

(6) AP: 11, 8, 5, 2...

⇒ $d = 8 - 11$

$d = -3$

$a_n = -150$

$a = 11$

⇒ $a_n = a + (n-1)d$

$-150 = 11 + (n-1) \cdot (-3)$

$-150 = 11 - 3n + 3$

$-3n = -150 - 11 - 3$

$-3n = 164$

$n = \frac{164}{-3}$

∴ No

(7) $a_{11} = 38$

$a_{16} = 73$

$a + 10d = 38$ - (i)

$a + 15d = 73$ - (ii)

$-5d = -35$

$d = \frac{-35}{-5}$

$d = 7$

$a + 10d = 38$

$a + 10 \times 7 = 38$

$a + 70 = 38$

$a = 38 - 70$

$a = -32$

$a_{31} = a + 30d$

$= (-32) + 30 \times 7$

$= -32 + 210$

$a_{31} = 178$

(8) $a_3 = 12, a_{50} = 106$

$$a + 2d = 12 \quad \text{--- (i)}$$

$$a + 49d = 106 \quad \text{--- (ii)}$$

$$a + 2d - a - 49d = 12 - 106$$

$$-47d = -94$$

$$d = \frac{-94}{-47}$$

$$d = 2$$

$$a + 2 = 12$$

$$a = 12 - 2$$

$$a = 10$$

$$\Rightarrow a + (n-1)d$$

$$\Rightarrow 10 + (29-1)2$$

$$\Rightarrow 10 + 28 \times 2$$

$$\Rightarrow 10 + 56$$

$$\Rightarrow 66$$

$$a_{29} = 66$$

(9) $a_3 = 4, a_9 = -8$

$$a + 2d = 4 \quad \text{--- (i)}$$

$$a + 8d = -8 \quad \text{--- (ii)}$$

$$\begin{array}{r} a + 8d = -8 \\ -(a + 2d = 4) \\ \hline 6d = -12 \end{array}$$

$$d = \frac{-12}{6}$$

$$d = -2$$

$$a + 2(-2) = 4$$

$$a - 4 = 4$$

$$a = 4 + 4$$

$$a = 8$$

$$a + 3d$$

$$= 8 + 3(-2)$$

$$= 8 - 6$$

$$= 2$$

$$a + 4d$$

$$= 8 + 4(-2)$$

$$= 8 - 8$$

$$= 0$$

$$a_5 = 0 \text{ , 5th term}$$

(10)

$$a_{17} - a_{10} = 7$$

$$= a + 16d - (a + 9d) = 7$$

$$= a + 16d - a - 9d = 7$$

$$= 7d = 7$$

$$= d = \frac{7}{7}$$

$$\Rightarrow \boxed{d = 1}$$

(11)

$$AP: 3, 15, 27, 39, \dots$$

$$a = 3$$

$$d = 15 - 3$$

$$\boxed{d = 12}$$

$$n = 54$$

\Rightarrow

$$a_{54} = a + (n-1)d$$

$$= 3 + (54-1) \times 12$$

$$= 3 + 53 \times 12$$

$$= 3 + 636$$

$$= 639$$

$$\boxed{a_{54} = 639}$$

$$639 + 132 = 771$$

$$a_n = 771$$

$$771 = 3 + (n-1) \times 12$$

$$771 - 3 = (n-1) \times 12$$

$$768 = (n-1) \times 12$$

$$\frac{768}{12} = n-1$$

$$64 = n-1$$

$$n = 64 + 1$$

$$\boxed{n = 65}$$

2) For 1st AP
1st term = A
common difference = d
100th term = $A + 99d$

For 2nd AP
1st term = a
common difference = d
100th term = $a + 99d$

$$\text{difference} = A + 99d - a - 99d = 100$$
$$A - a = 100 \quad \text{--- (1)}$$

difference between 1000th terms

$$\begin{aligned} &= A_{1000} - a_{1000} \\ &= [A + (1000 - 1)d] - [a + (1000 - 1)d] \\ &= [A + 999d] - [a + 999d] \\ &= A + 999d - a - 999d \\ &= A - a \\ &= \text{Putting values from (1)} \\ &= A - a = 100 \end{aligned}$$