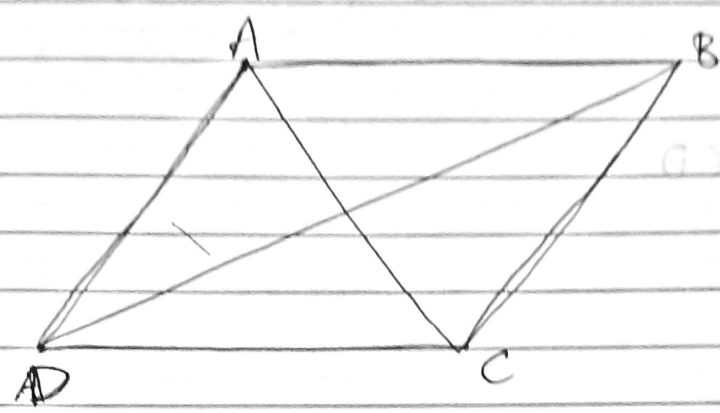
Now, $AB \parallel DC$ & BC is a transversal

[\because ABCD is a parallelogram]

$$\therefore \angle ABC + \angle DCB = 180^\circ \dots \dots (ii)$$

(Co-int. angles)

from (i) & (ii), we get
 $\angle ABC = \angle DCB = 90^\circ$
 which means that ABCD is a parallelogram having an angle equal to 90° .
 \therefore ABCD is a rectangle.



Q3. Given,
 A quadrilateral, in which the diagonals are perpendicular bisectors of each other.

To prove :- Its a Rhombus.

Proof :-

As diagonals are perpendicular bisectors of the quadrilateral, so the angles formed by bisecting of diagonals are equal. (90°)

Let's take ABCD quadrilateral.

So, $AC = BD$ and intersecting point is E.
 $\therefore \angle AED = \angle BEC = \angle AEB = \angle CED$

which means, $DA = CB = AB = DC$
(side opposite to equal angles are equal)

Hence, a quadrilateral with all sides equal is called a Rhombus.