

$$9. a \frac{5}{14} < \frac{5}{8}$$

$$b. \frac{12}{14} < \frac{11}{12}$$

$$c. \frac{16}{19} > \frac{15}{23}$$

$$d. \frac{33}{98} \Rightarrow \frac{23}{100}$$

$$e. \frac{45}{70} > \frac{43}{55}$$

$$f. \frac{37}{80} \Rightarrow \frac{37}{90}$$

$$g. \frac{67}{79} < \frac{72}{79}$$

$$h. \frac{82}{39} > \frac{27}{39}$$

$$10. a. \frac{3}{4} < \frac{6}{7}$$

$$b. \frac{8}{9} > \frac{5}{8}$$

$$c. \frac{3}{10} < \frac{5}{8}$$

$$d. \frac{11}{12} > \frac{8}{9}$$

$$e. 6 \frac{6}{7} \cdot \frac{49}{8}$$

$$f. \frac{48}{7} > \frac{49}{8}$$

$$= \frac{66}{7} > \frac{49}{8}$$

(8)  ~~$5\frac{2}{7}$~~   ~~$5\frac{4}{8}$~~   $5\frac{2}{7}$   ~~$5\frac{4}{8}$~~   $>$   ~~$5\frac{4}{8}$~~

$=$   ~~$5\frac{2}{7}$~~   ~~$5\frac{4}{8}$~~   $5\frac{2}{7}$   $>$   ~~$5\frac{4}{8}$~~

$=$   ~~$5\frac{2}{7}$~~   ~~$5\frac{4}{8}$~~   $5\frac{2}{7}$   $>$   ~~$5\frac{4}{8}$~~

(9)  $1\frac{11}{12}$   $1\frac{12}{15}$

$=$   $\frac{23}{12}$   $>$   $\frac{27}{15}$

~~$1\frac{11}{12}$~~   $= 1\frac{11}{12} > 1\frac{12}{15}$

(10)  $16\frac{3}{5}$   $16\frac{4}{7}$

$=$   $\frac{83}{5} > \frac{116}{7}$

$=$   $16\frac{3}{5} > 16\frac{4}{7}$

$$11. a, \frac{11}{13}, \frac{11}{17}, \frac{11}{15}$$

$$A \rightarrow \frac{11}{13} < \frac{11}{15} < \frac{11}{17}$$

$$b. \frac{8}{15} < \frac{8}{11} < \frac{8}{9}$$

$$c. \frac{8}{17}, \frac{16}{17}, \frac{15}{17}$$

$$\frac{8}{17} < \frac{15}{17} < \frac{16}{17}$$

$$4. \frac{3}{4}, \frac{5}{6}, \frac{7}{10}$$

$$\frac{3 \times 9 = 27}{4 \times 9 = 36}$$

$$\frac{5 \times 6 = 30}{6 \times 6 = 36}$$

$$\frac{7 \times 4 = 28}{10 \times 2 = 20}$$

$$\frac{27}{36}, \frac{28}{36}, \frac{20}{36}$$

$$\frac{7}{18} < \frac{7}{9} < \frac{5}{9}$$

$$b. (c) \frac{8}{9}, \frac{7}{9}, \frac{2}{3}$$

$$\frac{8 \times 1 = 8}{9 \times 1 = 9}$$

$$\frac{7 \times 1 = 7}{9 \times 1 = 9}$$

$$\frac{2 \times 3 = 6}{3 \times 3 = 9}$$

$$\frac{8}{9} < \frac{7}{9} < \frac{6}{9}$$

$$\begin{array}{l|l} 2 & 4, 6, 8 \\ 3 & 2, 3, 9 \\ & 2, 1, 3 \end{array}$$

$$LCM = 2 \times 3 \times 2 \times 3 = 36$$

$$\begin{array}{l|l} 3 & 36 \\ & 1, 2 \end{array}$$

(e)  $\frac{5}{12}, \frac{2}{6}, \frac{3}{3}$

$= \frac{5 \times 1}{12 \times 1} = \frac{5}{12}$

$\frac{5 \times 2}{12 \times 2} = \frac{10}{12}$

$\frac{2 \times 4}{3 \times 4} = \frac{8}{12}$

$= \frac{5}{12} < \frac{8}{12} < \frac{10}{12}$

$= \frac{5}{12} < \frac{8}{12} < \frac{10}{12}$

(g)  $\frac{7}{10}, \frac{2}{3}, \frac{11}{24}$

$\frac{7 \times 12}{10 \times 12} = \frac{84}{120}$

$\frac{2 \times 40}{3 \times 40} = \frac{80}{120}$

$\frac{11 \times 9}{24 \times 9} = \frac{99}{216}$

$\frac{99}{216} < \frac{80}{120} < \frac{84}{120}$

$\frac{11}{24} < \frac{2}{3} < \frac{7}{10}$

(b)  $\frac{11}{21}, \frac{5}{7}, \frac{7}{2}$

$\frac{11 \times 2}{21 \times 2} = \frac{22}{42}$

$\frac{5 \times 6}{7 \times 6} = \frac{30}{42}$

$\frac{7 \times 21}{2 \times 21} = \frac{147}{42}$

~~$\frac{11}{21}, \frac{5}{7}, \frac{7}{2}$~~   
 $12 = 2 \times 2 \times 3$   
 $6 = 2 \times 3$   
 $3 = 3 \times 1$

LCM =  $2 \times 2 \times 3 \times 1 = 12$

3 | 10, 3, 24  
 2 | 10, 8  
 2 | 5, 4  
 5, 1, 2

LCM =  $3 \times 2 \times 2 \times 5 \times 2 = 120$

7 | 21, 7, 2  
 3, 1, 2

LCM =  $7 \times 3 \times 2 = 42$

$$\frac{21}{42} < \frac{22}{42} < \frac{30}{42}$$

$$\frac{1}{2} < \frac{11}{21} < \frac{5}{7}$$

$$12 \text{ (d) } \frac{7}{4}, \frac{7}{8}, \frac{9}{12}$$

$$\frac{1 \times 6 = 6}{4 \times 6 = 24}$$

$$\frac{7 \times 3 = 21}{8 \times 3 = 24}$$

$$\frac{5 \times 2 = 10}{12 \times 2 = 24}$$

$$\frac{6 \times 21}{14 \times 24} > \frac{10}{24} > \frac{6}{24}$$

$$\frac{7}{8} > \frac{5}{12} > \frac{7}{9}$$

$$(b) \frac{5}{8}, \frac{3}{8}, \frac{3}{9}$$

$$\frac{5 \times 2 = 10}{8 \times 2 = 16}$$

$$\frac{3 \times 1 = 3}{16 \times 1 = 16}$$

$$\frac{3 \times 4 = 12}{9 \times 4 = 36}$$

$$\frac{12}{36} > \frac{10}{36} > \frac{3}{36}$$

$$(c) \frac{8}{8}, \frac{3}{4}, \frac{5}{14}$$

$$\frac{5 \times 7 = 35}{8 \times 7 = 56}$$

$$\frac{3 \times 14 = 42}{4 \times 14 = 56}$$

$$2 \mid 4, 8, 12$$

$$2 \mid 2, 4, 6$$

$$2 \mid 2, 3$$

$$\text{LCM} = 2 \times 2 \times 2 \times 3 = 24$$

$$2 \mid 8, 16, 4$$

$$2 \mid 4, 8, 2$$

$$2 \mid 2, 4, 1$$

$$1, 2, 1$$

$$\text{LCM} = 2 \times 2 \times 2 \times 2 = 16$$

$$2 \mid 4, 8, 14$$

$$2 \mid 2, 4, 7$$

$$1, 2, 7$$

$$\text{LCM} = 2 \times 2 \times 2 \times 7 = 56$$

$$\frac{5 \times 4 = 20}{14 \times 4 = 56}$$

$$\frac{42}{56} < \frac{35}{56} < \frac{20}{56}$$

(d)  $\frac{5}{14}, \frac{7}{9}, \frac{2}{3}$

$$\frac{5 \times 9 = 45}{14 \times 9 = 126}$$

$$\frac{7 \times 18 = 126}{9 \times 14 = 126}$$

$$\frac{2 \times 63 = 126}{14 \times 9 = 126}$$

$$\frac{45 \times 2 = 90}{126} > \frac{35}{126} > \frac{20}{126}$$

$$\frac{7}{9} > \frac{2}{3} > \frac{5}{14}$$

(e)  $\frac{7}{16}, \frac{3}{8}, \frac{5}{12}$

$$\frac{7 \times 3 = 21}{16 \times 3 = 48}$$

$$\frac{3 \times 6 = 18}{8 \times 6 = 48}$$

$$\frac{5 \times 4 = 20}{12 \times 4 = 48}$$

$$\frac{21}{48} > \frac{20}{48} > \frac{18}{48}$$

$$= \frac{7}{16} > \frac{5}{12} > \frac{3}{8}$$

(f)  $\frac{25}{27}, \frac{8}{9}, \frac{5}{18}$

$$= \frac{25 \times 2 = 50}{27 \times 2 = 54}$$

$$\begin{array}{l|l} 3 & 14, 9, 3 \\ \hline 3 & 14, 3, 1 \\ \hline 3 & 7, 3, 1 \\ \hline & 7, 1, 1 \end{array}$$

$$LCM = 3 \times 2 \times 3 \times 7 = 126$$

$$\begin{array}{l|l} 2 & 16, 8, 12 \\ \hline 2 & 8, 4, 6 \\ \hline 2 & 4, 2, 3 \\ \hline & 2, 1, 3 \end{array}$$

$$LCM = 2 \times 2 \times 2 \times 2 \times 3 = 48$$

$$\begin{array}{l|l} 3 & 27, 9, 18 \\ \hline 3 & 9, 3, 6 \\ \hline & 3, 1, 2 \end{array}$$

$$LCM = 3 \times 3 \times 3 \times 2 = 54$$

$$\frac{8 \times 6 = 48}{9 \times 6 = 54}$$

$$\frac{6 \times 3 = 18}{18 \times 3 = 54}$$

$$\frac{50}{54} > \frac{48}{54} > \frac{18}{54}$$

$$= \frac{25}{27} > \frac{8}{9} > \frac{5}{18}$$

$$(g) \frac{11}{20}, \frac{4}{5}, \frac{17}{40}$$

$$\frac{11 \times 2 = 22}{20 \times 2 = 40}$$

$$\frac{4 \times 8 = 32}{5 \times 8 = 40}$$

$$\frac{17 \times 1 = 17}{40 \times 1 = 40}$$

$$\frac{32}{40} > \frac{22}{40} > \frac{17}{40}$$

$$= \frac{4}{5} > \frac{11}{20} > \frac{17}{40}$$

$$(b) \frac{11}{17}, \frac{7}{9}, \frac{7}{2}$$

$$\frac{11 \times 4 = 44}{17 \times 4 = 68}$$

$$\frac{1 \times 17 = 17}{4 \times 17 = 68}$$

$$\frac{1 \times 34 = 34}{2 \times 34 = 68}$$

$$\frac{44}{68} > \frac{34}{68} > \frac{17}{68}$$

$$= \frac{11}{17} > \frac{1}{2} > \frac{1}{4}$$

$$5 \mid 20, 5, 40$$

$$2 \mid 4, 1, 8$$

$$2 \mid 2, 1, 4$$

$$1, 1, 2$$

$$LCM = 5 \times 2 \times 2 \times 2 = 40$$

$$2 \mid 17, 4, 2$$

$$17 \mid 17, 2, 1$$

$$1, 2, 1$$

$$LCM = 2 \times 17 \times 2 = 68$$