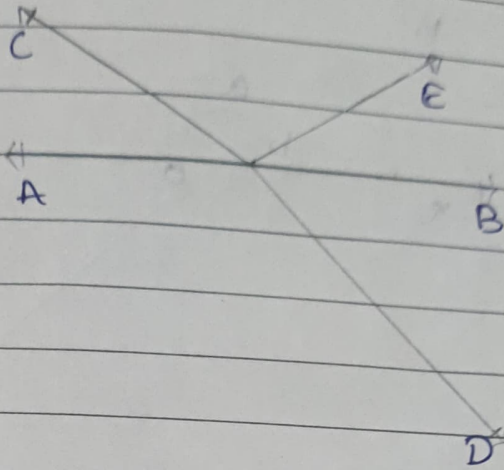


- (1) In given figure, lines AB and CD intersect at O. If  $\angle AOC + \angle BOE = 70^\circ$  and  $\angle BOD = 40^\circ$ , find  $\angle BOE$  and reflex  $\angle COE$ .



Ans. AB is straight line, rays OC and OE stand on it.

$$\text{① } \angle AOC + \angle COE + \angle BOE = 180^\circ$$

$$(\angle AOC + \angle BOE + \angle COE) = 180^\circ$$

$$70^\circ + \angle COE = 180^\circ$$

$$\angle COE = 180^\circ - 70^\circ = 110^\circ$$

$$\text{Reflex } \angle COE = 360^\circ - 110^\circ = 250^\circ$$

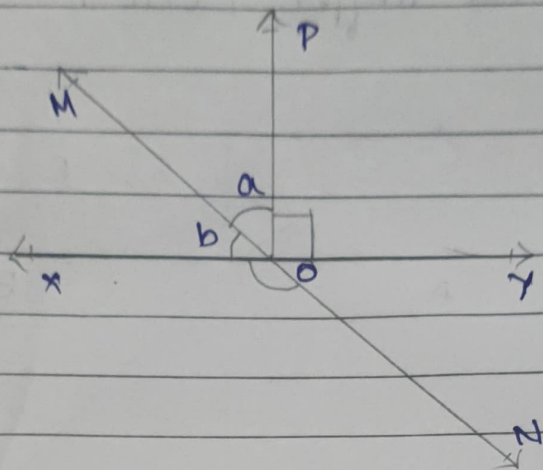
CD is a straight line, rays OE and OB stand on it.

$$\angle COE + \angle BOE + \angle BOD = 180^\circ$$

$$\Rightarrow 110^\circ + \angle BOE + 40^\circ = 180^\circ$$

$$\Rightarrow \angle BOE = 180^\circ - 150^\circ = 30^\circ$$

2. In the ~~given~~ given figure, lines XY and MN intersect at O. If ~~∠POY = 90°~~  $\angle POY = 90^\circ$  and  $a:b = 2:3$ , find C.



Ans Let the common ratio between a and b be  $x$ .

$$a = 2x \text{ and}$$

$$b = 3x$$

XY is a straight line, rays OM and OP stand on it.

$$\therefore \angle XOM + \angle MOP + \angle POY = 180^\circ$$

$$b + a + \angle POY = 180^\circ$$

$$3x + 2x + 90^\circ = 180^\circ$$

$$5x = 90, \quad x = 18^\circ$$

$$a = 2x = 2 \times 18 = 36^\circ$$

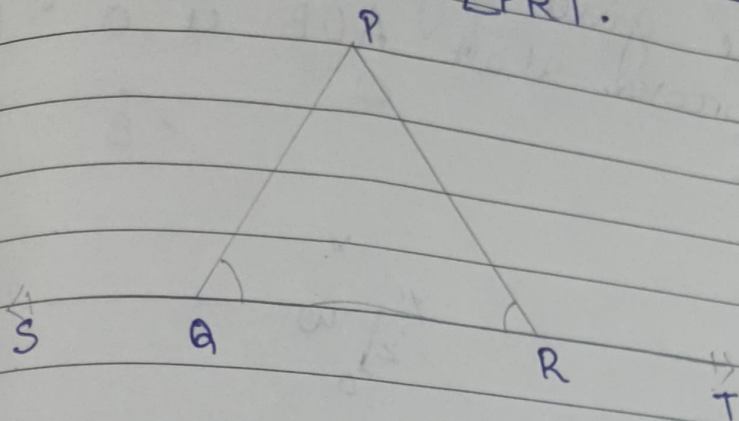
$$b = 3x = 3 \times 18 = 54^\circ$$

MN is a straight line, Ray OX stands on it.

$$\therefore b + c = 180^\circ, \quad 54^\circ + c = 180^\circ$$

$$\therefore c = 180^\circ - 54^\circ = 126^\circ, \quad c = 126^\circ$$

3. In the given figure,  $\angle PAR = \angle PRA$ , then prove that  $\angle PQS = \angle PRT$ .



Ans In the given figure, ST is a straight line and ray AP stands on it.

$$\therefore \angle PQS + \angle PAR = 180^\circ$$

$$\angle PAR = 180^\circ - \angle PQS \rightarrow (1)$$

$$\angle PRT + \angle PRA = 180^\circ$$

$$\angle PRA = 180^\circ - \angle PRT \rightarrow (2)$$

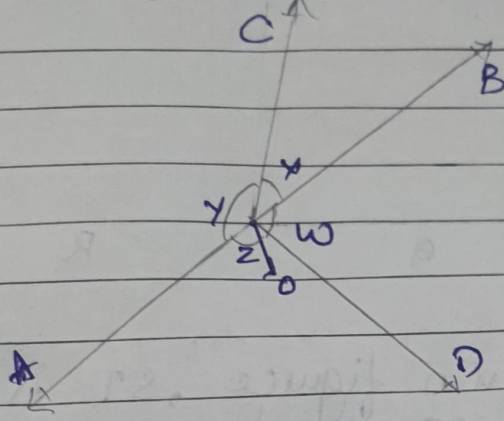
It is given that  $\angle PAR = \angle PRA$ .

Equating equations (1) and (2), we obtain,

$$180^\circ - \angle PQS = 180^\circ - \angle PRT$$

$$\angle PQS = \angle PRT$$

4. In the given figure, if  $x + y = w + z$ , then prove that  $AOB$  is a line.



Ans. It can be observed that,

$$x + y + z + z = 360^\circ$$

It is given that

$$x + y = z + w$$

$$\therefore x + y + x + y = 360^\circ$$

$$2(x + y) = 360^\circ$$

$$x + y = 180^\circ$$

Since  $x$  and  $y$  form a linear pair,  $AOB$  is a line.