



Exercise 14(A)

23) In this figure,

$$5x + x + 80^\circ + 123^\circ + 85^\circ = 360^\circ$$

(Angles at a point)

$$= 6x + 80^\circ + 123^\circ + 85^\circ = 360^\circ$$

$$= 6x + 288^\circ = 360^\circ$$

$$= 6x = 360^\circ - 288^\circ = 72^\circ$$

$$= \text{So } x = \frac{72^\circ}{6} = 12^\circ$$

$$\text{Now, } \angle AOB = 5x = 5 \times 12^\circ = 60^\circ$$

$$\text{and } \angle BOC = x = 12^\circ$$

24) In this figure,

$$3\frac{1}{2}y^\circ + 2y^\circ + 2y^\circ + 2\frac{1}{2}y^\circ = 360^\circ$$

(Angles at a point)

$$= \frac{7}{2}y^\circ + 2y^\circ + 2y^\circ + \frac{5}{2}y^\circ = 360^\circ$$

$$= \frac{7}{2}y^\circ + \frac{5}{2}y^\circ + 4y^\circ = 360^\circ$$

$$= \frac{12y^\circ}{2} + 4y^\circ = 360^\circ$$

$$= 6y^\circ + 4y^\circ = 360^\circ$$

$$= 10y^\circ = 360^\circ$$

$$= y = \frac{360}{10} = 36^\circ$$

$$\therefore \angle AOB = 2\frac{1}{2}y^\circ = \frac{5}{2}y^\circ = \frac{5}{2} \times 36^\circ$$

$$= 90^\circ$$

$$\angle BOC = 2y^\circ = 2 \times 36 = 72^\circ$$

$$\angle COD = 2y^\circ = 72^\circ$$

$$\angle DOA = 2\frac{1}{2}y^\circ = \frac{5}{2}y^\circ$$

$$= \frac{5}{2} \times 36^\circ = 90^\circ$$

25) AB, CD, and EF are intersecting each other at O.

$$\angle DOF = x^\circ, \angle AOC = y^\circ$$

$$\text{and } \angle BOF = z^\circ$$

$$\text{But } \angle DOB = \angle AOC = y^\circ$$

(Vertically opposite angles)

$$\text{Similarly, } \angle COE = \angle DOF = x^\circ$$

$$\text{and } \angle AOF = \angle BOE = z^\circ$$

∴ CD is straight line

$$\therefore \angle COE + \angle BOF + \angle DOB = 180^\circ$$

$$\therefore x^\circ + z^\circ + y^\circ = 180^\circ$$

$$\therefore x^\circ + y^\circ + z^\circ = 180^\circ$$

25) i) If $y = 45^\circ$ and $z = 90^\circ$ then

$$= x^\circ + 45^\circ + 90^\circ = 180^\circ$$

$$= x^\circ + 135^\circ = 180^\circ$$

$\therefore x^\circ = 180^\circ - 135^\circ = 45^\circ$

ii) If $x = 3a$, $y = 5x$, $z = 6x$
then $x + y + z = 180^\circ$

$$= x + 5x + 6x = 180^\circ = 12x = 180^\circ$$

$$= x = \frac{180^\circ}{12} = 15^\circ$$

But $x = 3a$

$$\therefore 3a = 15^\circ = a = \frac{15^\circ}{3} = 5^\circ$$

Hence $a = 5^\circ$