

either $n-25 \geq 0$ or $n-30 \geq 0$

$$\Rightarrow n = 25 \text{ or } n = 30$$

Hence, the number of toys produced in a day, will be either 25 or 30.

Let the first number be n and second no. be $= 27-n$

Therefore the products of two numbers

$$n(27-n) = 182$$

$$\Rightarrow n^2 - 27n - 182 = 0$$

$$\Rightarrow n^2 - 13n - 14n + 182 = 0$$

$$\Rightarrow n(n-13) - 14(n-13) = 0$$

$$\Rightarrow (n-13)(n-14) = 0$$

Thus, either $n-13 \geq 0$ or $n-14 \geq 0$

$$\Rightarrow n \geq 13 \text{ or } n \geq 14$$

And if first number = 14, the second number = $27-13 = 14$

And if first no = 14
then second no = $27-14 = 13$

4 Let us take two consecutive positive integers be n and $n+1$.

Therefore, as per the given question,

$$n^2 + (n+1)^2 = 365$$

$$n^2 + n^2 + 1 + 2n = 365$$

$$\Rightarrow 2n^2 + 2n - 365 = 0$$

$$= n^2 + n - 182 = 0$$

$$\Rightarrow n^2 + 14n - 13n - 182 = 0$$

$$\Rightarrow n(n+14) - 13(n+14) = 0$$

$$(n+14)(n-13) = 0$$

5 Thus, either $n+14 = 0$ or $n-13 = 0$
 $n = -14$ or $n = 13$

Since integers are positive, so n can be 13,

$$n+1 = 13 + 1 = 14$$

Therefore, two consecutive positive integers will be 13 and 14

5 The base of the right triangle becomes altitude of right triangle $(n-7)$

Pythagoras

$$\text{Base}^2 + \text{Altitude}^2 = \text{Hypotenuse}^2$$

$$= n^2 + (n-7)^2 = 13^2$$

$$\Rightarrow n^2 + n^2 + 49 - 14n = 169$$

$$\Rightarrow 2n^2 - 14n - 120 = 0$$

$$\Rightarrow n^2 - 7n - 60 = 0$$

$$\Rightarrow n^2 - 12n + 5n - 60 = 0$$

$$\Rightarrow n(n-12) + 5(n-12) = 0$$

$$\Rightarrow (n-12)(n+5) = 0$$

So either $n-12=0$ or $n+5=0$
 $n=12$ or $n=-5$

Since sides cannot be negative
 n can only be 12.

Therefore the base of the given triangle is 12 cm and the altitude of the triangle will be $(12-7)$ cm
 $= 5$ cm

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Let us say the no. of articles produced = n .

Therefore cost of production = $\text{₹}(2n+3)$

Total cost = $\text{₹}90$,

$$\therefore n(2n+3) = 90$$

$$\Rightarrow 2n^2 + 3n - 90 = 0$$

$$2n^2 + 15n - 12n - 90 = 0$$

$$\Rightarrow n(2n+15) - 6(2n+15) = 0$$

$$\Rightarrow (2n+15)(n-6) = 0$$

either $2n+15=0$ or $n-6=0$

$$n = \frac{-15}{2} \text{ or } n = 6$$

Hence no. of articles produced = 6
 Cost = $\text{₹}15$