

Q4) Perimeter = 42

two sides = 18 and 10 cm

third side = ~~42~~  $42 - (18 + 10)$

$$\Rightarrow 42 - 28$$

$$\Rightarrow 14 \text{ cm}$$

Area of triangle =

$$s = \frac{42}{2} = 21 \text{ cm}$$

$$\text{Area} = \sqrt{21(21-18)(21-10)(21-14)} \text{ cm}^2$$

$$= \sqrt{21 \times 3 \times 11 \times 7} \text{ cm}^2$$

$$\Rightarrow \sqrt{3 \times 7 \times 3 \times 11 \times 7} \text{ cm}^2$$

$$\Rightarrow 3 \times 7 \sqrt{11} \text{ cm}^2$$

$$\Rightarrow 21\sqrt{11} \text{ cm}^2$$

Q5) let the three sides be  $12n$ ,  $17n$ ,  $25n$ .  
Perimeter = 540 cm.

$$\Rightarrow 12n + 17n + 25n = 540$$

$$\Rightarrow 54n = 540$$

$$\Rightarrow n = \frac{540}{54}$$

$$\Rightarrow n = 10$$

$$\text{Sides} = 12 \times 10 = 120 \text{ cm}$$

$$17 \times 10 = 170 \text{ cm}$$

$$25 \times 10 = 250 \text{ cm}$$

Area of triangle =

$$s = \frac{120 + 170 + 250}{2} = \frac{540}{2} = 270 \text{ cm}$$

$$\begin{aligned}
 \text{Area} &= \sqrt{(270)(270-120)(270-170)(270-250)} \text{ cm}^2 \\
 &= \sqrt{270 \times 150 \times 100 \times 20} \text{ cm}^2 \\
 &= \sqrt{3 \times 3 \times 3 \times 2 \times 5 \times 3 \times 5 \times 2 \times 5 \times 2 \times 5 \times 2 \times 2 \times 5} \text{ cm}^2 \\
 &= 3 \times 3 \times 2 \times 5 \times 2 \times 5 \times 2 \times 5 \text{ cm}^2 \\
 &= 9000 \text{ cm}^2
 \end{aligned}$$

Example

2. Sides of park = 120m, 80m, 50m

$$s = \frac{120 + 80 + 50}{2} \Rightarrow s = \frac{250}{2} = 125 \text{ m}$$

$$\begin{aligned}
 \text{Area} &= \sqrt{125(125-120)(125-80)(125-50)} \text{ cm}^2 \\
 &= \sqrt{125 \times 5 \times 45 \times 75} \text{ cm}^2 \\
 &= \sqrt{5 \times 5 \times 5 \times 5 \times 3 \times 3 \times 5 \times 3 \times 5 \times 5} \text{ m}^2 \\
 &\Rightarrow 5 \times 5 \times 3 \times 5 \sqrt{3 \times 5} \text{ m}^2 \\
 &\Rightarrow 375\sqrt{15}
 \end{aligned}$$

$$\begin{aligned}
 \text{Perimeter} &= 120 + 80 + 50 \\
 &= 250 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 \text{Length of wire needed} &= 250 - 3 \text{ m} \\
 &= 247 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 \text{Cost of fencing} &= ₹ 20 \times 247 \\
 &= ₹ 4940
 \end{aligned}$$

3. Let the side of a triangle be  $3n$ ,  $5n$ ,  $7n$ .  
Perimeter = 300m

$$3n + 5n + 7n = 300 \text{ m}$$

$$\Rightarrow 15n = 300 \text{ m}$$

$$\Rightarrow n = \frac{300}{15}$$

$$\Rightarrow n = 20 \text{ m}$$

$$\text{Sides} = 3 \times 20 = 60 \text{ m}$$

$$5 \times 20 = 100 \text{ m}$$

$$7 \times 20 = 140 \text{ m}$$

$$s = \frac{60 + 100 + 140}{2} = \frac{300}{2} = 150$$

$$\text{Area} = \sqrt{150(150-60)(150-100)(150-140)}$$

$$= \sqrt{150 \times 90 \times 50 \times 1}$$

$$= \sqrt{3 \times 5 \times 2 \times 5 \times 3 \times 3 \times 2 \times 5 \times 5 \times 2 \times 5 \times 1}$$

$$\Rightarrow 5 \times 2 \times 3 \times 5 \sqrt{3 \times 2 \times 5}$$

$$\Rightarrow 150\sqrt{30}$$