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8x52

Q1 (i) $a=7$.

$$d=3$$

$$n=8$$

$$\therefore a_n = a + (n-1)d$$

$$a_8 = 7 + (8-1)3 = 7 + 21 = 28.$$

(ii) $a=-18$.

$$n=10$$

$$a_n=0$$

$$\therefore a_n = a + (n-1)d$$

$$\Rightarrow 0 = -18 + (10-1)d$$

$$\Rightarrow 0 = -18 + 9d$$

$$d=2$$

(iii) $d=-3$.

$$n=18$$

$$a_n = 5 - 3$$

$$\therefore a_n = a + (n-1)d$$

$$\Rightarrow -5 = a + (18-1)(-3)$$

$$\Rightarrow a = 46$$

(iv) $a=-18.9$.

$$d=2.5$$

$$a_n = 3.6$$

$$\therefore a_n = a + (n-1)d$$

$$3.6 = -18.9 + (n-1)2.5$$

$$\Rightarrow 25 = 2.5n$$

$$\Rightarrow n = \frac{25}{2.5} = 10$$

$$\begin{aligned} \text{(v)} \quad a &= 3.5 \\ d &= 0 \\ n &= 105 \\ \therefore a_n &= a + (n-1)d \\ &= 3.5 + (105-1)0 = 3.5 \end{aligned}$$

$$\begin{aligned} \text{OR: (i) } &10, 7, 4, \dots \\ a &= 10 \\ d &= 7 - 10 = -3 \\ n &= 30 \\ a_n &= a + (n-1)d \\ \Rightarrow a_{30} &= a + (30-1)d = d + 29d = 10 + 29(-3) \\ &= 10 - 87 = -77 \end{aligned}$$

$$\begin{aligned} \text{(ii) } &-3, -\frac{1}{2}, 2, \dots \\ a &= -3 \\ n &= 11 \\ d &= -\frac{1}{2} - (-3) \\ &= -\frac{1}{2} + \frac{3}{1} = \frac{5}{2} \\ a_n &= a + (n-1)d \Rightarrow a_{11} = a + (11-1)d \\ \Rightarrow a_{11} &= a + 10d \\ &= -3 + 10 \times \frac{5}{2} = -3 + 25 = 22 \end{aligned}$$

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$$\text{Q3) (i) } a = 2$$

$$t_3 = 26$$

$$t_3 = a + (3-1)d$$

$$\Rightarrow 26 = 2 + 2d$$

$$\Rightarrow d = 12$$

$$t_2 = t_3 - d = 26 - 12 = 14$$

\therefore the complete sequence is 2, $\boxed{14}$, 26.

$$\text{(ii) } t_2 = 13$$

$$t_4 = 3$$

$$t_2 = a + (2-1)d$$

$$\Rightarrow 13 = a + d \dots (i)$$

$$t_4 = a + (4-1)d$$

$$\Rightarrow 3 = a + 3d \dots (ii)$$

$$d = -5$$

$$d = -5$$

$$\text{(iii) } a = 5$$

$$t_4 = a + 3d = \frac{19}{2}$$

$$\text{then, } t_4 = a + (4-1)d$$

$$= \frac{19}{2} - \frac{3}{2} = \frac{16}{2} = 8$$

$$\& t_2 = t_3 - d$$

$$= 8 - \frac{3}{2} = \frac{16-3}{2} = \frac{13}{2} = 6\frac{1}{2}$$

Hence, the complete sequence is 5, $\boxed{6\frac{1}{2}}$, $\boxed{8}$, $9\frac{1}{2}$.

$$\text{(iv) } a = -4$$

$$t_6 = 6$$

$$\text{then, } t_6 = a + 5d$$

$$\Rightarrow 6 = -4 + 5d$$

$$\therefore t_2 = a + d$$

$$t_3 = a + 2d$$

$$t_4 = a + 3d$$

$$t_5 = a + 4d$$

$\therefore -4, \boxed{2}$

$$\text{Q4) given: } 3$$

$$a = 3$$

$$d = 8 - 3$$

$$\text{Let term}$$

$$a_n = 78$$

$$a + (n-1)d$$

$$\Rightarrow 3 + (n-1)8 = 78$$

$$\Rightarrow (n-1)8 = 75$$

$$\Rightarrow n-1 = \frac{75}{8}$$

$$\Rightarrow n = \frac{75}{8} + 1 = \frac{83}{8}$$

(iv) $a = -4$.

$t_6 = 6$.

then, $t_6 = a + (6-1)d$.

$\Rightarrow 6 = -4 + 5d \Rightarrow d = 2$.

$\therefore t_2 = a + d = -4 + 2 = -2$.

$t_3 = a + 2d = -4 + 4 = 0$.

$t_4 = a + 3d = -4 + 6 = 2$.

$t_5 = a + 4d = -4 + 8 = 4$.

$\therefore -4, \boxed{-2}, \boxed{0}, \boxed{2}, \boxed{4}, 6$.

Q4: given: $3, a, 13, 18, \dots$

$a = 3$.

$d = 8 - 3 = 5$

Let term is 78.

$a_n = 78$

$a + (n-1)d = 78$.

$\Rightarrow 3 + (n-1)5 = 78$.

$\Rightarrow (n-1)5 = 78 - 3$.

$\Rightarrow (n-1)5 = 75$.

$\Rightarrow n-1 = 15$

$\Rightarrow n = 15 + 1$.

$\Rightarrow n = 16$.

Q5) i) $a = 7$.

$$d = 13 - 7 = 6$$

$$l = 205$$

$$l = a + (n-1)d$$

$$205 = 7 + (n-1) \times 6$$

$$\Rightarrow (n-1) = \frac{198}{6} = 33$$

$$\Rightarrow n = 33 + 1 = 34$$

\therefore Hence, the no. of terms in this AP is 34.

ii) $d = 15\frac{1}{2} - 18 = \frac{31 - 36}{2} = \frac{-5}{2}$

$$l = -47$$

$l = a + (n-1)d$, we get:

$$-47 = 18 + (n-1) \left(\frac{-5}{2} \right)$$

$$\Rightarrow (n-1) = \frac{65 \times 2}{5} = 26$$

$$\Rightarrow n = 26 + 1 = 27$$

\therefore hence, the no. of terms in AP is 27.

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